

RPQ: ROBOTIC PROXIMITY QUERIES

Development and Applications

Albert Hernansanz, Xavier Giral

Research Group On Intelligent Robotics and Systems, Technical University of Catalonia, 08028 Barcelona, Spain

Alberto Rodriguez

Robotics Institute, Carnegie Mellon University, Pittsburgh, PA 15213, USA

Josep Amat

Institute of Robotics and Industrial Informatics, Technical University of Catalonia, 08028 Barcelona, Spain

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Abstract: This paper presents a robotic proximity query package (RPQ) as an optimization of the general collision library PQP (Proximity Query Package) for the detection of collisions and distance computation between open kinematic chains such as robotic arms. The performance of the optimizations to non specific collision query packages are explained and evaluated. Finally, a robotic assisted surgical application is presented which has been used as a test bed for the proximity package.

1 INTRODUCTION

One of the most important problems to solve in robotics is the collision avoidance between a robot and its environment. A robot should perceive the risk and have a reactive behavior before an imminent collision occurs. Path planning is a hard computational problem, so having a fast tool to calculate collisions is a key factor to decrease the necessary time to generate safety trajectories. In applications where no path planning exists, for instance in manual guidance or teleoperation, a real time collision detector is needed so as to avoid collisions and to be able to interact with the environment, for example sliding over a surface.

The knowledge of minimum distances between robots or objects that share a workspace enables robots to behave in a predictive way. In the human-robot interaction field, virtual fixtures can be used both to prevent collisions and help the human operator by increasing his performance (Stanisic et al., 1996). In this kind of applications minimum distance and collision detection must be known in real time.

A new library: Robotic Proximity Queries (RPQ) package (Giral and Hernansanz, 2006) has been developed to deal with these requirements, using PQP (UNC, 1999) as the a proximity query engine.

The original package has been used to optimize the queries when working with open kinematic chains, like robots. These optimizations have been done with the aim of improving the time performance of the generic package and simplifying its use in robotic environments. A system composed of two robots has been used as a test bed to show the performance of the RPQ library.

Finally a robotic assisted surgical application that benefits from RPQ performance is presented. The application consists of the execution of an assisted cut of a rigid tissue. The surgeon guides freely the driller held by a slave robotic arm that avoids undesired drillings by means of virtual protections. With this application not only proximity queries are shown, but also the graphical interface and the use of a virtual robot based on RPQ. More information and videos are available at <http://grins.upc.edu>

2 RELATED WORK

During the last years, great efforts have been devoted to the development of efficient collision detection algorithms due to their wide range of applications, such as CAD/CAM, manufacturing, robotics, simulation

and computer animation. A wide study of the performance and applicability of such methods can be found in (B.Geiger, 2000). Proximity query algorithms vary in terms of their range of applicability and the type of queries they can solve, mainly collision detection, minimum distance computation and interpenetrations modelling. Although most algorithms allow as input triangulated meshes of 3D points, they differ in the way those points are pre-processed and represented internally in order to speed up specific queries.

There is a wide set of methods that rely on Lin-Canny or Gilbert-Johnson-Keiethi like algorithms for computing minimum distances between pairs of objects as I-Collide, Swift, Swift++, SOLID, DEEP. . . , but they are only applicable to convex polytopes (S.Ehmann and Lin, 2000; S.Ehmann and Lin, 2001; Kim et al., 2002; Bergen, 2002). This restriction makes them inappropriate for RPQ purposes, due to the need to deal with more general geometric models.

More general collision detection methods usually base their efficiency on pre-computed representations by means of hierarchies of bounding volumes. Their differences rely on the specific type of bounding volumes used, ranging from binary space decompositions, spheres trees to oriented bounding boxes (OBB).

Among this set of algorithms, RAPID and PQP turn to be those that have both, fewer restrictions in the range of allowable geometric models and an easier application programming interface (API). Both of them use oriented bounding boxes for performing collision tests, and have similar time performances. However, the fact that PQP offers a wider range of queries, including minimum distance computation and tolerance tests makes PQP the best option for the proximity queries engine of RPQ, the Robotics Query Package presented in this paper.

3 LIBRARY DESCRIPTION

The goal of the Robotic Proximity Queries (RPQ) library is to offer an easy, modular and fast proximity query package oriented to robotics. As explained above, the aim of the project was not the development of a new collision detector, but specialize an existing one into the robotics field.

As described in section 2, there is a wide set of general purpose proximity query packages. The criteria used to choose PQP as the best candidate for the development of RPQ are:

1. Types of proximity queries available.
2. High time performance on proximity queries.

3. Ability to use geometrical models based on triangulated meshes of points.
4. Lack of restrictions on possible geometrical models.

The PQP library has been developed by UNC Research Group on Modelling, Physically-Based Simulation and Applications and offers three different kind of queries:

- *Collision detection*: detecting whether two models overlap, and optionally, give the complete list of overlapping triangle pairs.
- *Distance computation*: computing the minimum distance between a pair of models.
- *Tolerance verification*: determining whether two models are closer or farther than a given tolerance distance.

RPQ has been implemented in C++ language and its graphical interface has been developed using OpenGL. The RPQ library can be easily integrated into any software application.

The library interface allows non expert programmers to use it in an easy manner. The graphical interface is a separate module, allowing the programmer to decide whether using it or not. Fig. 1 shows the integration of the library and its graphical interface into a generic application.

3.1 Class Description

The RPQ library is based on the Object Oriented paradigm. Focused on this paradigm, and based on robotic environments, three main classes have been developed: Scenario, Object and Robot.

3.1.1 Scenario

Scenario is the workspace where the objects cohabit. Concerning its implementation, Scenario is a class that contains all the objects (Robots and generic objects), a global reference frame, and all the methods necessary to generate the proximity query.

3.1.2 Object

An Object is the minimum entity that exists in a Scenario. There are two types of Objects: simple and complex. A simple Object is represented by a geometrical model composed of a set of triangles referred to a frame tied to the Object. The Object has also a transformation matrix to refer itself to the world reference frame. A complex Object is an Object composed of a set of geometrical models with joints (rotational

or prismatic) between them. Thus, a complex Object is an open kinematic chain composed of sub objects. The transformation matrix M_i refers subobject $_i$ to subobject $_{i-1}$. The transformation matrix M_0 refers the object base (subobject $_0$) to the world. The object stores its own geometrical model. Concerning its implementation, an Object is a class containing the geometrical model, the transformation matrix and a set of methods to position and to orient itself in space. This class also contains methods to calculate the different detail representations of its geometrical model.

3.1.3 Robot

A Robot is a particularization of a complex Object where each of its links is represented by a simple Object. A Robot has a set of functions to make a complex Object as similar as possible to a real robot. For instance, the spatial relationship between links is described using the Denavit-Hartenberg notation. Direct and inverse kinematics can be calculated considering the robots own restrictions (joint limitations, configurations, etc). Concerning implementation, the class Robot is derived from the class Object. Robot adds all the functions that are necessary to control a robot. For instance joint positioning of the robot (direct kinematics), position and orientation of its tool center point (inverse kinematics), change of the robot configuration, joints overshoot . . . These added functions with respect an Object are very helpful when a new robot is created or used in robotic applications like simulators, path planners, etc.

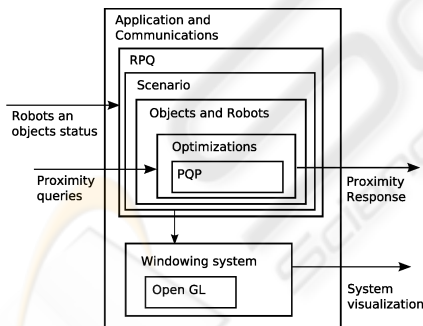


Figure 1: Schema of integration of RPQ into a generic application.

3.2 Optimizations

PQP is a generic package that does not use the knowledge of the object's kinematics. In contrast, RPQ is oriented to robotics, and the knowledge of robot's kinematics is the base of the optimizations that specialize it. RPQ is designed to answer proximity queries between two robots or between a robot and any kind of rigid object.

Three optimizations have been developed and tested to improve the performance offered by PQP:

- Different resolution levels of object's representation
- Collision queries sorted using a Weight Matrix
- Collision Matrix

3.2.1 Different Resolution Levels of Object's Representation

Objects can be represented in very different resolution levels. The idea of this optimization is to use the simplest representation models (minimum number of triangles) to discard collisions. The lower the number of triangles of the geometric model are, the faster the collision queries are executed.

Three resolution levels are used to represent robots and two for the rest of objects. The highest resolution level is the complete geometrical model. The second level is the oriented bounding box (OBB) of each sub object in which a complex object is divided. The lowest resolution level is the bounding box of the whole complex object. This level is only defined for complex objects with more than a sub object, as in robots with several links. There are other possible intermediate resolution levels that can be used, for instance the convex hull. It offers a good ratio between resolution and the quantity of triangles, although it does not reduce it as drastically as the low resolution levels chosen.

This optimization is useful in two different situations. First, in applications where no high precision is required, for instance when the precision of the OBB or the convex hull of each link is enough. The second situation occurs when the different resolution levels are used in a complementary manner.

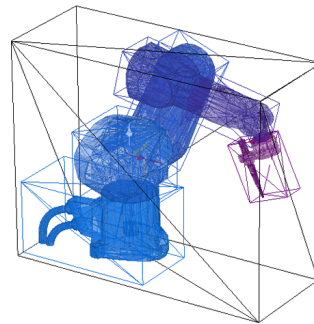


Figure 2: Robot with three resolution level representation: The geometrical model of each link (L3), the OBB of each link (L2) and the whole bounding box(L1).

When a collision query is performed, a low to high resolution level list of collision queries is generated.

Starting with the lowest resolution level, queries are generated until any collision can be completely discarded. For instance, if a possible collision between two 6-DOF robots is studied, the first query is done between the bounding boxes of each robot. If the collision can not be discarded, then the bounding box of each link is used. If at this level collisions still can not be discarded, the geometrical models of each link are checked. As shown in Fig. 2 a Robot with its three resolution levels of representation.

A test has been developed for the evaluation of the performance of the optimizations. It consists on a couple of virtual robotic arms (Staubli RX60B) that are placed one close to the other in a scenario. The geometrical models used for the test are high resolution (composed of 23012 triangles each). The robots are placed at a variable distance between them and the scenario is checked for collisions for an equidistributed set of joint positions in their 6 dof.

This test allows us to study the dependency on the performance of the proposed improvements in terms of the probability of collision. This is because, as shown in Table 1, in the designed test, the closer the robots are, the greater the number of joint configurations that result in collision.

Table 1: Dependence of the amount of colliding configurations on the distance between robots.

Dist. robots(m)	Joint config. checked	Collis.	Not Collis.
0,4	9216	4864	4352
0,5	9216	3530	5686
0,6	9216	2500	6716
0,7	9216	1121	8095
0,8	9216	140	9076

Fig. 3 shows the consequences of using different resolution levels. When the distance between the robots increases, the queries solved with the bounding box of the robot increases, and consequently the time to solve a collision query between the robot decreases. If the distance decreases, the best combination is using levels two and three or only level three.

3.2.2 Collision Queries Sorted using a Weight Matrix

This optimization is based on two assumptions. The first one is that the goal of the query is just to know whether there is a collision or not, but not the number of them. The second assumption is that the kinematics and the morphology of the robots are well known.

Given these assumptions, the objective is to find quickly whether there is collision or not, by means of minimizing the number of partial collision queries.

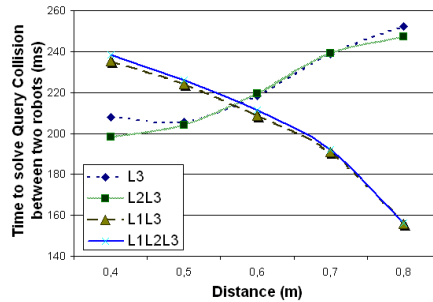


Figure 3: Time to solve a collision query between two Staubli RX60B robots using different resolution levels. L3: Geometrical model of each link. L2: The OBB of each link. L1: Bounding box of the robot.

The knowledge of the kinematics and the morphology of the robots gives us the possibility of assigning an *a priori* collision probability to each link of the robot with respect to the rest of robots and objects present in the same workspace. During execution time, these probabilities are automatically updated depending on the result of the collision queries (Probability increases in case of detecting a collision and decreases otherwise). Therefore, a weight matrix C is generated combining the probability of collision between each pair of objects in the workspace. Each component $c_{ij} \in C$ verifies $c_{ij} = P_i + P_j$ where P_i and P_j are the assigned probability of collision of Object _{i} and Object _{j} respectively. These weights determine the order of the collision queries, that is if $c_{ij} > c_{kt}$ the collision query between Object _{i} and Object _{j} will be generated before Object _{k} and Object _{t} .

A simple way to assign a collision probability to the links of a robot is to assign higher probability to those links that are farther in the kinematic chain, with respect to the base of the robot.

3.2.3 Collision Matrix

The Collision Matrix is a binary matrix that reflects the possibility of collision between two objects. If the collision matrix indicates that a collision between two objects is impossible, its correspondent collision query is not performed. Of course, a matrix query is much less expensive than a collision query in computational terms.

This optimization improves the performance of the system when a high number of collision queries are discarded by the Collision Matrix. Computationally, this condition can be expressed as in equation (1):

$$n \cdot QC > m \cdot QM + k \cdot (QC + QM) \quad (1)$$

with $n = m + k$

where:

n Total number of queries.

m Queries resolved with the Collision Matrix.

k Queries resolved with the Query Collision.

QC Average time to solve a Query Collision.

QM Time to solve a query with the Col. Matrix.

The performance of the Collision Matrix has been studied using the same test designed for testing the use of different levels of representation. The results are shown in Fig. 4. The farther the robots are, the lower is the number of links that can collide, as seen in Table 2. Therefore, the higher the number of queries that are solved with the Collision Matrix. As it is shown in the figure, using the Collision Matrix the number of collision queries decreases, so does the time to solve the query.

Table 2: Dependence of the percentage of collision queries solved by the collision matrix on the distance between robots.

Dist. between robots (m)	Pairs solved with CM
0,4	4,94
0,6	9,88
0,9	24,69
1,2	64,20

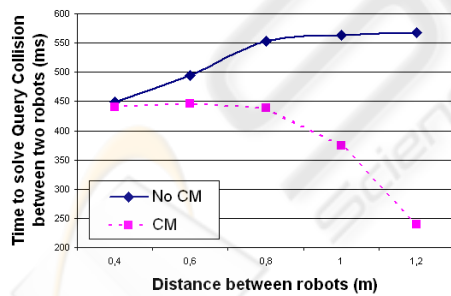


Figure 4: Time necessary to solve a collision query between two Staubli RX60B robots using the Collision Matrix (CM) or not (NoCM).

Each one of the optimizations proposed improves the performance of the original library, PQP. However, the combined use of all of them improves even more the global performance of the application.

The complete algorithm with all three optimizations is shown in Fig. 5. First of all, a query collision between the whole bounding box of both robots

is performed. If at this level the collision cannot be solved then it is necessary to study collisions among the whole set of links of both robots. The order in which these queries must be performed is given by the Weight Matrix. The query finishes as soon as a collision appears between a pair of links either in the second or third level, or when all pairs have not reported any collision. For each pair of links, the second and third representation levels are studied consecutively, so if a collision is detected in the second level, the third level has to be studied as well.

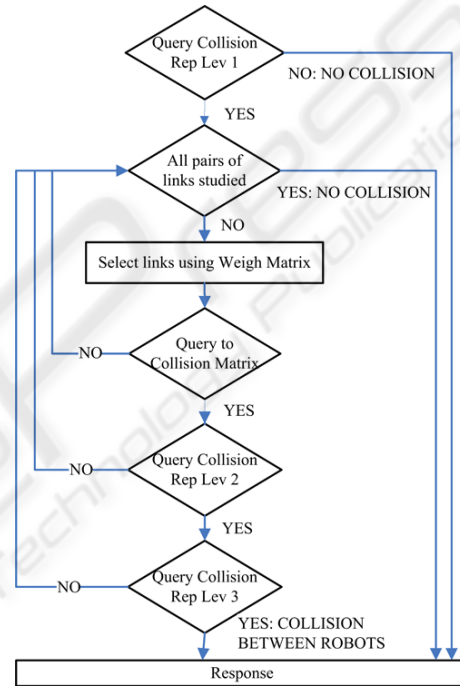


Figure 5: Algorithm for collision detection between two robots using all the optimizations.

4 APPLICATION

One of the advantages of making RPQ generic (although it is optimized for robots) is that this library can be applied in a wide set of applications. In this paper a robotic assisted surgical application is presented. This application has the aim of helping the surgeon to make a cut on a rigid tissue, for example in the cranium, avoiding undesired collisions between the patient and the driller. The surgeon guides freely the driller that is held by the robot acting in a passive mode as seen in Fig. 6, allowing all movements except those which produce undesired collisions.

The system is composed by a Staubli RX60B robotic arm and a driller. Between the robot and the

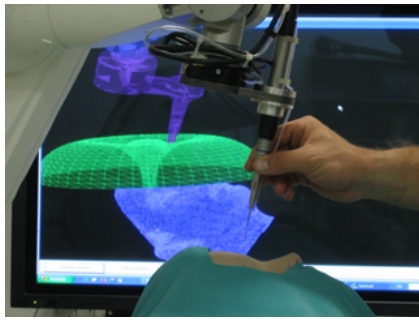


Figure 6: Robotic assisted surgical application.

driller there's a ATI Multi-Axis Force/Torque Sensor. The system transforms forces and torques generated in the driller by the surgeon in new destination points were the robot must go.

The geometric model of the patient's cranium is obtained transforming Computer Tomography data into a geometrical model composed of triangles. The surgeon can define the cutting area in the pre-operative phase and, as will be explained latter, virtual fixtures are automatically generated to protect the patient in the operative phase. The possibility of introducing virtual objects in the scene and the interaction between them is one of the key factors of RPQ.

The surgeon has a friendly and easy-use graphical interface that allows the navigation over the virtual system. This graphical interface helps the surgeon not only in the pre-operative phase but also during the surgical operation, providing an augmented reality visual feedback (collisions, minimal distance between the cranium and the tool, different points of view of the scene, virtual fixtures).

4.1 Surface Navigation

The library developed is useful not only to avoid collisions but also to navigate over an object's surface. For instance, the robot tool slides over the surface of the virtual shield described in section 4.2. This surface navigation allows the surgeon to feel smooth movements of the robot when the tool is in contact with the virtual fixtures. The navigation algorithm helps the surgeon not only avoiding the forbidden regions defined in the pre-operative phase but also guiding him to the desired cutting path.

The navigation algorithm modifies the position of the robot tool, but not its orientation. The algorithm is based on three steps: Knowing the new desired destination of the robot tool, the first step consists of detecting all collisions between the tool and the object's surface. When all collisions are detected, the second step consists of projecting the desired point to the plane of the collision triangle, Fig. 7.a. Fi-

nally the projected point that is closer to the desired one is selected. A problem can occur when the projected point falls outside the triangle region. In this situation it is not possible to ensure that this new projected point is always be outside the object Fig. 7.c. In this case the new point is projected to the perimeter of the triangle. To accomplish this, the outside region of the triangle is divided into six new regions ($R1, R12, R2, R23, R3, R31$), which are defined by the normals of the edges of the triangle applied to the vertices of the triangle. The point is then projected to the closest point of the triangle border of its region Fig. 7.b. Now, the new destination point is collision free Fig. 7.d.

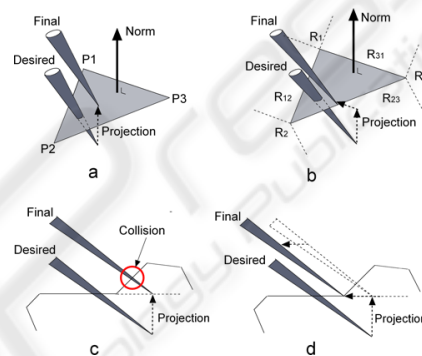


Figure 7: Different contact situations between the tool and a triangle or set of triangles.

4.2 Virtual Protections

Virtual Protections are constraints that rule the behaviour of the robot that are specifically designed to prevent motion into a forbidden region of the workspace. In this work, the surgeon guides freely a driller held by the slave robot. The main idea is to develop a system helpful for the surgeon that prevents undesired drillings.

4.2.1 Strategy Description

The main goal of the system is to give the robot a reactive behaviour by means of the definition of virtual objects in the PQP Scenario with two objectives:

- Protect the patient from the robot and the driller.
- Help the surgeon to locate the desired cutting area.

PQPs ability to check collisions in real time allows us not only to achieve these objectives but to operate in an efficient manner.

Throughout a simple interface, in the pre-operative phase, the surgeon specifies the exact location and shape of the cut that must be done. With that

information, the system generates a shield that covers the patient while it adapts perfectly to the target area defined by the surgeon, as shown in Fig. 8.

The proposed behaviour is achieved by the navigation algorithm exposed in chapter 4.1. The system gives the surgeon the confidence of knowing that the robot will never let him approach the patient in a non-desired area. However, while the surgeon does not attempt to cross the shield, the reobot can be moved freely.

4.2.2 Shield Generation

The problem here is to generate a surface that connects the inner polygonal curve defined by the surgeon with an outer curve. The connection between them is done in a smooth way, as Fig. 8 illustrates.

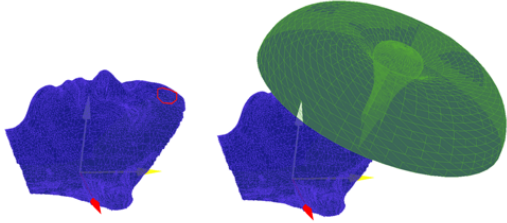


Figure 8: Lateral view of a face and the virtual shield.

The surface, $s(u, v)$, is parametrized as the upper part of a regular torus, but adapting its equators to the inner and outer curves, as in (4).

$$\text{Inn. curve } i(t) = (i_x(t), i_y(t)) \quad t \in 0..2\pi(2)$$

$$\text{Out. curve } o(t) = (o_x(t), o_y(t)) \quad t \in 0..2\pi(3)$$

$$s(u, v) = \left(\begin{aligned} &\sin^2\left(\frac{v}{2}\right)i_x(u) + \cos^2\left(\frac{v}{2}\right)o_x(u), \\ &\sin^2\left(\frac{v}{2}\right)i_y(u) + \cos^2\left(\frac{v}{2}\right)o_y(u), \\ &H \sin(v) \end{aligned} \right) \quad u \in 0..2\pi \quad v \in 0..\pi \quad (4)$$

There are peculiarities of the shield to consider:

- The shield should be smooth, in order to make navigation over it as comfortable as possible. Once the surface is generated it is transformed into a triangle model. By augmenting or decreasing the number of triangles, one can vary the smoothness of the surface.
- Reaching the inner curve from the surface it has to be easy and intuitive. This implies certain restrictions on the shield design. This property depends on the way inner points are connected to outer points. First of all inner and outer curves

have to be parametrized, (2) and (3). There are some restrictions regarding them in order to make the surface easy and intuitive.

- $i(t)$ and $o(t)$, must be parametrized radially, from an inner point, with constant radial velocity, in order to avoid self intersections of the surface, as in Fig. 9 a) and b).
- The polygon defined by $i(t)$, must be star-shaped from the parametrization origin, in order to avoid self intersections of the surface, as in Fig. 9 c) and d).
- If $i(t)$ defines a non star-shaped polygon a previous step must be done. An adaptation disc between the polygon and its convex hull is needed before constructing the shield, so that the latter can be parametrized radially from a suitable inner point, as in Fig. 10.

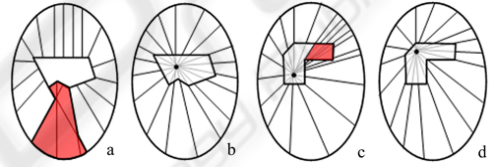


Figure 9: a) Non valid parametrization of curves (self intersection of the surface). b) Valid parametrization of curves. c) Non valid point for radial parametrization of curves. Polygon is not star-shaped from that point. d) Valid point for radial parametrization of curves.

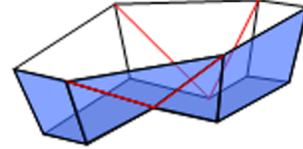


Figure 10: Adaptation disc between an non star-shaped polygon and its correspondent 2D Convex Hull.

- H , the height of the shield, must be chosen in order to protect the patient.

Once the required smoothness for the surface is defined, the parametrization for $i(t)$ and $o(t)$, solved the problem with non star-shaped polygons and chosen a desired height, the surface is generated by eq. (4).

Finally, the intersections of the discrete set of geodesics $u = \frac{2\pi}{N}n$ and $v = \frac{\pi}{N}n$ for $n \in 1 \dots N$ is triangulated in order to obtain the geometrical model. The parameter N allows us to choose the number of points and triangles of the surface, and ultimately its smoothness.

4.2.3 Cutting Aid

Besides the shield generated, another virtual object is proposed in order to aid the surgeon to carry out the cut with great accuracy. It consists of an inner cover that prevents the drillers from escaping the perimeter of the shape defined.

Since (2) has the shape of the cut to be done, we define $\hat{i}(t)$ as an under scaled version of $i(t)$. $\hat{i}(t)$ has the same shape as $i(t)$ but its sides are placed at a distance Δx from $i(t)$ sides, being Δx the desired width for the cut.

Therefore, a new shield is generated, $\hat{s}(u, v)$, having a semisphere shape, with $\hat{i}(t)$ as its equator, parametrized by (5).

$$\begin{aligned} \hat{s}(u, v) = & \\ = & \left((\hat{H} \cos^2(v) \cos(u) + \sin^2(v) \hat{i}_x(u)) \sin(v), \right. \\ & \left. (\hat{H} \cos^2(v) \sin(u) + \sin^2(v) \hat{i}_y(u)) \sin(v), \right. \\ & \left. \hat{H} \cos(v) \right) \quad u \in 0..2\pi \quad v \in 0..\frac{\pi}{2} \quad (5) \end{aligned}$$

5 CONCLUSION

This paper presents the development of RPQ, a proximity queries library optimized for applications where robots share a common workspace and interact with objects. Due to the amount of collision detection packages, RPQ is built above a generic collision package, PQP. It is the generic collision package that better fits RPQ purposes.

The goal of developing RPQ was to fill an existing gap in computer tools for robotic applications, where robots interact with objects in their environment. Three optimizations have been performed to a generic collision library: working with different resolution levels of representation, the use of a weighted matrix for choosing the best order for collision checking and the definition of a binary matrix that determines the possibility of collision between objects. RPQ has been validated in different applications such as multirobot collision avoidance, virtual robot controller and surface navigation.

As expected, optimizations improve the time performance of the system, although this improvement is highly application dependent.

The introduction of different levels of resolution in the geometric models of the objects and robots generally decreases the computational time for collision checking. The use of bounding boxes decreases drastically the number of high resolution queries needed.

This is a really important point taking into account that they are much more time consuming. There are cases where low resolution queries do not solve the whole collision query. This increases the computation time. However, choosing a suitable order for checking collisions helps to find them in a quicker manner. The precomputation of impossibilities of collision between different objects (Collision Matrix) increases the performance of the system in case of having objects with restricted mobility in the workspace.

The combined use of optimizations generate good results in workspaces shared by at least two robots and objects.

RPQ has a wide range of applicability. RQP library is not only useful for proximity queries but has also proved to be a good tool for surface navigation and virtual representations, due to its ability to introduce virtual objects in the shared workspace. The virtual fixtures developed in the paper are examples of how RPQ can be used to modify robot's behaviour.

As proved in the application presented, RPQ is not only useful for developers of robotic applications, but also for users of robotic applications, i.e. surgeons that require new robotic tools for improving surgical procedures.

REFERENCES

- Bergen, G. V. D. (2002). Solid collision detection library users guide.
- B.Geiger (2000). Real-time collision detection and response for complex environments. In *International Conference on Computer Graphics*. IEEE Computer Society.
- Giralt, X. and Hernansanz, A. (2006). Optimization of proximity queries in robotic environments. In *AVR - 2es Jornades UPC de Recerca en Automtica, Visio i Robotica (in catalan)*.
- Kim, Y., Lin, M., and Manocha, D. (2002). Deep: Dual-space expansion for estimating penetration depth between convex polytopes. In *International Conference on Robotics and Automation*. IEEE.
- S.Ehmann and Lin, M. (2000). Accelerated proximity queries between convex polyhedra by multilevel voronoi marching. Technical report, Department of Computer Science, University of North Carolina.
- S.Ehmann and Lin, M. (2001). Accurate and fast proximity queries between polyhedra using convex surface decomposition. In *Eurographics*, volume 3.
- Stanisic, Z., Jackson, E., and Payandeh, S. (1996). Virtual fixtures as an aid for teleoperation. In *9th Canadian Aeronautics and Space Institute Conference*.
- UNC (1999). Pqp - a proximity query package by research group on modeling, physically-based simulation and applications.