

Systematic Design of Real-Time Systems Based on CSP+T Process Algebra

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Abstract. In this paper, a bottom-up formal technique to obtain a correct system specification from the RT/SA requirements specification of real-time systems is proposed. As an application, a design of the *production cell* is introduced.

1 Introduction

We present a complete bottom-up systematic specification technique in order to derive a correct system specification from a semi-formal user requirements specification in RT/SA [2], [3] by applying a set of transformation rules. The proposed technique integrates two complementary approaches to describe a real-time system: (1) RT/SA based notations, and (2) *CSP+T* [4] process terms to model real-time processes including the specification of their timing requirements.

A semantic interpretation of RT/SA entities must be flexible enough to accept alternative interpretations of some analysis entities in order to maintain the adaptability of RT/SA to different modeling cases [1]. Thus, our method does not fix a particular semantics, when there are different possibilities to solve a given ambiguity of RT/SA and it is up to the analyst to select the most convenient notation semantics depending on the system to be specified. This feature of the method is a result of the flexibility provided by *CSP+T* design notation.

2 Real-Time Systems Specification with CSP+T

The use of extensions of algebraic process description languages such as *Timed CSP* or *CSP+T* gives a precise and flexible semantics to *RT/SA* entities. *CSP+T* description language is a powerful notation to specify deterministic processes with time constrained behavior. There are only a few new operators, which are mainly related to the specification of time, in *CSP+T* with respect to those offered by *CSP*.

A new operator \star (star) is introduced to denote process instantiation. This event is unique in the system since it represents the origin of a global time at which the processes start their execution.

The event operator $\triangleright\triangleleft$ is used jointly with a variable to record the time instant at which the event occurs. The variables associated with this operator are called *marker variables* and their scope is strictly limited to one sequential process. Each event is associated with the *event enabling interval* during which the event is available for

communication between the process and its environment, and is relative to a preceding event. The following term is an example of a process written in $CSP+T$.

$$P = 0. \star \rightarrow [1, 2] a \triangleright \langle \nu \rightarrow \text{STOP}$$

After the execution of the above process P , the value of the *marker variable* satisfies the inequality $1 \leq v \leq 2$.

Transformation rules for RT/SA entities

1. *Modeling input interface.* This consists of an input communication symbol for every origin entity O communicating data or control signals towards P , and, vice-versa, of an output communication for every destination entity D . O and D are RT/SA entities with the only limitation being that neither of them are data stores (DS).

2. *Modeling continuous data flows.* These cannot be directly modeled by means of communication events. It is therefore necessary to write an extra $CSP+T$ process for each continuous data flow.

3. *Modeling state-transition diagrams.* Every control transformation scheme (CTP) is represented by a unique state-transition diagram (STD) from the point of view of control specification. An STD can be formally defined as a tuple (Q, C, A, T, q) in which: Q is a set of states; C is a set of conditions, each one corresponding to an input flow of control in the CTP ; A is a set of actions, each one causing the execution of an activity in the process; T is a set of transitions, where each one is a tuple defined as (q_1, c, a, q_2) in which $q_1, q_2 \in Q$, $c \in C$ or is null, $a \in A$ or is null.

4. *Modeling timed control transformation processes.* A *timed STD* is an initial STD plus the timing constraints imposed on the system. The transition concept can be extended to specify timing constraints in the system by describing *enabling intervals* and marker events. These constraints are described as a set R of tuples (e_1, I, e_2) in which $e_1 \in C$ or $e_1 \in A$, and e_1 is called the *marker event*, I is a real number interval of the form $[\alpha, \beta]$, where $\alpha, \beta \in R^+$, and $\alpha \leq \beta$ or I is an interval relative to the preceding event or to event e_1 . The event $e_2 \in C$ or $e_2 \in A$ is called a *restricted event*. The interpretation of a timing constraint R is as follows: event e_2 can only occur within the interval of time I from the occurrence of e_1 .

5. *Modeling data and control storages.* A DS or a control store (CS) with input flows $\{f_{i1}, \dots, f_{in}\}$ and output flows $\{f_{o1}, \dots, f_{om}\}$ is modeled using the interface $\{f_{i1}, \dots, f_{in}, f_{o1}, \dots, f_{om}\}$ that comprises all communication actions by which the process interacts with its environment.

6. *Modeling transformation specifications.* We suppose that the functionality of primitive data transformation schemes ($DTPs$) is simple enough to allow the analyst to obtain a $CSP+T$ process for each DTP .

The bottom-up design method proposed

We follow a systematic design process that consists of the following steps:

1. Prepare the RT/SA schemes to perform the transformation into $CSP+T$ processes. It may be necessary to rename analysis entities to avoid conflicts.
2. Transform the $CTPs$ and $DTPs$ of the lower level.
3. Select the other schemes in ascending order.
4. Once the $CSP+T$ model has been obtained for all the entities in a scheme, a

CSP+T process is defined to model the complete scheme. If this scheme is already included in a *CTP* or *DTP* of a higher level, repeat step (3), thus progressively integrating the *CSP+T* model of the system in an ascending way. The process finishes when the model of the *System Context Diagram* is obtained.

3 Specification example: The Production Cell

As an application result of our method, a complete *CSP+T* model for the production cell problem can be found at <http://lsi.ugr.es/~sc/vveis04.pdf>. We now present part of the design of the Robot Control Process (*RCP*).

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RCT= start→actions(start)→RTurnCW
RTurnCW= (robot_pos_1▷◁t→action(RTurnCW)→POS_1
          | robot_pos' ? robot_pos→RTurnCW)
POS_1= (I1(a1_finish)→actions(POS_1_CCW)→RTurnCCW→POS_1
        | I2(a1_finish)→disable_a1→action(blank_timeout)→RTurnCCW)

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Its associated enabling intervals are defined as follows: $I_1(a_{1_finish}) = [t, t+T]$, which indicates that the robot arm1 (a_1) picked up a blank from the rotary table; $I_2(a_{1_finish}) = (t+T, \infty)$, in this case there is no blank to pick up within time T .

We have two possible cases to model: the first one represents the presence of a blank on the rotary table that the *arm1* gripper will be able to pick up, the action a_{1_finish} is therefore executed, then *arm1* is positioned and is prepared to extend to pick up the blank; the second one occurs when no new blank prompts on time (i.e., within the deadline T) causing an exception to be raised to inform the system of a *blank_timeout* event. When it reaches the position POS_1 , the control of the robot starts turning arm1 counterclockwise (CCW) until *arm2* picks a forged plate from the press, or *arm 2* (a_2) points to the deposit belt to place a plate on it, or *arm1* goes to the position in which it deposits a blank on the press.

Conclusions

Our methodological scheme uses *CSP+T* process algebra to provide the user with a set of patterns into which they can translate from RT/SA entities into *CSP+T* processes with different semantics.

We are currently working on the development of a formal software tool based on *CTJ* and Java, capable of automated specification, verification and code generation of real-time and embedded system software for several platforms.

References

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