

REAL-TIME POSITION CONTROL OF A PNEUMATIC SYSTEM USING MODEL PREDICTIVE CONTROL

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Abstract: Studies on the precise control applications with pneumatic systems have been growing in recent years. In addition to this, due to the complexity and non-linearity of the system the expected performance will only be gained by applying modern control strategies. So the subject of this paper is identification and real-time model predictive control of a pneumatic system. In order to realise system identification, a white noise signal is sent to the plant and the displacement outputs are stored. Afterwards these data are digitally processed and the parametric single-input single-output step response model is obtained. In the previous study on this system with a PD controller, a steady-state error is observed. In order to eradicate this, a Model Predictive Control – Dynamic Matrix Control algorithm is applied. To run this, in real-time, a programme is written in Matlab - Simulink and by using the code generated by Matlab - Real-Time Workshop, the real-time position control of the system is performed.

1 INTRODUCTION

Pneumatics technology is preferred in industry because it has relatively lightweight and cheap components. Pneumatic actuators are extensively used in position control applications with open-loop control mode where the strokes of the moving parts are fixed by the mechanical stops. A closed-loop control system is generally not common due to the problems arising from air compressibility, poor damping ability, mechanical frictions, nonlinearities etc. Because of these regulations studies on the precise control applications with pneumatic systems employing advanced control techniques of sliding mode control, variable structure control, PWM control, adaptive tracking control etc. instead of conventional PID have been increased in recent years. In this paper we present a scheme to use one of the most popular control strategies, model predictive control, in order to control the system precisely.

2 PNEUMATIC SYSTEM MATHEMATICAL MODEL

Pneumatics system mathematical model consists of two parts: The first part is piston dynamics defining motion of the piston, carriage and payload masses, the second is thermodynamical pressure dynamics defining pressure variations in the chambers according to piston motion and air mass flow rate, which depends on valve dynamics [1, 2].

2.1 Piston Dynamics

The dynamics of piston motion is described by:

$$M \ddot{x} + B \dot{x} + F_{df} = A(P_1 - P_2) \quad (1)$$

where M is the total moving mass, x is the position of the piston, B is the viscous-friction coefficient, F_{df} is the dry friction forces (static or dynamic according to piston velocity), A is the piston cross-sectional area of the rodless cylinder and P_1, P_2 are the chamber air pressures, as shown on Figure 1.

$$\frac{M}{A} \ddot{x} + \frac{B}{A} \dot{x} = (P_1 - P_2) - \frac{F_{df}}{A} \quad (2)$$

Where $\frac{F_{df}}{A}$ is the pressure equivalent of the dry friction force [7].

$$\dot{v} = -\frac{B}{M}v + \frac{A}{M}\Delta P_{net} \quad (3)$$

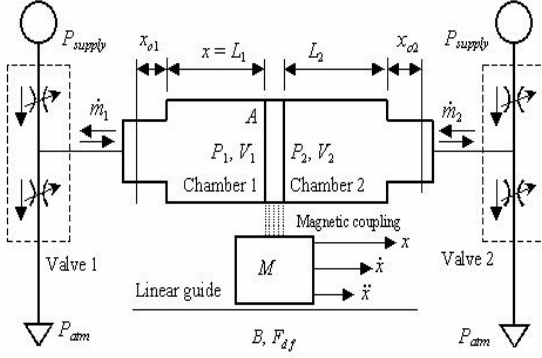


Figure 1: Schematic diagram of pneumatic system.

Where $v = \dot{x}$ and

$$\Delta P_{net} = (P_1 - P_2) - \frac{F_{df}}{A} \quad (4)$$

2.2 Pressure Dynamics

The dynamics of pressures P_1 and P_2 can be expressed as [3]:

$$\dot{P}_1 = \frac{f_1}{(x_{o1} + x)} S_1 - \gamma \frac{P_1}{(x_{o1} + x)} \dot{x} \quad (5a)$$

$$\dot{P}_2 = \frac{f_2}{(L + x_{o2} - x)} S_2 + \gamma \frac{P_2}{(L + x_{o2} - x)} \dot{x} \quad (5b)$$

$$L = L_1 + L_2 \quad (6)$$

Where S_1 and S_2 are the valve cross-sectional areas, γ is the ratio of specific heats, L is the stroke of the piston (L_1 and L_2 are shown in Figure 1), x_{o1} and x_{o2} are the position increments for dead volumes of the chambers, f_1 and f_2 are nonlinear functions of the form

$$f_1 = \frac{\gamma T_1}{A} \sqrt{\frac{2R}{T_1}} P_{u1} Y_1 \left(\frac{P_{d1}}{P_{u1}} \right) \quad (7a)$$

$$f_2 = \frac{\gamma T_2}{A} \sqrt{\frac{2R}{T_2}} P_{u2} Y_2 \left(\frac{P_{d2}}{P_{u2}} \right) \quad (7b)$$

Here R is the universal gas constant, T_1 and T_2 are the temperatures of the air inside the chambers, and are assumed to be constant, P_{ui} and P_{di} are upstream and downstream pressures respectively ($i = 1, 2$). And,

$$Y_i(r_i) = \sqrt{\frac{\gamma}{\gamma+1}} \sqrt{(2/(\gamma+1))^{2/(\gamma-1)}} \quad \text{for} \quad 0 \leq r_i \leq 0.528 \quad (8a)$$

$$Y_i(r_i) = \sqrt{\frac{\gamma}{\gamma-1}} \sqrt{r_i^{2/\gamma} - r_i^{(\gamma+1)/\gamma}} \quad \text{for} \quad 0.528 < r_i \leq 1 \quad (8b)$$

Where

$$r_i = \frac{P_{di}}{P_{ui}}$$

P_{ui} and P_{di} are assumed to take the values in Table I according to operation of the valves.

The input signals applied to the valves control the chamber reference pressures instead of orifice areas as the valves are of servo operation through pressure feedback.

$$S_i = k_i (P_{iref} - P_i) \quad (i = 1, 2) \quad (9)$$

Where P_{iref} is the reference pressure for the i -th chamber and k_i is the coefficient for i -th valve.

TABLE I

P_{ui} AND P_{di} VALUES

Valve no (i)	Valve operation	P_{ui}	P_{di}
1	Connected to supply	P_{supply}	$0.9P_1$
	Open to the atmosphere	P_1	$0.9P_{atm}$
2	Connected to supply	P_{supply}	$0.9P_2$
	Open to the atmosphere	P_2	$0.9P_{atm}$

The relationship between the input voltage and output reference pressure is described by

$$P_{iref} = a_i + b_i u_i \quad u_i > a_{oi} \quad (i = 1, 2) \quad (10a)$$

$$P_{iref} = P_{atm} \quad 0 \leq u_i \leq a_{oi} \quad (i = 1, 2) \quad (10b)$$

Where a_i , b_i and a_{oi} are constant values, u_i is the input voltage for i -th valve.

3 MODEL PREDICTIVE CONTROL

Model Predictive Control refers to a class of algorithms that compute a sequence of manipulated variable adjustments in order to optimize the future behaviour of a plant. So the term Model Predictive Control does not designate a specific control strategy but a very ample range of control methods which make an explicit use of a model of the process to obtain the control signal by minimizing an objective function. In this study we used one of these methods named Dynamic Matrix Control (also called "Cutler's Method"). The process model employed in this formulation is the step response of the plant, while the disturbance is considered to obtain constant along the horizon. The procedure to obtain the predictions is as follows:

As a step response model is employed:

$$y(t) = \sum_{i=1}^{\infty} g_i \Delta u(t-i) \quad (11)$$

the predicted values along the horizon will be:

$$\begin{aligned} \hat{y}(t+k | t) &= \sum_{i=1}^{\infty} g_i \Delta u(t+k-i) + \hat{n}(t+k | t) \\ &= \sum_{i=1}^k g_i \Delta u(t+k-i) + \sum_{i=k+1}^{\infty} g_i \Delta u(t+k-i) + \\ &\quad + \hat{n}(t+k | t) \end{aligned} \quad (12)$$

Disturbances are considered to be constant, that is $\hat{n}(t+k | t) = \hat{n}(t | t) = y_m(t) - \hat{y}(t | t)$. Then it can be written that:

$$\begin{aligned} \hat{y}(t+k | t) &= \sum_{i=1}^k g_i \Delta u(t+k-i) + \\ &+ \sum_{i=k+1}^{\infty} g_i \Delta u(t+k-i) + y_m(t) - \sum_{i=1}^{\infty} g_i \Delta u(t-i) = \\ &= \sum_{i=1}^k g_i \Delta u(t+k-i) + f(t+k) \end{aligned} \quad (13)$$

where $f(t+k)$ is the free response of the system, that is, the part of the response that does not depend on the future control actions and given by:

$$f(t+k) = y_m(t) + \sum_{i=1}^{\infty} (g_{k+i} - g_i) \Delta u(t-i) \quad (14)$$

As only a finite number of terms (N) are considered, the process is assumed to be stable and

casual and therefore the free response is computed as:

$$f(t+k) = y_m(t) + \sum_{i=1}^N (g_{k+i} - g_i) \Delta u(t-i) \quad (15)$$

If this equation is expressed in matrix form:

$$\begin{aligned} \begin{bmatrix} f(t+1) \\ f(t+2) \\ \vdots \\ f(t+k) \end{bmatrix} &= \begin{bmatrix} y_m(t) \\ y_m(t) \\ \vdots \\ y_m(t) \end{bmatrix} + \\ & \left(\begin{bmatrix} g_2 & g_3 & \dots & g_N & g_{N+1} \\ g_3 & g_4 & \dots & g_{N+1} & g_{N+2} \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ g_{k+1} & g_{k+2} & \dots & g_{k+N-1} & g_{k+N} \end{bmatrix} - \begin{bmatrix} g_1 & g_2 & \dots & g_{N-1} & g_N \\ g_1 & g_2 & \dots & g_{N-1} & g_N \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ g_1 & g_2 & \dots & g_{N-1} & g_N \end{bmatrix} \right) * \\ & * \begin{bmatrix} \Delta u(t-1) \\ \Delta u(t-2) \\ \vdots \\ \Delta u(t-N) \end{bmatrix} \end{aligned} \quad (16)$$

The prediction horizon p for the DMC algorithm is taken into account. The DMC technique allows for m consecutive changes in the input variable ($m \leq N$), m being called the control horizon. In this way the changes in the model output over the prediction horizon due to consecutive changes in the input variable over the control horizon, can be expressed as:

$$\begin{aligned} \hat{y}(t+1 | t) &= g_1 \Delta u(t) + f(t+1) \\ \hat{y}(t+2 | t) &= g_2 \Delta u(t) + g_1 \Delta u(t+1) + f(t+2) \\ &\vdots \\ \hat{y}(t+p | t) &= \sum_{i=p-m+1}^p g_i \Delta u(t+p-i) + f(t+p) \end{aligned} \quad (17)$$

Defining the system's dynamic matrix G as:

$$G = \begin{bmatrix} g_1 & 0 & \dots & 0 \\ g_2 & g_1 & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ g_m & g_{m-1} & \dots & g_1 \\ \vdots & \vdots & \ddots & \vdots \\ g_p & g_{p-1} & \dots & g_{p-m+1} \end{bmatrix} \quad (18)$$

The prediction can be computed by the general known expression:

$$\hat{y} = Gu + f \quad (19)$$

The objective of a DMC controller is to drive the output as close to the setpoint as possible in a least squares sense with the possibility of the inclusion of a penalty term on the input moves. Therefore, the manipulated variables are selected to minimize a quadratic objective that can consider the minimization of the future errors and the control effort, in which case it presents the generic form;

$$J = \sum_{j=1}^p [\hat{y}(t+j | t) - w(t+j)]^2 + \sum_{j=1}^m \lambda [\Delta u(t+j-1)]^2 \quad (20)$$

If there are no constraints, the solution to the minimization of the cost function $J = \mathbf{e}\mathbf{e}^T + \lambda\mathbf{u}\mathbf{u}^T$, where \mathbf{e} is the vector of future errors along the prediction horizon and \mathbf{u} is the vector composed of the future control increments $\Delta u(t)$, ..., $\Delta u(t+m)$, can be obtained analytically by computing the derivative of J and making it equal to 0, which provides the general result:

$$\mathbf{u} = (G^T G + \lambda I)^{-1} G^T (\mathbf{w} - \mathbf{f}) \quad (21)$$

As in all predictive strategies, only the first element of vector \mathbf{u} is really sent to the plant. It is not advisable to implement the entire sequence over the next m intervals. This is because it is impossible to perfectly estimate the disturbance vector and therefore it is also impossible to anticipate precisely the unavoidable disturbances that cause the actual output differ from the predictions that are used to compute the sequence of control actions. Furthermore, the setpoint can also change over the next m intervals.

4 SYSTEM IDENTIFICATION

In section 3, it was mentioned that DMC algorithm uses a single-input single-output step response model, to calculate the control signals. In order to obtain these model coefficients, a system identification process has been realized by using Matlab - System Identification Toolbox.

The Simulink model, which was developed for data acquisition is shown in Figure 2.

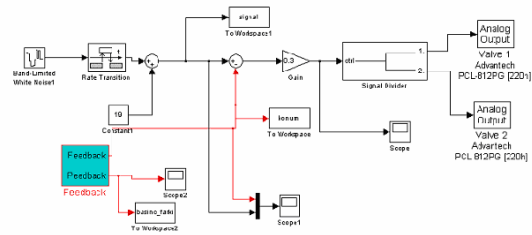


Figure 2: The Simulink Model for System Identification.

The SISO Step response Model is obtained by sending a white noise signal to the plant. The white noise signal and the response of the plant is given in Figure 3.

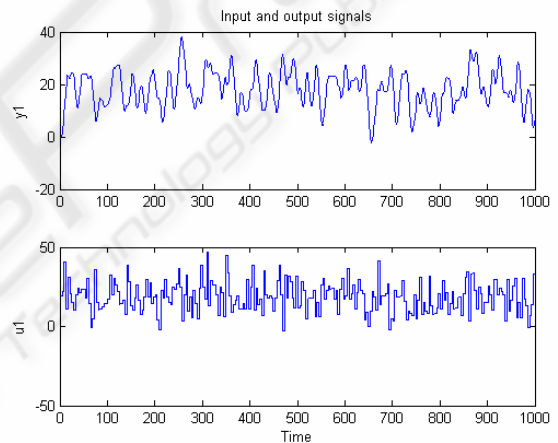


Figure 3: Input and Output Signals.

In Figure 3, u_1 is the white noise signal and y_1 is the position signal of the plant.

After the system identification process, the validation is carried out and the validation results indicate a 3rd order system model. The measured and computed values are given in Figure 4 and the unit step response of this 3rd model is given in Figure 5.

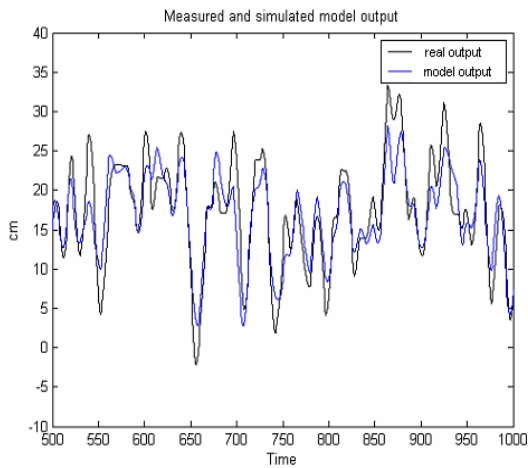


Figure 4: The Validation Results.

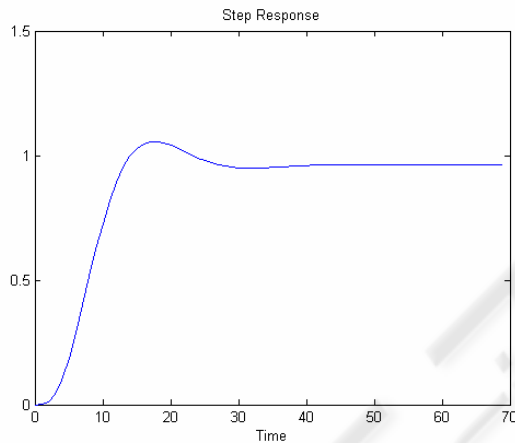


Figure 5: Unit Step Response of 3rd Order SISO Model.

5 REAL - TIME POSITION CONTROL

The feedback gain matrix was built by the step response coefficients which were calculated offline and shown in Figure 5. Afterwards the algorithm applied to the system and twelve real-time position control trials were realised. The reference trajectory for these trials is chosen as in Figure 6.

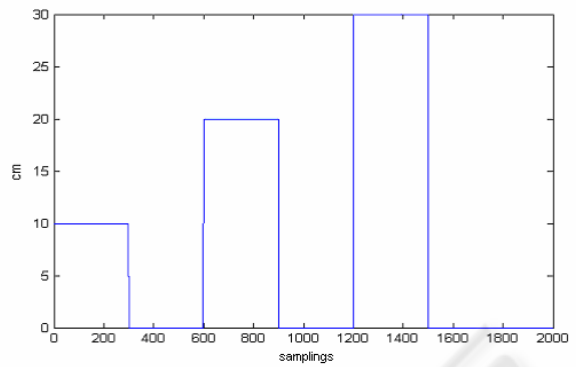


Figure 6: Reference Trajectory.

For real-time control purposes, Matlab - Simulink - Real-Time Workshop Toolbox is used. A Simulink model containing the dynamic matrix control algorithm and signal conditioners are prepared. The main block is shown in Figure 6.

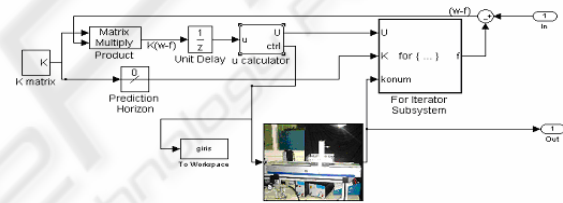


Figure 6: The Main Simulink Block

In these twelve real-time experiments, controller parameters, such as prediction horizon and control horizon, and also the coefficient lambda were changed. The optimal response is illustrated in Figure 7. Figure 8 shows the worst among these experiments.

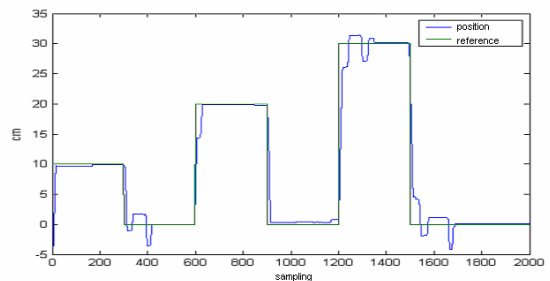


Figure 7: Optimal Response
(Prediction Horizon: 20, Control Horizon: 20,
Lambda:80)

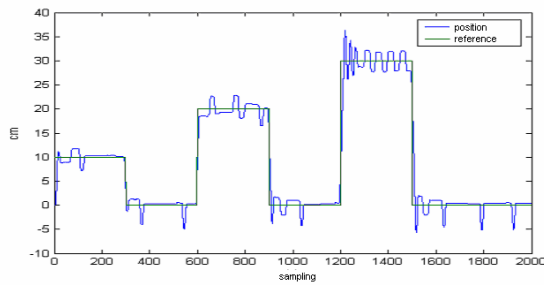


Figure 8: The Worst Response
(Prediction Horizon: 20, Control Horizon: 10,
Lambda:20)

It is observed that in some positions the system response goes away from the reference and again starts to follow. This can be explained related to the high dry friction values in those regions. In the mean time steady-state errors are eliminated by this control algorithm as seen in Figure 7.

6 EXPERIMENTAL INSTALLATION

The system consists of a magnetically coupled rodless pneumatic cylinder with high precision guide (SMC CY1HT32, stroke 0.5 m, diameter 0.032 m), two three-way electropneumatic servovalves (SMC VEP 3121), a magnetic linear scale (SONY Magnescale SR10-060A, a computer having a 1.6 GHz microprocessor, 256 MB RAM and a data acquisition card (Advantech PCL-812PG). Matlab - Simulink data acquisition software is used under Windows 98 operating system.

7 CONCLUSION

In this paper we considered a system identification and a real-time DMC position control on a pneumatic system. We observed a steady-state error from the previous studies on the same test bench with PD controller. In order to eradicate this error we used Model Predictive Control algorithm.

In Matlab software, it can be seen that there is a MPC Toolbox which cannot be used in real-time applications. So we prepared a new real-time usable Simulink algorithm for unconstrained SISO systems.

The step response coefficients, which are necessary for the DMC algorithm, were calculated off-line in this study. It can be said that a self-tuning DMC application will increase the system's performance and will efface the need of an operator.

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