

MODELLING HUMAN REASONING IN INTELLIGENT DECISION SUPPORT SYSTEMS

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Abstract: Methods of analogy-based solution searches in intelligent decision support systems are considered. The special attention is drawn to methods based on a structural analogy that use the analogy of properties and relations and take the context into account. Besides the problem of concept generalization is viewed. Several algorithms based on the rough set theory are compared and the possibility to use them for generalization of data stored in real-world databases is tested.

1 INTRODUCTION

Investigation of mechanisms that are involved in the analogous reasoning process is an important problem both for psychologists and specialists in artificial intelligence (AI). The analogy can be used in various applications of AI and for solving various problems, e.g., for generation of hypotheses about an unknown problem domain or for generalizing experience in the form of an abstract scheme. The great interest in this problem is caused by the necessity of modelling human reasoning (common sense reasoning) in AI systems and, in particular, in intelligent decision support systems (IDSS).

In the encyclopaedia the word *analogy* (analogia, Greek: correspondence, similarity, likeness, closeness) is defined as the similarity of objects (phenomena, processes) with respect to some properties. *Reasoning by analogy* is the transfer of knowledge obtained from an object to a less studied one which is similar to the latter with respect to some essential properties or attributes. Reasoning of this kind is a source of scientific hypotheses.

Thus, *analogy-based reasoning* can be defined as a method that allows to understand a situation when compared with another one. In other words, an analogy is an inference method that allows to detect likeness between several given objects due to transfer of facts and knowledge valid for both objects, to other objects and to determine means of problem solution or to forecast unknown properties. It is this type of inference that is used by a human in the first stages of solving a new problem. At the present time, there are a great number of various

models, schemes, and methods that describe mechanisms of reasoning by analogy. Another important problem is a problem of concept generalization especially in case it is necessary to treat incomplete and inconsistent information. However the real data bases (DB) contain, as a rule, "raw" data and without analysis and generalization these flows of "raw" data are of no use.

The common point of these data is that they contain a large number of hidden regularities. At present, to reveal these regularities and construct inductive models, generalization methods and computer systems that implement these methods are being developed. Using generalization methods in decision-making systems, the features that characterize the group to which one or another object belongs are selected. This is achieved by analyzing already classified objects and forming a certain set of rules (generalized model). Then, this generalized model can be used for recognizing objects not known to the system in advance. The problem of classifying objects under excessive, incomplete, or inconsistent information is very important. We consider the opportunities of using the rough set theory for solving problems of inductive concept generation, as well as to propose methods for improving known algorithms. A new algorithm for discretization of continuous attributes which considerably improves the efficiency of generalization procedures is proposed. The generalized structure of a real-time IDSS is given in Fig. 1. The search for an analogous solution may be applied in units of analysis of the problem situation, learning, adaptation and modification, modelling, and forecasting (Vagin, Ereemeev, 2001).

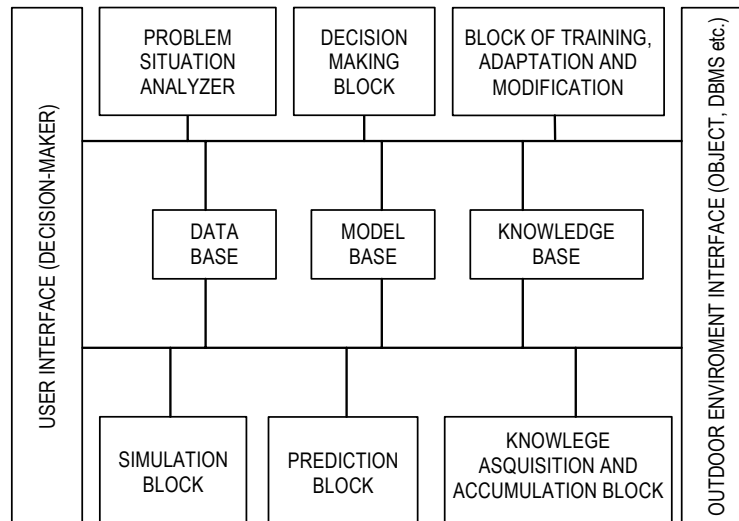


Figure 1: The generalized structure of a real-time IDSS.

2 REASONING BY ANALOGY

Questions about the nature of analogies, a formal definition, justification of reasoning by analogy, etc., arose in the time of epicureans and stoics. The attempts to answer these questions, starting from the first attempts of Leibniz to formalize this notion up to our time, have not received a final answer (Pospelov, 1989; Varshavskii, Ereemeev, 2005).

At the present time, there are a great number of various models, schemes, and methods that describe mechanisms of reasoning by analogy (Varshavskii, Ereemeev, 2005; Long, Garigliano, 1994; Ereemeev, Varshavsky, 2005; Haraguchi, Arikawa, 1986).

In (Haraguchi, Arikawa, 1986), the authors have proposed two types of analogies: an analogy for solving problems and an analogy for forecasting.

The analogy for solving problems assumes applying reasoning by analogy for increasing the efficiency of the problem solution which, generally speaking, can be solved without analogy as well, as, e.g., in programming and proving theorems.

Analogy for prediction (forecasting) uses reasoning by analogy for obtaining new facts. Due to the transformation of knowledge based on the likeness of objects, one can make the conclusion that new facts probably hold. For example, if an analogy is applied to a system of axioms, the result may be certain theorems valid with respect to the system. Here, using the similarity between axiom systems, one can transform a theorem in a system to a logical formula in another system and make a conclusion that the latter is a theorem.

Depending on the nature of information transferred from an object of analogy to the other

one, the analogy of properties and the analogy of relations can be distinguished.

The analogy of properties considers two single objects or a pair of sets (classes) of homogeneous objects, and the transferred attributes are properties of these objects, for example, analogy between illness symptoms of two persons or analogy in the structure of the surfaces of Earth and Mars, etc.

The analogy of relations considers pairs of objects where the objects can be absolutely different and the transferred attributes are properties of these relations. For example, using the analogy of relations, bionics studies processes in nature in order to use the obtained knowledge in a modern technology.

According to plausibility degrees one can distinguish three types of analogies: strict scientific analogies, nonstrict scientific analogies, and nonscientific analogies.

A strict scientific analogy is applied to scientific studies and mathematical proofs. For example, the formulation of the attributes of the similarity of triangles is based on a strict analogy which results in a deductive inference, i.e., which deduces a valid conclusion.

Unlike the strict analogy, a nonstrict scientific analogy results only in plausible (probable) reasoning. If the probability of a false statement is taken equal to 0 and that of the true statement is taken equal to 1, then the probability of inference by a nonstrict analogy lies in the interval from 0 to 1. To increase this probability, one needs to satisfy a number of requirements to the method of reasoning by analogy, otherwise, a nonstrict analogy may become nonscientific.

A nonscientific analogy is often used deliberately to perplex the opponent. Sometimes, a

nonscientific analogy is used unintentionally, by someone not knowing the rules of analogies or having no factual knowledge concerning the objects and their properties that underlie the inference.

We consider the methods of solution search on the basis of structural analogy which allows to take into account a context and based on the theory of structural mapping. We use semantic networks (SNs) as a model of knowledge representation.

3 REASONING BY STRUCTURAL ANALOGY TAKING INTO ACCOUNT A CONTEXT

In (Long, Garigliano, 1994), the authors have proposed to consider an analogy as a quadruple $A = \langle O, C, R, P \rangle$ where O and R are the source object and the receiver one and C is the intersection object, i.e., the object that structurally intersects them and has larger cardinality of a set of properties as compared with these objects. In other words, the analogy between the source object and the receiver object is considered in the context of the intersection, and P is a property for definition of the

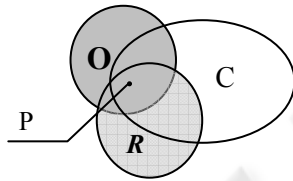


Figure 2: The structure of the analogy.

original context. The structure of this analogy is represented in Fig. 2.

Using the described structure of the analogy, the authors of (Long, Garigliano, 1994) have proposed the algorithm for the problem solution that is based on analogy of the properties. A SN with information about the problem domain, a receiver R , and a property for defining the original context P provide input data for this algorithm.

The algorithm for the problem solution on the basis of analogy taking into account the context consists of the following steps.

Step 1. Determine all objects of the SN, except for receiver R , that have property P . If there are no objects of this kind, then the search for a solution fails, otherwise, go to step 2.

Step 2. For the objects found in step 1, determine all possible intersections of C with R taking into account P . If there are no intersections of C , then the search for a solution fails, otherwise, go to step 3.

Step 3. From the objects extracted in step 1, determine all possible sources O for analogies with the receiver R and the intersection C taking into account P . In the case of success (possible analogies for R are defined), go to step 4, otherwise, the search for a solution fails.

Step 4. From the analogies extracted in step 3, choose the most appropriate (taking into account the requirements of the decision making person (DMP)). In the case of success, go to step 5; otherwise, the search for a solution fails.

Step 5. The analogies obtained in step 4 are given to the DMP which means successful termination of the algorithm.

Having obtained analogies, the DMP may then make the final choice of the best ones. On the basis of these facts, the facts (properties) that hold for the source O are transferred to the receiver R .

Consider the modified algorithm for a problem solution that uses the structural analogy based on the modified structure of analogy and the algorithm for the search of minimal intersections (Varshavskii, Ereemeev, 2005). The modification consists in the fact that P is considered not as a unique property, but as a set of properties that determine the original context of the analogy. As compared with the base variant, one of the main advantages of this modified algorithm is the possibility of implementing the search for a solution on the basis of analogy without refining the original context, since in the result of the search for the minimal intersection, one can easily distinguish all possible contexts for the analogy. Another important advantage of the modified algorithm is the possibility of a more detailed refinement of the original context for the determination of analogies. Moreover, in the modified algorithm there is a possibility to construct analogy taking into account the context between well-known objects, the source and the receiver.

4 GENERALIZATION PROBLEM

For the description of an object we will use features a_1, a_2, \dots, a_k , which are further called attributes. Each object x is characterized by a set of given values of these attributes: $x = \{v_1, v_2, \dots, v_k\}$ where v_i is a value of the i -th attribute. Such description of an object is called *feature description*. For example, the attributes may be a colour, a weight, a form, etc.

Let we have a learning set U of objects. It contains both the positive examples (which are concerning to interesting concept) and the negative examples. The concept generalization problem is the construction of the concept allowing the correct classifying with the help of some recognizing rule (*decision rule*) of all positive and negative objects of

a learning set U . Here the construction of the concept is made on the basis of analysis of a learning set.

Let's introduce the following notions related with the set U . Let $U = \{x_1, x_2, \dots, x_n\}$ is a non-empty finite *set of objects*. $A = \{a_1, a_2, \dots, a_k\}$ is a non-empty finite *set of attributes*. For each attribute the set V_a is defined which refers to the *value set* of an attribute a . We will denote the given value of an attribute a for an object $x \in U$ by $a(x)$. At the decision of the generalization problem, it is often necessary to receive the description of the concept which is specified by a value of one of the attributes. We will denote such attribute d and call it *decision* or a *decision attribute*. The attributes which are included in A are called *conditional attributes*. The decision attribute can have some values though quite often it is binary. The number of possible values of a decision attribute d is called the rank of the decision and is designated at $r(d)$. We will denote the value set of the decision by $V_d = \{v_1^d, v_2^d, \dots, v_{r(d)}^d\}$. The decision attribute d is defined by the partition of U into classes $C_i = \{x \in U: d(x) = v_i^d\}$, $1 \leq i \leq r(d)$.

Generally, the concept generated on the basis of the learning set U is an approximation to a concept of the set X where the closeness degree of these concepts depends on the representativeness of a learning set, i.e. how complete the features of set X are expressed in it.

5 CONCEPT GENERALIZATION METHODS BASED ON THE THEORY OF ROUGH SETS

The rough set theory has been proposed in the beginning of 80th years of the last century by the Polish mathematician Z. Pawlak. We will consider how the rough set theory can be used to solve concept generalization problem – see also (Pawlak, 2002; Bazan, 1998; Vagin, Golovina, ec.,2004; Nguyen, Nguyen, 1996). In Pawlak's works the concept of an information system has been introduced. An *information system* is understood as the pair $S = (U, A)$ where $U = \{x_1, x_2, \dots, x_n\}$ is a non-empty finite set of objects named the *learning set* or *universe*, and $A = \{a_1, a_2, \dots, a_k\}$ is a non-empty finite *set of attributes*. A *decision table* is an information system of the form $S = (U, A \cup \{d\})$, where $d \notin A$ is a distinguished attribute called *decision* or a *decision attribute*. A is a set of *conditional attributes*.

Now let us consider the methods of concept generalization using the theory of rough sets.

Generally, work of the algorithm based on the rough set theory consists of the following steps: search of equivalence classes of the indiscernibility relation, search of upper and lower approximations, search of a reduction of the decision system and constructing a set of decision rules. Moreover, discretization is applied to processing attributes with a continuous domain. In the case of the incomplete or inconsistent input information, the algorithm builds two systems of decision rules, one of them gives the certain classification, the second gives the possible one. Further, we will consider the most labour-consuming steps: search of reduction and discretization making.

5.1 The Problem of Search of Reduction

Let's consider the process of search of reduction that is very important part of any method used the rough set approach. Quite often an information system has more than one reduction. Each of these reductions can be used in the procedure of decision-making instead of a full set of attributes of an original system without a change of dependence of the decision on conditions that is characteristic for an original system. Therefore, the problem of a choice of the best reduction is reasonable. The answer depends on an optimality criterion related to attributes. If it is possible to associate with attributes the cost function which expresses complexity of receiving attribute values, then the choice will be based on the criterion of the minimal total cost. The problem of searching for a reduction with minimal length is NP-hard (Skowron, Rauszer, 1992).

Thus, the problem of a choice of relevant attributes is one of the important problems of machine learning. There are several approaches based on the rough set theory. One of the first ideas was to consider as the relevant attributes those attributes which are contained in intersection of all reductions of an information system.

Other approach is related to dynamic reductions (Bazan, 1998), i.e. conditional attribute sets appearing "sufficiently often" as reductions of subsamples of an original decision system. The attributes belonging to the "most" of dynamic reductions are considered as relevant. The value thresholds for "sufficiently often" and "most" should be chosen for given data.

The third approach is based on introduction of the notion of significance of attributes that allows by real values from the closed interval $[0, 1]$ to express how important an attribute in a decision table.

5.2 The Modification of the Discretization Algorithm

The stage of discretization is necessary for the most of modern algorithms for generalization. The discretization is called a transformation of a continuous domain of attributes in a discrete one. For example, the body temperature of the human being which is usually measured by real numbers can be divided into some intervals, corresponding to a low, normal, high and very high temperature. The choice of suitable intervals and partition of continuous domains of attributes is a problem whose complexity grows in exponential dependence on the number of attributes to which discretization should be applied. The general approach of the most discretization algorithms is based on that any irreducible set of cuts of a decision table S is a reduction of other decision table constructed on the basis of S .

Our algorithm is directed towards decreasing time and memory consumption. It is based on the Jonson’s strategy and extension of idea of iterative calculation of the number of pair of objects, discerned by a cut. This idea has been offered in (Nguyen, Nguyen, 1996), however, originally, it is applicable only when some restrictions on the decision table are imposed. This idea is based on assumption that there is a close relation between two consecutive cuts. So, for example, it is possible to notice, that in each row of the table all the cells with value 1 are placed successively within one attribute. Therefore some pairs of objects are discerned by both consecutive cuts, and changes in the number of discernible pairs of objects can be only due to objects which attribute values lay between two these cuts. In (Nguyen, Nguyen, 1996), the situation, when no more than one object lies in this interval, is

considered. We generalize this idea on a case of the arbitrary number of such objects. Thus, our algorithm extends idea of iterative calculating number of pairs of objects discerned by a cut to an arbitrary decision table. In the majority of the algorithms which are based on the rough set theory and carrying out splitting of continuous attribute domains into finite number of intervals, the stage of discretization is considered as preparatory before search of significant attributes. And consequently at a stage of discretization, there is a splitting the domains of all continuous attributes including insignificant. In this work, the combined implementation of discretization with search of a reduction is offered to make discretization only for those quantitative attributes which appear to be significant during search of reduction.

Thus, the developed algorithm for search of significant attributes is based on two ideas: 1) combination of discretization of quantitative attributes with search of significant attributes, 2) search for an approximation of reduction, but not for reduction itself. Let’s name it as **Generalized Iterative algorithm based on the Rough Set approach, GIRS**.

5.3 Results of the Experiments

The implemented experiments have shown that the developed algorithm allows to reduce time for search of significant attributes essentially, due to combination with the discretization stage and use of the proposed algorithm.

The results of the experiments executed on 11 data sets from a well known collection UCI Machine Learning Repository (Merz, Murphy, 1998) of the University of California are given in Table 1.

For all data sets taken into the comparison, the

Table 1: Comparison of classification accuracy of the developed algorithm with other generalization algorithms.

Data set	Classification accuracy				
	ID3	C4.5	MD	Holte-II	GIRS
Monk-1	81.25	75.70	100	100	100
Monk-2	65.00	69.91	99.70	81.9	83.10
Monk-3	90.28	97.20	93.51	97.2	95.40
Heart	77.78	77.04	77.04	77.2	78.72
Hepatitis	n/a	80.80	n/a	82.7	84.51
Diabetes	66.23	70.84	71.09	n/a	81.00
Australian	78.26	85.36	83.69	82.5	88.71
Glass	62.79	65.89	66.41	37.5	70.10
Iris	94.67	96.67	95.33	94.0	96.24
Mushroom	100	100	100	100	100
Soybean	100	95.56	100	100	100
Average	81.63	83.18	88.67	85.3	88.89

developed algorithm has shown classification accuracy that not concedes to other generalization algorithms, and in some cases surpasses them. Average accuracy of classification is approximately 88.9%. It is necessary to note that the classification accuracy received by our algorithm is much above that the classification accuracy achieved by methods of an induction of deciding trees (ID3, ID4, ID5R, C4.5) at the solving the majority of the problems. It is explained by the impossibility of representation of the description of some target concepts as a tree. Moreover, it is possible to note that combining of search of significant attributes and the discretization procedure is very useful. Most clearly, it is visible from the results received at the decision of the Australian credit task. It is possible to explain by the presence in these data the attributes both with continuous and with discrete domains. The modification of the search procedure of significant attributes is directed namely to processing of such combination.

6 CONCLUSIONS

The method of reasoning by analogy on the basis of structural analogy was considered from the aspect of its application in modern IDSS, in particular, for a solution of problems of real-time diagnostics and forecasting. The example of the algorithm for solution search on the basis of analogy of properties that takes into account the context was proposed. This algorithm uses a modified structure of analogy that is capable of taking into account not one property (as in the base algorithm), but a set of properties. These properties determine the original context of analogy and transfer from the source to the receiver only those facts that are relevant in the context of the constructed analogy.

The presented method was applied at implementation of a prototype of IDSS on the basis of non-classical logics for monitoring and control of complex objects like power units.

We have also considered the concept generalization problem and the approach to its decision based on the rough set theory. The heuristic discretization algorithm directed towards the decreasing of time and memory consumption has been proposed. It is based on Jonson's strategy and extension of idea of iterative calculation number of pairs of objects discerned by a cut. Also the search algorithm of the significant attributes combined with the stage of discretization is developed. It allows to avoid splitting into intervals of continuous domains of insignificant attributes.

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