

# SCALE ROBUST ADAPTIVE FEATURE DENSITY APPROXIMATION FOR VISUAL OBJECT REPRESENTATION AND TRACKING

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**Abstract:** Feature density approximation (FDA) based visual object appearance representation is emerging as an effective method for object tracking, but its challenges come from object's complex motion (e.g. scaling, rotation) and the consequent object's appearance variation. The traditional adaptive FDA methods extract features in fixed scales ignoring the object's scale variation, and update FDA by sequential Maximum Likelihood estimation, which lacks robustness for sparse data. In this paper, to solve the above challenges, a robust multi-scale adaptive FDA object representation method is proposed for tracking, and its robust FDA updating method is provided. This FDA achieve robustness by extracting features in the selected scale and estimating feature density using a new likelihood function defined both by feature set and the feature's effectiveness probability. In FDA updating, robustness is achieved updating FDA in a Bayesian way by MAP-EM algorithm using density prior knowledge extracted from historical density. Object complex motion (e.g. scaling and rotation) is solved by correlating object appearance with its spatial alignment. Experimental results show that this method is efficient for complex motion, and robust in adapting the object appearance variation caused by changing scale, illumination, pose and viewing angel.

## 1 INTRODUCTION

Visual object tracking is widely demanded in traffic management, pedestrian monitoring, and security inspection. The challenge of visual object tracking is that the changing illumination, changing object's pose, changing viewing angel and partial occlusion will all change the object's scale, size and visible parts. Thus the low-level image features can not be constantly detected across frames without variations, as the feature probability density function (pdf) of the object does not rely on every exact local feature the methods representing an object's as its pdf approximations by feature density approximations (FDA) have emerged as a effective object representation for tracking. Those can be divided into the two groups: parametric approximation and non-parametric approximation. The parametric approximation methods (e.g. Raja, Yu, Jepson et al) used a Gaussian Mixture Model (GMM) to

approximate the object's feature density and Expectation-Maximization (Dempster et al) (EM) to estimate the GMM parameters. To adapt to object's changing appearance, Raja et al update estimate Maximum likelihood (ML) GMM parameter online recursively. However, it is not able to cope with complex motion (e.g. rotation and scaling) because there's no spatial information in their model. Yu & Wu attempted to resolve this issue by extending feature vector by pixel coordinates and track object in an ML estimation process by EM algorithm. Jepson et al developed a three components mixture model to represent object appearance. They used online ML estimation to update the model parameters, but it's not robust when observed data are sparse (object moving in decreasing scale or resolution). For non-parametric FDA methods, Comaniciu et al used spatially weighted kernel functions to represent target object and use mean-shift to determine the kernels. Han et al proposal to

use On-line learning to update kernel density to adapt to object’s appearance variation. However, as pointed by Carreira-Perpinan, the kernel density derived by meanshift developed by Comaniciu et al in the above methods is the ML estimation; it is not capable in providing a robust estimate with sparse data.

In this paper, to solve the above limitations, we propose a robust multi-scale adaptive feature density approximation (FDA) object representation method for tracking, and provide its robust Bayesian updating method using density’s prior knowledge from historical frames. We also solve object complex motion by correlating object appearance with its spatial alignment. Experiment result shows the effectiveness of this method.

This paper is organized as follow: in Section 2 we introduce the object representation for tracking, and robust representation updating method; in Section 3 the experiment and results are presented and discussed; and the paper is concluded in Section 4.

## 2 ROBUST FDA FOR OBJECT REPRESENTATION AND MAP FDA UPDATING

In the proposed object representation method, scale robustness is achieved in both feature extraction and density estimation. The image features are extracted from image patches in the selected scale and size according to local image pattern. and the effective probability for the features from each patch is defined by the size of the patch. Using a new likelihood function defined by the feature sets and their effective probability, the Feature density is estimated robustly to object changing scale. Based on this representation, we also proposal how to measure the compatibility between feature set and its density representation for object tracking. To adapt to an object’s changing appearance, we provide the MAP-EM updating FDA updating method using the density’s conjugate priors to transfer priori knowledge in historical frames to current estimation in a Bayesian way. To cope with object complex motion (e.g. rotation and scaling) we correlate object appearance with the appearance’s spatial alignment by extend feature with spatial coordinates in the coordinate system of the object itself. The following gives the detail description for our method.

### 2.1 Scale Robust Feature Extraction

In our method, scale robust FDA is achieved in both the stages of feature extraction and feature density estimation. As image feature appears in its own scale and size, the robust features should be extracted accordingly. As in our previously works by Liu & Yung, the method partition a frame into multi-scale patches w.r.t. the scale and size of local feature, and extract features on these patches. The process for feature extraction is depicted in Fig. 1, a result is demonstrated in Fig. 2.

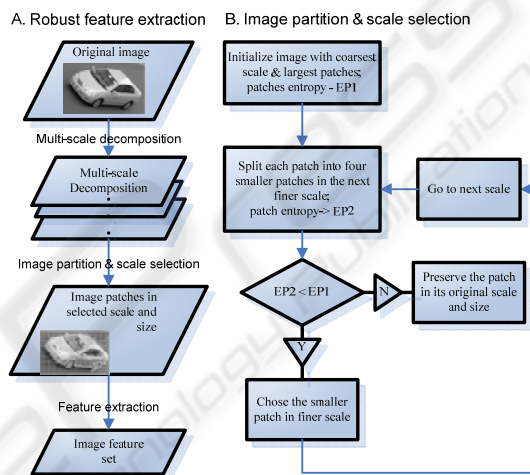


Figure 1: Robust feature extraction.

*This figure depicts the process of scale-robust feature extraction. Diagram A describes the data flow in this process; diagram describes how a frame is partitioned into multi-scale patches. Here Lindeberg’s multi-scale decomposition is used; as suggest by Timor et al, patches’ scale and size are select by comparing entropy across scale.*

After frame partition, an effective probability  $P_i^{creb}$  for each patch is defined on the number of pixels in the patch, to control the contribution of each patch’s feature in FDA.  $P_i^{creb}$  is defined as:

$$P_i^{creb} = Size_i / Size_{max} \tag{1}$$

To solve complex motion (e.g. rotation, scaling), the model should acknowledge the object’s pose. This is achieved through correlating the object appearance feature with its spatial alignment by extending the features’ dimension with the coordinate of patches’ geometry centre in the coordinate system of the object itself (As depicted in Fig. 3) The transformation between the coordinate system of the object  $(x^1, y^1)$  and the coordinate system of original frame  $(x, y)$  is:

$$(x^1, y^1) = (x - m_x, y - m_y) \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix}, \tag{2}$$

where  $(m_x, m_y)$  is the center of the object,  $\theta$  is the rotation angel of object.



Figure 2: Multi-scale patches after image partition.

Image 1 is the original image; image 2 is the partition result. It should be noted that the singularity regions are split into small patches in the fine scale. In the homogeneous regions, large patches in a coarse scale are retained. Image 3 is the final entropy map of each patch.

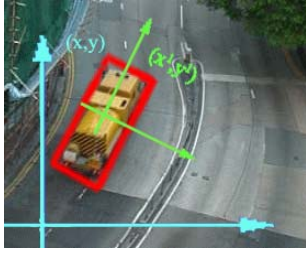


Figure 3: Coordinate system of the frame (blue) and coordinate system the object (green).

## 2.2 Robust Feature Density Approximation

In this paper we approximate the object's feature density by a Gaussian Mixture Model:

$$P(\mathbf{x}_i | \Omega) = \sum_{j=1}^M \omega_j p(\mathbf{x}_i | \omega_j; \theta_j); \quad \Omega = \{\theta_j; \omega_j\}; \quad \theta_j = \{\mu_j, \Sigma_j\}, \quad (3)$$

where  $\omega_j$  is its mixing coefficient,

$$p(\mathbf{x}_i | \omega_j; \theta_j) = (2\pi)^{-1/2} |\Sigma_j|^{-1/2} \exp\left\{-\frac{1}{2}(\mathbf{x}_i - \mu_j)^T \Sigma_j^{-1} (\mathbf{x}_i - \mu_j)\right\}$$

is a Gaussian component.

The robust FDA should be robust to both object's scale variation and the consequent variation in image partition. As the features of large patches correspond to the statistics of more pixels, they will contribute more in FDA than the feature from smaller patches. Therefore, a new likelihood function defined by both the feature observations and their effective probability, is used in GMM estimation. The likelihood function is defined as:

$$\begin{aligned} l(\mathbf{X}; \Omega) &= \log \prod_{i=1}^N P(\mathbf{x}_i; \mathbf{z}; \theta) P_i^{creb} \\ &= \log \prod_{i=1}^N \prod_{j=1}^M [P(\mathbf{x}_i | z_{ij} = 1; \theta) P(z_{ij} = 1) P_i^{creb}]^{z_{ij}} \\ &= \sum_{i=1}^N \sum_{j=1}^M z_{ij} P_i^{creb} [\log P(\mathbf{x}_i | z_{ij} = 1; \theta) + \log P(\omega_j)], \end{aligned} \quad (4)$$

where  $z_{ij}$  is hidden variable indicating  $\mathbf{x}_i$  is generated by which one of the GMM components. Using  $l(\Omega)$  in eq. (4), the Maximum Likelihood estimated for GMM can be computed by EM algorithm:

*E - step :*

$$h_{ij} = E[z_{ij} | \mathbf{x}_i, \theta^k]$$

$$\begin{aligned} p(\omega_j) &= \frac{\sum_{i=1}^N h_{ij} \exp\left\{-\frac{(\mathbf{x}_i - \mu_j^k)^T \Sigma_j^{-1,k} (\mathbf{x}_i - \mu_j^k)}{2}\right\}}{\sum_{i=1}^M \sum_{j=1}^M h_{ij} \exp\left\{-\frac{(\mathbf{x}_i - \mu_j^k)^T \Sigma_j^{-1,k} (\mathbf{x}_i - \mu_j^k)}{2}\right\}} \end{aligned} \quad (5)$$

*M - step :*

$$\begin{aligned} p(\omega_j) &= \sum_{i=1}^N h_{ij} P_i^{creb} / \sum_{i=1}^N P_i^{creb} \\ \mu_j^{k+1} &= \sum_{i=1}^N h_{ij} \mathbf{x}_i P_i^{creb} / \sum_{i=1}^N h_{ij} P_i^{creb} \\ \Sigma_j^{k+1} &= \frac{\sum_{i=1}^N h_{ij} (\mathbf{x}_i - \mu_j^{k+1})(\mathbf{x}_i - \mu_j^{k+1})^T P_i^{creb}}{\sum_{i=1}^N h_{ij} P_i^{creb}}, \end{aligned} \quad (6)$$

Fig. 4 compares effectiveness of the new likelihood for FDA with conventional method which doesn't consider the relationship between the size of the patch and the contribution of its feature in the FDA. Our method solves the problem in conventional method.

Based on this FDA object representation, our method provides measure for tracking by measuring the compatibility of an image region's feature set to a GMM by:

$$P(X | \Omega) = \sum_{j=1}^K \{\omega_j \cdot \phi_j \sum_{\mathbf{x}_i \in X_j} P_i^{creb}\}, \quad (7)$$

$$\text{where } \phi_j = \sum_{\mathbf{x}_i \in X_j} P_i^{creb} \exp\left\{-\frac{1}{2}(\mathbf{x}_i - \mu_j)^T \Sigma_j^{-1} (\mathbf{x}_i - \mu_j)\right\}$$

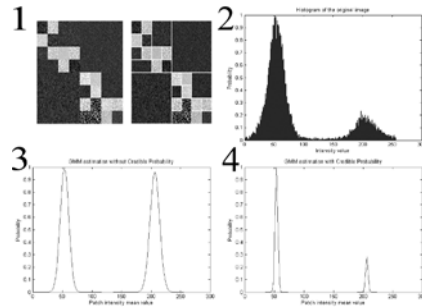


Figure 4: Comparison of FDA in simulation image.

In Figure 4, image 1 is the original image, image 2 is the image histogram, and image 3 is the histogram estimated by conventional method; whereas image 4 is the estimation by the proposed method. The proposed method produces an accurate estimation.

### 2.3 MAP-EM Updating

As object appearance change with changing illumination, scale, pose, and viewing angel, its GMM appearance representation thus should be updated to adapt its changing appearance. As compared by Gauvain et al and Goldberger et al, MAP estimation can be more robust the ML for sparse data (i.e. the feature set) because it utilize the prior knowledge of the model parameter.

We improve the robustness of model updating for sparse data by using the model prior knowledge in GMM conjugate priors (ref. Gamerman) and update GMM by its MAP estimate in a Bayesian way. To achieve scale robustness we also use the new likelihood function in e.q.(4). We derived the updating methods using MAP-EM algorithm. MAP estimation estimate the by maximizing the *a posteriori* probability  $\ell_{MAP}(\Omega) = \ell(\mathbf{X}; \Omega) p(\Omega)$ , thus  $\Omega$  is estimated by:

$$\Omega = \arg \max_{\Omega} \{ \ell(\mathbf{X}; \Omega) p(\Omega) \}, \quad (8)$$

The conjugate prior for the GMM is:

$$\begin{aligned} p(\theta) &= D(\omega | \alpha) \prod_{j=1}^M g(\mu_j, \Sigma_j) \\ &= (2\pi)^{-kd/2} \left\{ \prod_{j=1}^M \omega_j^{\alpha_j - 1} \right\} \times \\ &\quad \left\{ \prod_{j=1}^M c(\alpha_j, \Sigma_j) \eta_j^{1/2} |\Sigma_j|^{-d/2} \exp\left[-\frac{\eta_j}{2} (\mu_j - \mathbf{m}_j)^T \Sigma_j^{-1} (\mu_j - \mathbf{m}_j) - \text{tr}(\Sigma_j \Sigma_j^{-1})\right] \right\} \end{aligned} \quad (9)$$

where  $D(\omega | \alpha)$  is the Dirichlet density distribution for mixing coefficients, and  $\alpha_k > 1$  is its parameter. For the mean vector and the precision matrix (the inverse of covariance matrix) in each GMM Gaussian component, their conjugate priors are the normal distribution and the Wishart distribution. As suggested in Goldberger et al, give the parameters  $(\omega_j, \mu_j, \Sigma_j)$ ,  $j=1 \dots M$  of the GMM of last time step, the parameters of the GMM conjugate prior at the current time step can be extracted as:

$$\begin{aligned} \eta &= \text{constant}, \\ \eta_j &= \eta \omega_j, \mathbf{m}_j = \mu_j, \Sigma_{0j} = \eta \Sigma_j \\ a_j &= \eta_j + d, \alpha_j = \eta \omega_j + 1, \end{aligned} \quad (10)$$

Based on the conjugate prior and the new likelihood function, the auxiliary function for MAP estimation becomes:

$$\begin{aligned} Q(\theta | \theta) &= \log \prod_{i=1}^N \prod_{j=1}^M [P(\mathbf{x}_i | z_{ij} = 1; \theta) P(z_{ij} = 1)]^{p_i^{reb} \times z_{ij}}, \\ &\quad + \log D(\omega' | \alpha) + \log \prod_{j=1}^M g(\mu_j', \Sigma_j') \end{aligned} \quad (11)$$

Therefore we obtained the MAP-EM GMM updating method as:

*E-step*:

$$h_{ij}' = E[z_{ij} | x_i, \theta_k] = \frac{\omega_j G(\mu_j, \Sigma_j)}{\sum_{l=1}^M \omega_l G(\mu_l, \Sigma_l)}, \quad (12)$$

*M-Step*

$$\begin{aligned} \eta_j &= \eta \omega_j, \\ \omega_j' &= \frac{\sum_{i=1}^N z_{ij} P_i^{reb} + \eta \omega_j}{\sum_{i=1}^N z_{ij} P_i^{reb} + \eta} \\ \mu_j' &= \frac{\sum_{i=1}^N z_{ij} P_i^{reb} \mathbf{x}_i + \eta_j \mu_j}{\sum_{i=1}^N z_{ij} P_i^{reb} + \eta_j} \\ \Sigma_j' &= \frac{\sum_{i=1}^N z_{ij} P_i^{reb} (\mathbf{x}_i - \mu_j) (\mathbf{x}_i - \mu_j)^T + \eta_j (\mu_j - \mathbf{m}_j) (\mu_j - \mathbf{m}_j)^T + \eta_j \Sigma_j}{\sum_{i=1}^N z_{ij} P_i^{reb} + \eta_j} \end{aligned} \quad (13)$$

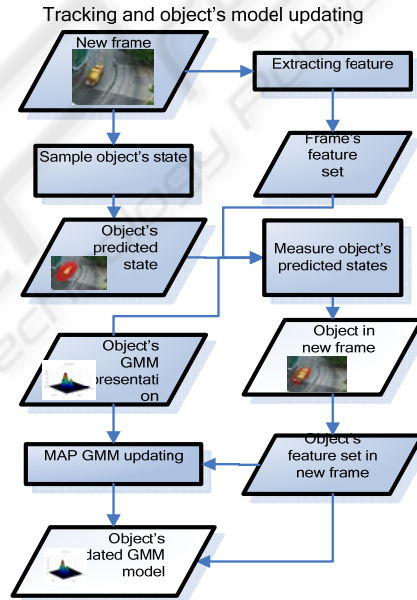


Figure 5: Object tracking and FDA model updating.

### 3 EXPERIMENTAL RESULTS

In the experiment, patches' average value in Lab colour space and centre coordinate are used as the image feature vector; besides small patches, the effectiveness of the non-homogeneous patches' features are also tuned down according to entropy. The state of the object is denoted as:  $\mathbf{s} = (T_1, T_2, \phi, \alpha)$  where  $T_1, T_2, \phi, \alpha$ , are the x, y translation, rotation, and scaling of the object. The object appearance is initialized using eq.(5), eq.(6);

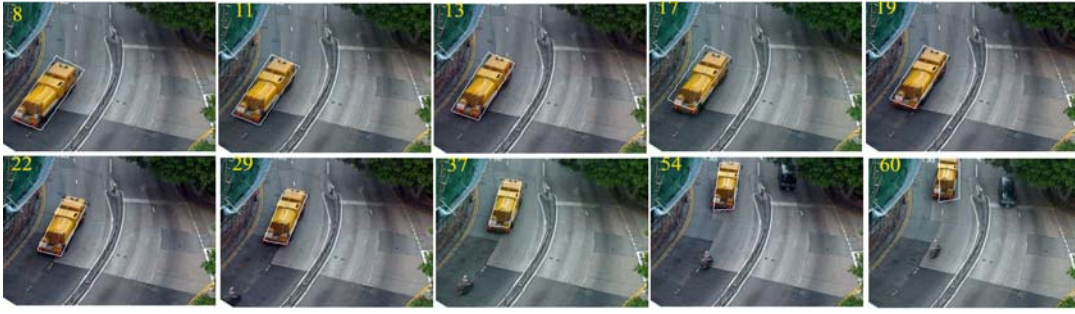


Figure 6: Tracking with complex motion and scale variation.

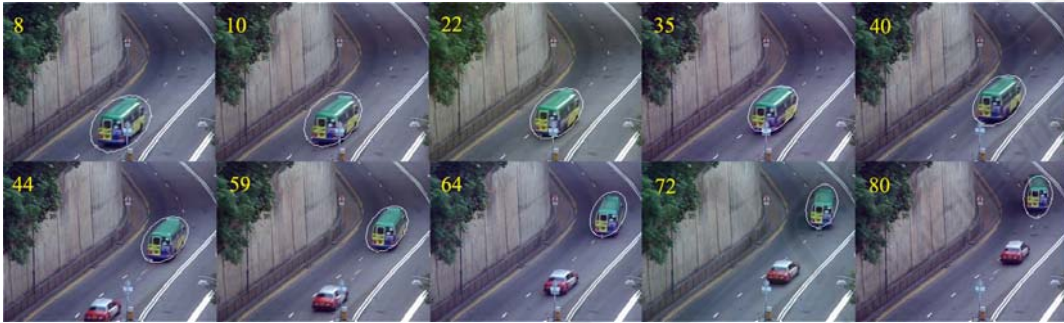


Figure 7: Tracking with complex motion, scale/pose/illumination/appearance variation.

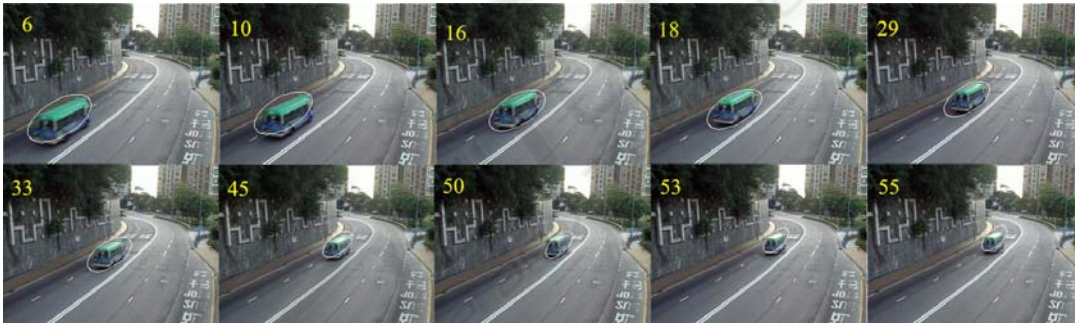


Figure 8: Tracking with appearance variation caused by changing illumination, changing pose, and changing scale.

then visual object is tracked by estimate the optimal object state using the measurement form the proposed FDA appearance representation in a particle filter (Arulampalam et al) framework. Specifically, the posterior probability of  $\mathbf{S}$  is approximated by a set of weighted discrete particles  $\{\mathbf{t}_i^{(j)}, w_i^{(j)}\}_{j=1}^N$ ,  $\sum_{j=1}^N w_i^{(j)} = 1$ , and its MAP estimate

is obtained by choosing the particle with the largest weight. The posterior probability are recursively updated by predict new particles and measure their weights by eq.(7) with GMM and the feature set in image region corresponding to each particle. I.e., the predicted particle is sampled from:  $p(\mathbf{s}_i | \mathbf{y}_{1:i-1}) = \sum_{j=1}^N G(\mathbf{s}_i | \mathbf{t}_{i-1}^j) w_{i-1}^{(j)}$ , and their weights measured

by:

$$w_i^{(j)} = p(\mathbf{t}_i | \mathbf{y}_{1:i}) = p(\mathbf{y}_i | \mathbf{t}_i) = P(X | \Omega) = \sum_{j=1}^K \{\omega_j \cdot \phi_j \sum_{\mathbf{x}_i \in X_j} P_i^{creb}\} \quad (14)$$

where  $\mathbf{y}_i$  is feature set in the image region of particle  $\mathbf{t}_i$ . In model updating the GMM prior knowledge is extracted form the last frame by eq.(10), and the MAP-EM method in eq.(12), eq.(13) is used for GMM updating.

Three experiments are given in Fig. 6~Fig.8. In Fig. 6, the vehicle moves in decreasing scale and change its pose by steering anti-clock wise. The proposed method accurately tracks it with correct scaling and rotation estimate, and capture its pose

precisely even part of the object has moved out of the image. In Fig. 7 & Fig. 8, tracking with significant object appearance variation is tested. In the two experiments, vehicles' visible parts change with its changing steering angle and view point; and the shadow in Fig. 7 and highlight in Fig. 8 were cast onto the vehicles when they move into the upper part, they all bring significant appearance variations to vehicles. The feature set for GMM updating becomes sparse as the number of patches decreases with vehicle's decreasing scale. But in both experiments the proposed method tracks the vehicle accurately with correct pose (scaling & rotation) estimate.

## 4 CONCLUSIONS

In this paper, to solve the above limitations in FDA based object representation method in tracking, we propose a robust multi-scale FDA object representation method for tracking, and provide the robust FDA updating method. Scale robustness is achieved by both robust feature extraction and robust density estimation. The Bayesian model updating method is proposed using model prior knowledge extracted from historical model. Experiment shows the effectiveness of the method. Our future directions could include explorations to different features and tracking by multiple feature fusion. Finally the aim is to develop it to a multiple interacting objects tracking method.

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