

# QUALITATIVE AND QUANTITATIVE PROBABILISTIC TEMPORAL REASONING *for Industrial Applications*

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**Abstract:** Many real-world domains, such as industrial diagnosis, require an adequate representation that combines uncertainty and time. Research in this field involves the development of new knowledge representation and inference mechanisms to deal with uncertainty and time. Current temporal probabilistic models become too complex when used for real world applications. In this paper, we propose a model, Temporal Events Bayesian Networks (TEBN), based on a natural extension of a simple Bayesian network. TEBN tries to make a balance between expressiveness and computational efficiency. Based on a temporal node definition, causal-temporal dependencies are represented by qualitative and quantitative relations, using different time intervals within each variable (multiple granularity). Qualitative knowledge about temporal relations between variables is used to facilitate the acquisition of the quantitative parameters. The inference mechanism combines qualitative and quantitative reasoning. The proposed approach is applied to a thermal power plant through a detailed case study, with promising results.

## 1 INTRODUCTION

In the last years the operating conditions of thermal power plants have changed. Today, the operation of thermal power plants must be optimal considering higher productions profits, safer operation and stringent environment regulation. An additional factor is the increment of the age of the plants. The reliability and performance of the plants is affected by its age. This means an increase in the number of equipment failures, thus increasing the number of diagnoses and control decisions which the human operator must make. Under these conditions the complexity of the operation of thermal power plants has been increased significantly.

As a result of these changes, the computer and information technology have been extensively used in thermal plant process operation. Distributed control systems (DCS) and information management systems (IMS) have been playing an important role to show the plant status. However, in nonroutine operations such as equipment failures and extreme operation (start up phase, changes in the load, etc.), human operators have to rely on their own experience. During disturbances, the operator must determine the best recovery action according to the

type and sequence of the signals received. In a major upset, the operator may be confronted with a large number of signals and alarms, but very limited help from the system, concerning the underlying plant condition. Faced with vast amount of raw process data, human operators find it hard to contribute a timely and effective solutions.

The process industry demands new computer integrated technologies that reduce operator's working burden by providing operation support systems. Process operations are knowledge-intensive work tasks because thermal plants are large, complex and influenced by unexpected disturbances and events over time. Artificial Intelligent applications and expert systems in particular, are recognized as providing efficient solutions to a wide range of industrial problems.

Artificial intelligence applications are showing a trend toward real world domains, such as medicine, real-time diagnosis, communications, planning, financial forecasting and scheduling. These applications have revealed a great need for powerful methods for knowledge representation. In particular, the evolutionary nature of these domains requires a representation that takes into account temporal information. The exact timing information for things like lab-test results, occurrence of symptoms,

observations, measures, as well as faults, can be crucial in this kind of applications.

Aside from temporal considerations, the world domain knowledge is imprecise, incomplete and not deterministic. The temporal model must be able to deal with uncertainty. Among the many formalism proposed for dealing with uncertainty, one of the most used techniques for the development of intelligent systems are probabilistic networks, also known as Bayesian Networks, causal networks or probabilistic influence diagrams. Bayesian networks (BN) are a robust and sound formalism to represent and handle uncertainty in intelligent systems in a way that is consistent with the axioms of probability theory (Pearl, 2000). Although BN were not designed to model temporal aspects explicitly, recently Bayesian networks have been applied to temporal reasoning under uncertainty (Santos 1996; Arroyo and Sucar, 1999, Galan and Diez 2002). Prior temporal modeling techniques have often made a trade-off in expressiveness between semantics for time and semantics for uncertainty. Therefore, to integrate uncertainty and time, it's necessary a combined approach integrating strong probabilistic semantics for representing uncertainty and expressive temporal semantics for representing temporal relations.

In this paper, we present the definition and application of an approach for dealing with uncertainty and time called Temporal Event Bayesian Network, based on a natural extension of a simple Bayesian network. TEBN tries to make a balance between expressiveness and computational efficiency. Based on a temporal node definition, causal-temporal dependencies are represented by qualitative and quantitative relations, using different time intervals within each variable (multiple granularity). The inference mechanism combines qualitative and quantitative reasoning. The proposed approach is applied to the diagnosis and prediction of events and disturbances (events sequence) to assist the operator in real time assessment of plant disturbances, and in this way contribute to the safe and economic operation of thermal power plants.

## 2 DEFINITION OF A TEBN.

Temporal Event Bayesian Network (TEBN) allows the representation of temporal and atemporal information in a probabilistic framework. A TEBN is capable of representing each variable with its interactions over multiple points of time. The domain is defined over time intervals. The state of the domain is represented by a value at a given time interval. Santos (Santos 1996) use a similar concept, but they used the time interval only as a temporal constraint. In our approach,

a time interval is an additional component of the network.

TEBN make a balance between the robust semantics of Bayesian Networks and the expressive temporal semantics of the interval algebra. The temporal expressiveness is defined by the time intervals. The balance between the exactness and the complexity of the temporal model is a function of the numbers of time intervals.

Intuitively, a temporal node consists of a set of states or values, e.g. {true, false}, {occur, does not occur}, {high, normal, low}, that the variable or event can take, and a set of temporal intervals associated to each state or value of the variable or event.

**Definition 1.** A *Temporal Node (TN)* is an ordered pair  $(E, I)$  in which  $E$  is a set of states or values of a random variable, and  $I$  is a set of time intervals associated to each state or value of the variable.

**Definition 2.** A causal-temporal relationship (*CTR*) describes a relationship between two temporal nodes  $A(Ea, Ia)$  and  $B(Eb, Ib)$ , where  $A$  is considered the "cause" and  $B$  is considered the "effect". Formally, the *CTR* is written as  $A(R, P)B$  where  $R$  is the set of temporal qualitative relationship between the time intervals, and  $P$  is the causal-temporal quantitative relationship, defined as a conditional probability matrix. Graphically, a *CTR* is represented by a directed edge from the cause node to the effect node, labeled with  $R$ , with a joint probability distribution  $P$ .

A Temporal Event Bayesian Network is a directed acyclic graph, which consists of finite set of temporal nodes and a finite set of causal-temporal relationships.

**Definition 3.** A *TEBN* is an ordered pair,  $(N, T)$ , where  $N$  is a set of temporal nodes and  $T$  is set of causal-temporal relationships given by  $R$  and  $P$ . Then  $EBN=(E, I, R, P)$  is called a Temporal Event Bayesian Network.

The TEBN model has two reasoning mechanisms: qualitative and quantitative temporal-causal reasoning. Qualitative reasoning is based on the interval algebra [Allen, 1983]. It is important to know the qualitative information about the timing relationships between the events. The qualitative reasoning has two levels of abstraction. In a superior level, we use a simplified temporal diagram of the history of the process using Allen's representation in order to define the general relation between the temporal range of occurrence of the events. In an inferior level, we apply the transitivity algorithm to get the temporal relations between each time interval that defines the temporal node. Qualitative reasoning permits an early diagnosis of the domain based on the temporal consistency. This early diagnosis gives

a preliminary idea about state of domain. The qualitative mechanism is explained in more detail in the example of the next section.

The quantitative reasoning mechanism is based on probability propagating. The method for propagating probabilities of a TEBN is an extension of the polytree and multiconnected algorithms proposed in the literature (Pearl, 2000). For some evidence  $e$  at the time interval  $u$  the posterior probability of a variable  $B$  is as follows:

$$P((b_i, o_j) | (e, u_k)) = \frac{P(e, u_k | b_i, o_j) P(b_i, o_j)}{P(e, u_k)}$$

where  $P((b_i, o_j) | (e, u_k))$  is the probability associated to the value  $b_i$  in time interval  $o_j$  given the evidence  $e$  in the time interval  $u_k$ .

The reasoning in TEBN consists in instantiating the input temporal variables (this can be any variable into the network) and propagating their effect through the network to update the probability of the hypothesis variables (diagnosis and prediction). The reasoning mechanism starts when a temporal variable is instantiated, and the probability of all temporal nodes is update. The quantitative reasoning gives the state of the domain with some probability value.

The qualitative knowledge about temporal relations between temporal nodes is relatively easy to obtain from domain experts. With this knowledge is possible to know the temporal relations between events and this is used to facilitate the acquisition of the quantitative parameters (conditional probabilities). For instance, given a particular qualitative relation between nodes A and B, some values in the conditional probability matrix,  $P(B/A)$ , are set to zero.

### 3 AN EXAMPLE OF APPLICATION

As an illustrative example, we present the drum level disturbance when a power load increment occurs. The drum is a subsystem of a thermal power plant. This subsystem provides steam to the superheater and water to the water wall of a steam generator. Figure 1 shows a simplified diagram of a drum system in a thermal power plant. For the proposes of demonstration, assume the following hypothetical case.

"The drum is a tank with a steam valve at the top, a feedwater valve at the bottom, a feedwater pump which provides water to the drum and a level control system. The drum level (DRL) can increase by the increase of the feedwater flow (FWF). The feedwater flow can increase by two main causes: the augmentation in the current of feedwater pump

(FWP) and the increase of the opening of the feedwater valve (FWV). This will lead to an increase in drum level to a dangerous level. The operator must open the steam valve in order to increase the steam flow. This will lead to a reduction of the water drum level in the drum tank so that the level will decrease to safe levels. Both disturbance can lead to down thermal power plant".

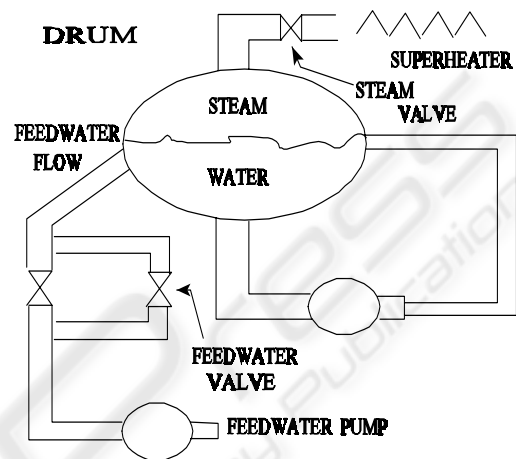


Figure 1: Steam Generator Drum system.

In the process, a signal exceeding its specified limit of normal functioning is called as an *event*, and a sequence of events that have the same underlying cause are considered as a *disturbance*. In the example, the feedwater flow (FWF) can be caused by two different disturbances: a power load increment or a control system failure. These disturbances are characterized respectively by the feedwater current augmentation (+FWP) and feedwater opening increase (+FWV).

To determine which of both disturbances are present is a complicated task. We need additional information to determine which it is the real cause. One of these is the temporal information. We can select the hypothesis of failure according to the time interval in which the disturbance occurs. The dynamic of the FWP is faster than the dynamic of the FWV. In order to reason about the sequence of facts and disturbances that occur, we require a temporal representation.

The knowledge representation uses the Allen's interval algebra (Allen, 1983) and its thirteen relations as temporal basis definition and a probabilistic framework for dealing with quantitative uncertainty. Figure 2 and table 1, depict a small TEBN with five temporal nodes, four edges, temporal relations between nodes and *a priori* probabilities. Each temporal node is associated to its time intervals., all nodes except the node *steam valve* have two time intervals. The formalism is

based on the probability of the event occurrence at a time interval. In this case, the TEBN is an event network (occurs or does not occur): the event occurs at the time interval one (for example FWP, O1); the event occurs at the time interval two (FWP, O2); and the event does not occur (FWP). The events might occur only in single time interval.

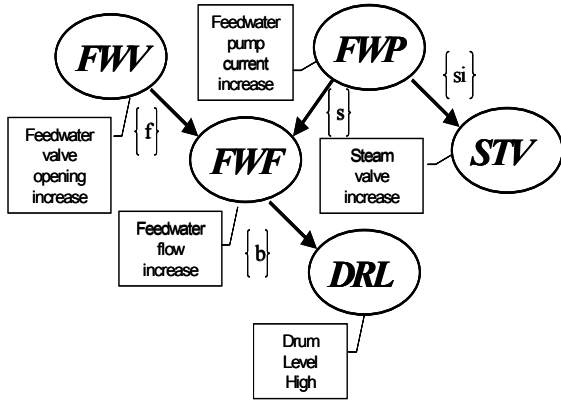


Figure 2: TEBN for Drum system example.

Table 1: Event probabilities for TEBN

Event Probabilities	
FWV, I1	0.30
FWV, I2	0.60
-FWV	0.10
FWP, O1	0.60
FWP, O3	0.30
-FWP	0.10
FWF, U1	0.51
FWF, U2	0.48
-FWF	0.01
STV, Q1	0.47
STV, Q2	0.29
STV, Q3	0.12
-STV	0.12
DRL, R1	0.51
DRL, R2	0.48
-DRL	0.01

#### 4 PROCESS DIAGNOSIS EXAMPLE

In this section we present the application of the TEBN model for diagnosis of disturbances in the drum system depicted in section three. According to the example, there are two possible causes of an increase in the feedwater flow (FWF): an

augmentation in feedwater pump current and an increase in the opening of the feedwater valve.

Figure 3 and figure 4 show the simplified temporal diagram and the consistent scenario of the drum level disturbance. These diagrams define the qualitative temporal relation between the time range of event occurrence. For instance the temporal relation between the temporal range of FWP and FWF is *start* and the temporal relation between the temporal range of FWV and FWF is *finishes*.

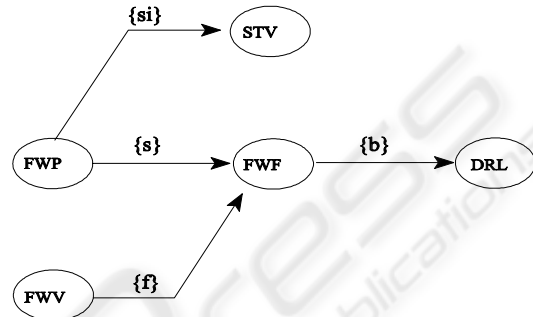


Figure 3: Simplified temporal diagram of the drum system.

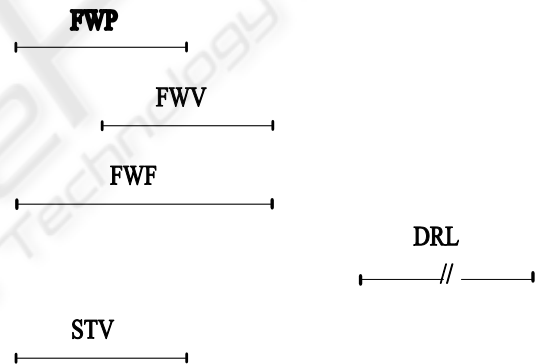


Figure 4: Temporal consistent scenario of the drum system.

Figure 5, shows the temporal relations between the time intervals of node FWP and node FWF. The intervals at the top, O1 and O2 represent the time intervals of FWP and the intervals U1 and U2 represent the time interval of the FWF. The relations between the four intervals are shown in the right. These relations can be obtained for each pair of nodes. Both diagrams, permits to made a preliminary selection of hypotheses and give an initial idea about the disturbance (faulty) that occurs. For this the time relations are considered, which produce a set of temporal constraints that permit to select some hypotheses using a consistency algorithm.

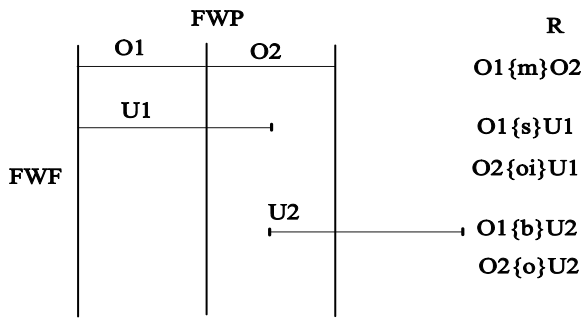


Figure 5: Temporal relations between the FWP and FWF time intervals

Quantitative reasoning in the TEBN gives the most probable hypotheses. The causal-temporal relationships between events are used for determining the most probable cause (disturbance). For instance, the figure 6 depicts the case when the event *drum level high* (DRL) occurs in the time interval R1. In this case the most probable cause is a feedwater pump current augmentation (+FWP). This disturbance may be characterized by a power load increase.

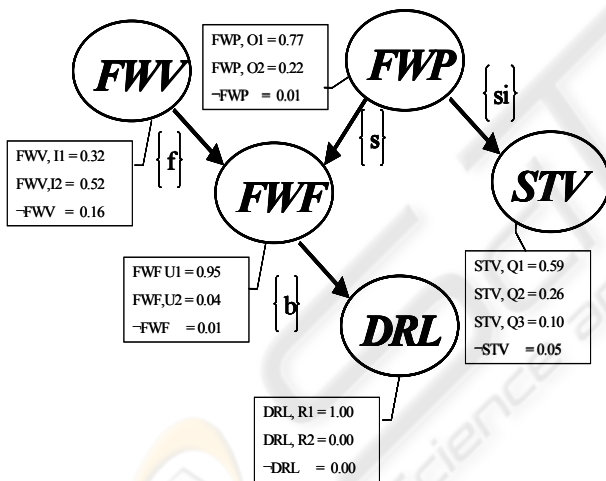


Figure 6: The drum level high occurs at the time interval R1

Figure 7 depicts the case when the *drum level high* (DRL) occurs in the time interval R2. In this case the most probable cause is an increase in the opening of the feedwater valve. This disturbance may be characterized by a failure in the level control system. To confirm which is the most probable disturbance is needed the time of occurrence of the increase of feedwater flow. This reasoning makes it possible to answer questions such as: “The event *drum level high* occurred 1:30 minutes after that the feedwater flow increase occurred. What is the most probable disturbance (cause)?”.

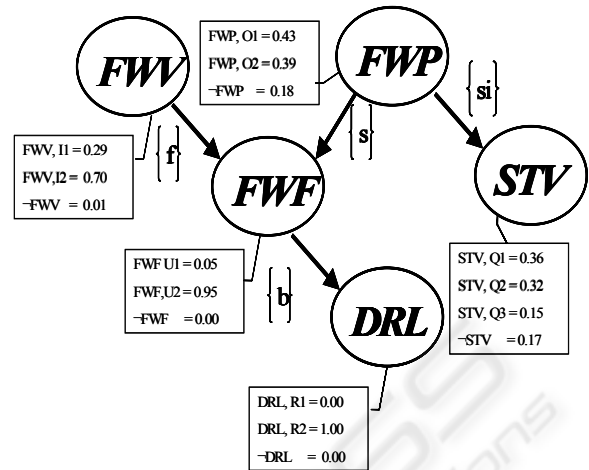


Figure 7: The drum level high occurs at the time interval R2

In this model, the time range definition of the intervals is independent of the hour of the day. In many real-domains the events do not occur as a function of the day hour. Under this situation, the TEBN is a model relative, not absolute. The reasoning mechanism starts when any event in the network is detected. The time interval definition is only dependent of the causal-temporal relationships between the events.

The use of qualitative reasoning mechanism permits an early diagnosis. The early diagnosis gives a preliminary idea of the events and disturbance that occurred. The quantitative reasoning gives the occurrence of events and disturbances with some probability values. The TEBN has been applied into two systems of a steam generator: drum level system and condenser system. The result obtained in this two subsystems indicate that it can be useful for many uncertainty temporal reasoning tasks that involve prediction and diagnosis in real complex environments (Arroyo et al., 2000).

## 5 EMPIRICAL EVALUATION

Table 2 summarizes the results of simulating failures for the four disturbances of the feedwater and superheater systems. The process data was generated by a full scale simulator of a thermal power plant. We selected 80% of this data-base (800 registers) for parameter learning and 20% (200 registers) for evaluation. The model was evaluated empirically using two scores: accuracy and a measure based on the Brier score (total square error). The Brier score is defined as:  $BS = \sum_{i=1}^n (1 - P_i)^2$ .  $P_i$  is the marginal posterior probability of the correct value of each node

given the evidence. The maximum Brier score is:  $BS_{MAX} = \sum^n (1)^2$ . A relative Brier score is defined as:  $RBS \text{ (in \%)} = \{1 - (BS / BS_{MAX})\} \times 100$ .

The results of the evaluation are shown in terms of the mean and the standard deviation for both scores. These results show the prediction and diagnosis capacity of the temporal model in a real process. Both scores are between 80 and 97% for all the set of tests, with better results when intermediate nodes are observed, and slightly better results for prediction compared to diagnosis. We consider that these differences have to do with the “distance” between assigned and unknown nodes and with the way that the temporal intervals were defined. We are encouraged by the fact that the model can produce a reasonable accuracy in times that are compatible with real time decision making.

Table 2: Empirical evaluation results

Parameter	$\mu$	$\sigma$
Prediction		
% of RBS	87	9.19
% of accuracy	84	14.98
Diagnosis		
% of RBS	84	8.09
% of accuracy	80	11.85
Diagnosis and prediction		
% of RBS	96	4.71
% of accuracy	95	8.59

## 6 CONCLUSIONS

The TEBN generates a formal and systematic structure used to model the temporal evolution of dynamics domains. TEBN is a hybrid model that combines a qualitative representation based on interval algebra with a quantitative representation based on a natural extension of Bayesian networks. Each event or variable occurrence is associated with a time interval. The definition of the numbers of time intervals for each variable is free (multiple granularity) and can be seen as a trade off between the complexity and the accuracy needed for depicting the knowledge of the temporal domain.

The model combines qualitative and quantitative causal-temporal reasoning mechanisms. The qualitative reasoning mechanism is based on the interval algebra and permits an early diagnosis. The early diagnosis gives a preliminary idea about of process state. The quantitative reasoning mechanism is based on the propagation of probabilities and gives the occurrence of events and disturbances with some probability values.

The formalism satisfies the requirements of temporal knowledge acquisition, low computational cost and temporal expressiveness. The qualitative knowledge about temporal relations between temporal nodes is relatively easy to obtain from domain experts and is used to facilitate the acquisition of the quantitative parameters (conditional probabilities).

Our future work will be focused on developing and integrating an intelligent support system (ISS) to aid the operation of human operators of thermal power plants. The ISS will be integrate by four modules: signal validation, supervisory system, diagnostic system, and planning systems. The ISS will be used to assist an operator in real-time assessment of plant disturbances and in this way contribute to the safe and economic operation of power plants.

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