

COMPARISON OF ANALYTIC APPROACHES FOR DETERMINING VARIABLES

A Case Study in Predicting the Likelihood of Sepsis

Femida Gwadry-Sridhar, Benoit Lewden, Selam Mequanint
Lawson Health Research Institute, I-THINK Research Lab, London, ON, Canada

Michael Bauer
Department of Computer Science, University of Western Ontario, London, ON, Canada

Keywords: Sepsis, Decision support, Decision trees.

Abstract: Sepsis is a significant cause of mortality and morbidity and is often associated with increased hospital resource utilization, prolonged intensive care unit (ICU) and hospital stay. The economic burden associated with sepsis is severe. With advances in medicine, there are now aggressive goal oriented treatments that can be used to help these patients. If we were able to predict which patients may be at risk for sepsis we could start treatment early and potentially reduce the risk of mortality and morbidity. Analytic methods currently used in clinical research to determine the risk of a patient developing sepsis may be further enhanced by using multi-modal analytic methods that together could be used to provide greater precision. Researchers commonly use univariate and multivariate regressions to develop predictive models. We hypothesized that such models could be enhanced by using multi-modal analytic methods that together could be used to provide greater precision. In this paper, we analyze data about patients with and without sepsis using a decision tree approach. A comparison with a regression approach shows strong similarity among variables identified, though not an exact match. We compare the variables identified by the different approaches and draw conclusions about the respective predictive capabilities.

1 INTRODUCTION

Sepsis is defined as infection plus systematic manifestations of infection (Dellinger et al., 2008). Severe sepsis is considered present when sepsis co-exists with sepsis-induced organ dysfunction or tissue hypo-perfusion (Dellinger et al., 2008). Sepsis can result in mortality and morbidity, especially when associated with shock and/or organ dysfunction (Angus et al., 2001). Sepsis can be associated with increased hospital resource utilization, prolonged intensive care unit (ICU) and hospital stay, decreased long-term health related quality of life and an economic burden estimated at US \$17 billion each year in the United States alone (Brun-Buisson et al., 1995; Salvo et al, 1995; Pittet et al., 1995; Angus et al., 2001). In Canada, there are limited data on the burden of severe sepsis; however, costs in Quebec may be as high as \$73M per year

(Letarte, Longo, Pelletier, Nabonne & Fisher, 2002), which contribute to estimates of total Canadian cost of approximately \$325 M per year.

Patients with severe sepsis generally receive their care in the ICU. A multicentre study of sepsis in teaching hospitals found that severe sepsis or septic shock is present or develops in 15% of ICU patients (Alberti et al., 2002). However, diagnosing sepsis is difficult because there is no “typical” presentation despite published definitions for sepsis (American College of Chest Physicians/Society of Critical Care Medicine Consensus Conference 1992; Levy et al., 2003).

In the Canadian Sepsis Treatment And Response (STAR) registry (mix of teaching and community hospitals across Canada), the total rate for severe sepsis was 19.0%. Of these, 63% occurred after hospitalization.

With advances in medicine there are now aggressive goal oriented treatments that can be used

to help these patients (Rivers et al., 2001; Minneci, Deans, Banks, Eichacker, & Natanson, 2004; Bernard et al., 2001). If researchers were able to predict which patients may be at risk for sepsis we could start treatment early and potentially reduce the risk of mortality and morbidity. Therefore, methods that can be developed to help with the early diagnosis of patients who either present with sepsis or develop sepsis in hospital are needed.

A variety of analysis techniques can be used to identify relationships among a set of measured variables or quantities. We hypothesized that analytic methods currently used in clinical research to determine the risk of a patient developing sepsis may be further enhanced by using multi-modal analytic methods that together could be used to provide greater precision. Researchers commonly use univariate and multivariate regressions to gather information about variables that are associated with the dependent variable, which in this case is whether the patient contracted sepsis or not. However, sometimes these models are constrained as we either use univariate analysis to guide our decision on which variable to include or rely on the literature to guide the variable selection. Earlier work had looked at the use of regression techniques to develop a linear predictive model or mortality and length of stay, but not sepsis (Martin et al., 2008).

In this paper, we consider the use of decision tree analysis and cluster analysis. Decision trees are interesting since they provide a prescriptive approach for arriving at a decision with an associated probability. In contrast, cluster analysis takes a holistic approach to partition the data into similar but disjointed sets. We were interested in using these approaches to identify the key variables or variable sets that can be used to predict the likelihood of sepsis or not having sepsis in patients.

2 DATA IN STUDY

We obtained data that was collected from 12 Canadian intensive care units that were geographically distributed and included a mix of medical and surgical patients (Martin et al., 2008). Data were collected on all patients admitted to the ICU who had an ICU stay greater than 24 hours or who had severe sepsis at the time of ICU admission. Patients who were not anticipated to obtain to receive active treatment were excluded.

Hospitals collected a minimum data set on all eligible patients admitted to the ICU. This included demographic information and data about their

admission, source of admission, diagnosis, illness severity, outcome and length of ICU and hospital stay. Illness severity scores were calculated using data obtained during the first 24 hours in the ICU (Knaus, Draper, Wagner, & Zimmerman, 1985; Knaus et al., 1991). All patients were subsequently assessed on a daily basis for the presence of infection and severe sepsis.

The management of severe sepsis requires prompt treatment within the first six hours of resuscitation (Dellinger et al., 2008b). Experts in critical care agree that the literature supports early goal-directed resuscitation which has been shown to improve survival in patients presenting to emergency rooms with septic shock (Dellinger et al., 2008a).

2.1 Ethical Review, Funding and Data Ownership

The study was approved by the University of Western Ontario Research Ethics Board and the need for informed consent was waived. Participating institutions submitted the study to their review process if local approval was required. All activities were compliant with the privacy and confidentiality practices of the participating institutions and the Federal and Provincial governments of Canada. Eli Lilly Canada provided a research grant to London Health Sciences Centre to support trial coordination, data collection, data management and data analysis. The investigators and sites retained control and responsibility for data collection, analysis and interpretation. Data is owned by and resides with London Health Sciences Centre.

3 DECISION TREE APPROACH

In data mining and machine learning, a decision tree is a predictive model, that is, a mapping from observations about an item to conclusions about its target value. In these tree structures, leaves represent classifications and branches represent conjunctions of features that lead to those classifications. The machine learning technique for inducing a decision tree from data is called decision tree learning, or (colloquially) decision trees.

A decision tree is made from a succession of nodes, each splitting the dataset into branches. Generally, the algorithm begins by treating the entire dataset as a single large set and then proceeds to recursively split the set. Three popular rules are typically applied in the automatic creation of

classification trees. The Gini rule splits off a single group of as large a size as possible, whereas the entropy and twoing rules find multiple groups comprising as close to half the samples as possible.

The algorithms construct the tree from the “top” down until some stopping criteria is met. In our current approach, we have used the gain in entropy in order to determine how to best create each node of the tree.

3.1 Entropy

In order to define information gain precisely, we used a measure commonly used in information theory, called entropy, that characterizes the “purity” (or, conversely, “impurity”) of an arbitrary collection of examples. Generally, given a set S , containing only positive and negative examples of some target concept (a so-called two-class problem), the entropy of set S relative to this simple, binary classification is defined as:

$$Entropy(S) = -p_p \log_2 p_p - p_n \log_2 p_n \quad (1)$$

where p_p is the proportion of positive examples in S and p_n is the proportion of negative examples in S . In all calculations involving entropy we define $0 \log_2 0$ to be 0.

One interpretation of entropy from information theory is that it specifies the minimum number of bits of information needed to encode the classification of an arbitrary member of S (i.e., a member of S drawn at random with uniform probability).

If the target attribute takes on c different values, then the entropy of S relative to this c -wise classification is defined as

$$Entropy(S) = \sum_{i=1}^c -p_i \log_2 p_i \quad (2)$$

where p_i is the proportion of S belonging to class i . Note that if the target attribute can take on c possible values, the maximum possible entropy is $\log_2 c$.

3.2 Information Gain

Given entropy as a measure of the impurity in a collection of training examples, we can now define a measure of the effectiveness of an attribute in classifying the data. The measure we will use, called *information gain*, is simply the expected reduction in entropy caused by partitioning the examples according to this attribute. More precisely, the

information gain, $Gain(S, A)$ of an attribute A , relative to a collection of examples S , is defined as

$$Gain(S, A) = Entropy(S) - \sum_{v \in Values(A)} \frac{|S_v|}{|S|} Entropy(S_v) \quad (3)$$

where $Values(A)$ is the set of all possible values for attribute A , and S_v is the subset of S for which attribute A has value v (i.e., $S_v = \{s \in S \mid A(s) = v\}$). Note the first term in the equation for $Gain$ is just the entropy of the original collection S and the second term is the expected value of the entropy after S is partitioned using attribute A . The expected entropy described by this second term is simply the sum of the entropies of each subset S_v , weighted by the fraction of examples $|S_v|/|S|$ that belong to S_v . $Gain(S, A)$ is therefore the expected reduction in entropy caused by knowing the value of attribute A . Put another way, $Gain(S, A)$ is the information provided about the target attribute value, given the value of some other attribute. The value of $Gain(S, A)$ is the number of bits saved when encoding the target value of an arbitrary member of S , by knowing the value of attribute A .

The process of selecting a new attribute and partitioning the training examples is now repeated for each non-terminal descendant node in the tree, this time using only the training examples associated with that node. Attributes that have been incorporated higher in the tree are excluded, so that any given attribute can appear at most once along any path through the tree. This process continues for each new leaf node until either of two conditions is met:

1. Every attribute has already been included along this path through the tree, or
2. The training examples associated with this leaf node all have the same target attribute value (i.e., their entropy is zero).

Some of the variables in the data set are continuous variables, such as temperature. These require a somewhat special approach. This is accomplished by dynamically defining new discrete-valued attributes that partition the continuous attribute value into a discrete set of intervals. In particular, for an attribute A that is continuous-valued, the algorithm can dynamically create a new Boolean attribute A_c that is true if $A < c$ and false otherwise. The only question is how to select the best value for the threshold c . This is done by selecting values for the threshold based on the existing values of the attribute A and computing the

gain. The threshold c that produces the greatest information gain is then chosen.

4 COMPARISON

In this section we compare the results of the decision tree analysis to the results obtained using regression techniques. In particular, we were interested in which variables were identified as key in determining sepsis in the two approaches.

4.1 Regression Analysis

Previous work had focused on the analysis of the data using regression techniques. From a multivariate logistic regression a number of variables emerged as significant in the model (computed using SAS 8.2). The model was very accurate in being able to classify patients not likely to get sepsis (99%) and reasonably accurate at predicting patients that were likely to get sepsis (66%). The variables in the model are summarized in Table 1.

As indicated, we were interested in exploring whether a decision tree analysis technique could provide additional or at least complementary insight into the regression model.

4.2 Decision Tree Analysis

The decision tree analysis yielded 9 distinct paths that led to a determination of sepsis with high probability. The four most frequent of the variables associated with sepsis are shaded in Table 2 along with all variables that appeared in one of these 9 paths.

We tested the accuracy of the tree by randomly removing 30 patients, for whom outcomes were known, regenerating the tree and then tested the accuracy of the tree in predicting whether those 30 patients would develop sepsis or not. Of the 30 patients, 6 had developed sepsis. Using the decision tree to predict the likelihood of developing sepsis for these 6 patients, the tree predicted that 5 would develop sepsis with a likelihood of 100% and the 6th would develop sepsis with a likelihood of 97%. Of the 24 patients that did not develop sepsis, the tree predicted their likelihood with values between 0% and 1.7%, i.e., that it was very unlikely that these patients would develop sepsis. Essentially, the decision tree correctly predicted all 30 of the patients.

Table 1: Logistic Regression Model.

| Variables | P value | Exp(B) |
|--|---------|--------|
| Anaerobe culture | .122 | .317 |
| Abdominal diagnosis | .000 | 15.027 |
| Blood diagnosis | .000 | 3.574 |
| Lung diagnosis | .000 | 10.360 |
| Other diagnosis | .000 | 8.492 |
| Urine diagnosis | .000 | 7.280 |
| Chest X-ray and purulent sputum | .000 | 2.756 |
| Gram negative culture | .047 | .679 |
| Gram positive culture | .001 | .533 |
| Heart rate >90bpm | .000 | 16.933 |
| No culture growth | .000 | .103 |
| PaO2/FiO2 <250 | .000 | 12.305 |
| pH <7.30 or lactate >1.5 upper normal with base deficit >5 | .141 | 1.242 |
| Platelets <80 or 50% decrease in past 3 days | .000 | 5.665 |
| Respiratory rate >19, PaCO2 <32 or Mechanical ventilation | .000 | 8.866 |
| SBP <90 or MAP <70 or Pressure for one hr | .000 | 9.963 |
| Abdominal culture | .259 | 1.872 |
| Blood culture | .000 | 2.311 |
| Lung culture | .724 | .932 |
| Other site culture | .614 | .869 |
| Urine culture | .100 | 1.450 |
| Temperature <36 or >38 | .000 | 8.246 |
| Urinary output <0.5 mL/kg/hr | .000 | 3.166 |
| WBC > 12 or <4 or >10% bands | .000 | 6.281 |
| Yeast culture | .011 | .492 |
| Constant | .000 | .000 |

Details on the variables and their decision points in paths 1, 3, 4 and 9 are provided in Tables 3-6. The variables which appear in these 9 paths of the decision tree are highlighted in the Table 1 of the regression model.

Table 2: Decision Tree Analysis.

| Variables | Path1 | Path2 | Path3 | Path4 | Path5 | Path6 | Path7 | Path8 | Path9 |
|--|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| Lung diagnosis | | | ✓ | ✓ | | ✓ | ✓ | ✓ | ✓ |
| Chest X-ray and purulent sputum | | | ✓ | | | | | | |
| Temperature <36 or >38 | ✓ | | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | |
| WBC > 12 or <4 or >10% bands | ✓ | | | ✓ | | ✓ | | | ✓ |
| No culture growth | | | ✓ | | ✓ | ✓ | ✓ | ✓ | ✓ |
| Heart rate >90bpm | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ |
| SBP <90 or MAP < 70 or pressors for one hour | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ |
| PaO2/FiO2 <250 | ✓ | ✓ | ✓ | ✓ | | | | | |
| Urinary output <0.5 mL/kg/hr | ✓ | ✓ | | | | | | | |
| pH <7.30 or lactate >1.5 upper normal with base deficit >5 | ✓ | ✓ | | | | | | | |
| Respiratory rate >19, PaCO2 <32 or Mechanical ventilation | | ✓ | | | ✓ | | | | ✓ |
| Other diagnosis | | | | | | ✓ | ✓ | | |
| Abdominal diagnosis | | | | | | ✓ | ✓ | ✓ | |
| Platelets <80 or 50% decrease in past 3 days | ✓ | ✓ | | | | | | | |

Note: Underlined check marks are for 'Yes'

Table 3: Decision Tree Analysis Path-1.

| Variables in the path | |
|--|-----|
| Platelets <80 or 50% decrease in past 3 days | Yes |
| pH <7.30 or lactate >1.5 upper normal with base deficit >5 | No |
| Urinary output <0.5 mL/kg/hr | No |
| SBP <90 or MAP < 70 or pressors for one hour | No |
| PaO2/FiO2 <250 | No |
| WBC > 12 or <4 or >10% bands | Yes |
| Temperature <36 or >38 | Yes |
| Heart rate >90bpm | No |

Table 4: Decision Tree Analysis Path-3.

| Variables in the path | |
|--|-----|
| Temperature <36 or >38 | Yes |
| Chest X-ray and purulent sputum | Yes |
| No culture growth | Yes |
| Lung diagnosis | No |
| PaO2/FiO2 <250 | Yes |
| SBP <90 or MAP < 70 or pressors for one hour | No |
| Heart rate >90bpm | Yes |

Table 5: Decision Tree Analysis Path-4.

| Variables in the path | |
|--|-----|
| Temperature <36 or >38 | No |
| WBC > 12 or <4 or >10% bands | Yes |
| Lung diagnosis | Yes |
| PaO2/FiO2 <250 | Yes |
| SBP <90 or MAP < 70 or pressors for one hour | No |
| Heart rate >90bpm | Yes |

Table 6: Decision Tree Analysis Path-9.

| Variables in the path | |
|---|-----|
| Respiratory rate >19, PaCO2 <32 or Mechanical ventilation | Yes |
| WBC > 12 or <4 or >10% bands | Yes |
| Lung diagnosis | Yes |
| No culture growth | Yes |
| SBP <90 or MAP < 70 or pressors for one hour | Yes |
| Heart rate >90bpm | Yes |

5 DISCUSSION

First, all variables appearing in the 9 paths also did appear in the regression model. This provides good support for both the regression model and decision tree result. Interestingly, urine diagnosis had

relatively high beta coefficient in the regression, but did not appear in any of these paths of the decision tree. However, other variables with higher beta coefficients in the regression, such as abdominal diagnosis, lung diagnosis, SBP and temperature, were also important in the tree.

This has implications for practice since clinicians want to apply models of risk at the bedside. Often it is not feasible to collect data on 20 variables, such as those we found in the regression or cluster and models that are easy to use to either rule out patients who are not at risk of sepsis or those who are at risk would be more useful. To test any model we have to ensure that it is reliable and valid. Here we have shown with the 30 patient accuracy test that our tree is reliable and it approaches 100% validity. Our analysis also illustrates the value of multiple methods: 1) in our analysis, regressions can be used to provide a broad estimate of risk, and 2) a more precise estimate in this case can be made using a decision tree. In a separate paper, we will compare a cluster analysis approach to a decision tree. This is outside the scope of this paper. A valid approach for future research is the comparison of cluster analysis, decision trees and regression analysis.

6 CONCLUSIONS

Multiple methods of analysing clinical data provide different perspectives on models of risk of disease. To develop robust models researchers may want to consider regression to get a broad perspective on the risk and utilize decision trees to provide more parsimonious models.

This study has several strengths. This was a prospective observational cohort and the determination of sepsis used standard criteria. The large sample size provided a large number of variables that we could use for our analyses.

Future research will now entail testing the decision tree paths in practice to determine which path is most reliable and valid as well as completing a more in depth measure of the accuracy of the regression and decision tree models. We did not have an opportunity to test other methods such as cluster analysis, Bayesian methods or neural networks, which we hope to do in the future.

ACKNOWLEDGEMENTS

We would like to thank Corey Hilliard for assisting with manuscript preparation.

REFERENCES

- American College of Chest Physicians/Society of Critical Care Medicine Consensus Conference: definitions for sepsis and organ failure and guidelines for the use of innovative therapies in sepsis. (1992). *Crit Care Med*, 20, 864-874.
- Alberti, C., Brun-Buisson, C., Burchardi, H., Martin, C., Goodman, S., Artigas, A., Sicignano, A., Palazzo, M., Moreno, R., Boulme, R., Lepage, E., & Le Gall, R., (2002). Epidemiology of sepsis and infection in ICU patients from an international multicentre cohort study. *Intensive Care Med*, 28, 108-121.
- Angus, D.C., Linde-Zwirble, W.T., Lidicker, J., Clermont, G., Carcillo, J., & Pinsky, M.R. (2001). Epidemiology of severe sepsis in the United States: analysis of incidence, outcome, and associated costs of care. *Crit Care Med*, 29, 1303-1310.
- Bernard, G.R., Vincent, J.L., Laterre, P.F., LaRosa, S.P., Dhainaut, J.F., Lopez-Rodriguez, A. Steingrub, J.S., Garber, G.E., Helterbrand, J.D., Ely, E.W. & Fisher, C.J.Jr. (2001). Efficacy and safety of recombinant human activated protein C for severe sepsis. *N Engl J Med*, 344, 699-709.
- Brun-Buisson, C., Doyon, F., Carlet, J., Dellamonica, P., Gouin, F., Lepoutre, A. Mercier, J.C., Offenstadt, G. & Regnier, B. (1995). Incidence, risk factors, and outcome of severe sepsis and septic shock in adults. A multicenter prospective study in intensive care units. French ICU Group for Severe Sepsis. *JAMA*, 274, 968-974.
- Dellinger, R.P., Levy, M.M., Carlet, J.M., Bion, J., Parker, M.M., Jaeschke, R., Reinhart, K., Angus, D.C., Brun-Buisson, C., Beale, R., Calandra, T., Dhainaut, J.F., Gerlach, H., Harvey, M., Marini, J. J., Marshall, J., Ranieri, M., Ramsay, G., Sevransky, J., Thompson, B.T., Townsend, S., Vender, J.S., Zimmerman, J.L. & Vincent, J. L. (2008). Surviving Sepsis Campaign: international guidelines for management of severe sepsis and septic shock: 2008. *Crit Care Med*, 36, 296-327.
- Knaus, W.A., Draper, E.A., Wagner, D.P., & Zimmerman, J.E. (1985). APACHE II: a severity of disease classification system. *Crit Care Med*, 13, 818-829.
- Knaus, W. A., Wagner, D. P., Draper, E. A., Zimmerman, J. E., Bergner, M., Bastos, P. G., Sirio, C.A., Murphy, D.J., Lotring, T. & Damiano, A. (1991). The APACHE III prognostic system. Risk prediction of hospital mortality for critically ill hospitalized adults. *Chest*, 100, 1619-1636.
- Letarte, J., Longo, C. J., Pelletier, J., Nabonne, B., & Fisher, H. N. (2002). Patient characteristics and costs

- of severe sepsis and septic shock in Quebec. *J Crit Care*, 17, 39-49.
- Levy, M. M., Fink, M. P., Marshall, J. C., Abraham, E., Angus, D., Cook, D. Cohen, J., Opal, S.M., Vincent, J.L. & Ramsay, G (2003). 2001 SCCM/ESICM/ACCP/ATS/SIS International Sepsis Definitions Conference. *Crit Care Med*, 31, 1250-1256.
- Martin, C., Priestap, F., Fisher, H. , Fowler R.A., Heyland, D.K., Keenan, S.P., Longo, C.J., Morrison, T., Bentley, D. & Antman, N.(In Press)A prospective, observational registry of patients with severe sepsis: The Canadian Sepsis Treatment And Response (STAR) Registry. *Crit Care Med*, (in press).
- Minnecci, P. C., Deans, K. J., Banks, S. M., Eichacker, P. Q., & Natanson, C. (2004). Meta-analysis: the effect of steroids on survival and shock during sepsis depends on the dose. *Ann Intern Med*, 141, 47-56.
- Pittet, D., Rangel-Frausto, S., Li, N., Tarara, D., Costigan, M., Rempe, L., Jebson, P. & Wenzel, R.P. (1995). Systemic inflammatory response syndrome, sepsis, severe sepsis and septic shock: incidence, morbidities and outcomes in surgical ICU patients. *Intensive Care Med*, 21, 302-309.
- Rivers, E., Nguyen, B., Havstad, S., Ressler, J., Muzzin, A., Knoblich, B., Peterson, E. & Tomlanovich, M. (2001). Early goal-directed therapy in the treatment of severe sepsis and septic shock. *N Engl J Med*, 345, 1368-1377.
- Salvo, I., de, C. W., Musicco, M., Langer, M., Piadena, R., Wolfler, A., Montani, C. & Magni, E. (1995). The Italian SEPSIS study: preliminary results on the incidence and evolution of SIRS, sepsis, severe sepsis and septic shock. *Intensive Care Med*, 21 Suppl 2, S244-S249.

