

BRAIN COMPUTER INTERFACE

Application of an Adaptive Bi-stage Classifier based on RBF-HMM

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Abstract: Brain Computer Interface is an emerging technology that allows new output paths to communicate the users intentions without the use of normal output paths, such as muscles or nerves. In order to obtain their objective, BCI devices make use of classifiers which translate inputs from the users brain signals into commands for external devices. This paper describes an adaptive bi-stage classifier. The first stage is based on Radial Basis Function neural networks, which provides sequences of pre-assignments to the second stage, that it is based on three different Hidden Markov Models, each one trained with pre-assignment sequences from the cognitive activities between classifying. The segment of EEG signal is assigned to the HMM with the highest probability of generating the pre-assignment sequence.

The algorithm is tested with real samples of electroencephalographic signal, from five healthy volunteers using the cross-validation method. The results allow to conclude that it is possible to implement this algorithm in an on-line BCI device. The results also shown the huge dependency of the percentage of the correct classification from the user and the setup parameters of the classifier.

1 INTRODUCTION

Since that Dr. Hans Berger discovered the electrical nature of the brain, it has been considered the possibility to communicate persons with external devices only through the use of the brain waves (Vidal, 1973).

Brain Computer Interface technology (Wolpaw, J.R.; et al., 2000) is aimed at communicating with persons using external computerized devices via the electroencephalographic signal as the primary command source (Birbaumer, N; et al., 2000); in the first international meeting for BCI technology it was established that BCI “*must not depend on the brain’s normal output pathways of peripheral nerves and muscles*” (Wolpaw, J. R.; et al., 2002). The primary uses of this technology are to benefit persons with blocking diseases, such as: Amiotrophic Lateral Sclerosis (ALS), brainstem stroke, or cerebral palsy; or persons whom have suffered some kind of traumatic accident like for example paraplegic (E. Donchin and K. M. Spencer and R. Wijesinghe, 2000). In order to control an external device using thoughts, it is necessary to associate some mental patterns to device commands. Therefore, an algorithm that detects, acquires, filters, and classifies the electroencephalographic signal is

required (Kostov, A.; Polak, M., 2000) (Pfurtscheller et al., 2000b). Actually different types of classifications can be established for BCI technology, from the physiologic point of view BCI devices can be classified in exogenous and endogenous. The devices in the first group provide some kind of stimuli to the user and they analyze the user’s responds to them, examples of this class are devices based on visual evoked potential or P300 (E. Donchin and K. M. Spencer and R. Wijesinghe, 2000). On the contrary, the endogenous devices does not depend on the user’s respond to external stimuli, they base their operation in the detection and recognition of brain-wave patterns controlled autonomously by the user, examples of this class are devices based on the desynchronization and synchronization of μ and β rhythms (Wolpaw, J. R.; et al., 2002), (Pfurtscheller et al., 2000a), (Pineda, J.A. et al., 2003).

In this paper is presented an endogenous classifier composed of two adaptive stages. In the first stage a Radial Basis Function neural network (Ripley, 2000) performs a pre-classification of the segment of EEG input signal and provides a pre-assignment sequence of data to the second stage. In this second stage is computed the generation probability of the in-

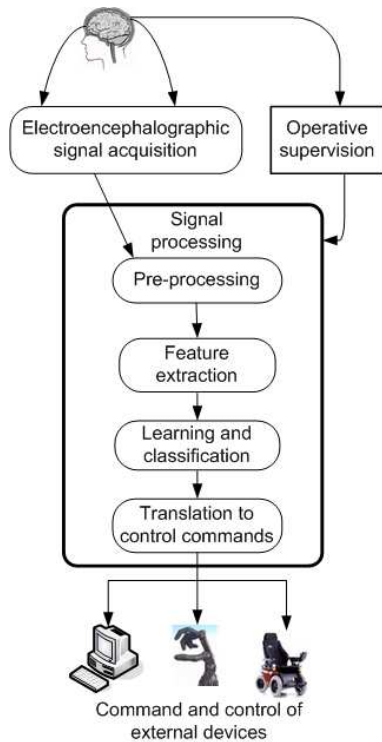


Figure 1: Block diagram of a BCI device.

put sequence by three different Hidden Markov Models, each one had been previously trained with data sequences from the different cognitive activities between classifying.

The content of this paper is as follows:

- Section 2 describes the experimental procedure, the cognitive activities or mental tasks, and the equipment to develop the experiment.
- Section 3 presents the proposed two-stage classifier and describes the algorithms employed in it for training and operation.
- Section 4 presents the results obtained from each volunteer.
- Section 5 analyzes the previous results.
- And finally section 6 is devoted to making conclusions.

2 EXPERIMENTAL PROCEDURE

The tests described below were carried out on five healthy male subjects, one of whom had been trained before but the other four of whom were novices in the use of the system.

In order to facilitate the mental concentration necessary for the proposed activities, the experiments were carried out in a room with a low noise level

and under controlled environmental conditions. For instance, all electronic equipment external to the experiment and unrelated to the subject were switched off in order to avoid electromagnetic artifacts. The experiments were carry out between 10:00 a.m. and 14:00 p.m. The subjects were directed to sit down 50 cm from the screen of the acquisition system monitor, and with their hands in a visible position. The supervisor of the experiment ensured the correct enactment of this process.

2.1 Flow of Activities in the Experimental Process

The experimental process is shown in Figure 2.

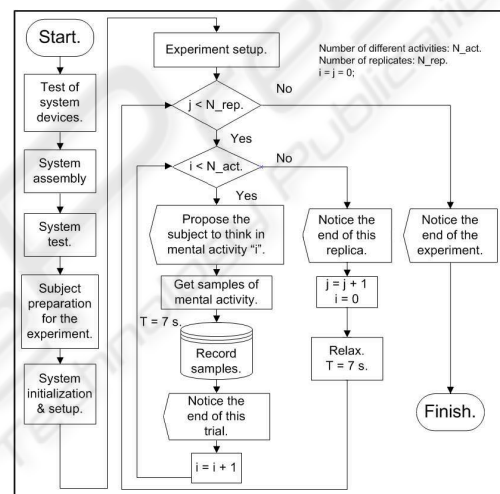


Figure 2: Diagram of the experiment carried out.

System Devices Test. The correct battery level and correct state of the electrodes were checked.

System Assembly. Device connections: superficial electrodes (Grass Au-Cu), battery, bio-amplifier (g.BSamp by g.tec), acquisition signal card (PCI-MIO-16/E-4 by National Instrument), computer.

System Test. The correct operation of the whole system was verified. To minimize noise from the electrical network the Notch filter (50Hz) of the bio-amplifier was switched on.

Subject Preparation for the Experiment. Electrodes were applied to the subject's head. Electrode impedance $\leq 4\text{K}\Omega$ ms.

System Initialization and Setup. The data register was verified. The signal evolution was monitored; it was imperative that a very low component of 50 Hz appeared within the spectrogram.

Experiment Setup. The experiment supervisor set up the number of replications $N_{rep} = 10$, and the quantity of different mental activities. The duration of each trial was $t = 7s$, and the acquisition frequency was $f_s = 384Hz$. The system suggested that the subject think about the proposed mental activity. A short relaxation period was allowed at the end of each trial; between replications the relax time is $t = 7s$.

2.2 Electrode Position

Electrodes were placed in the central zone of the skull, next to C3 and C4 (Penny, W. D.; et al., 2000), and two pairs of electrodes were placed in front of and behind the Rolandic sulcus. This zone has the highest discriminatory power and receives signals from motor and sensory areas of the brain (Birbaumer, N; et al., 2000) (Neuper, C.; et al., 2001). A reference electrode was placed on the right mastoid and two more electrodes were placed near the corners of the eyes to register blinking.



Figure 3: Electrode placement.

2.3 Description of Cognitive Activities

The experiment supervisor asked the subject to figure out the following mental activities; tasks that were used to differentiate between cerebral patterns (Neuper, C.; et al., 2001):

Activity A. Mathematical task. Recursive subtraction of a prime number, i.e. 7, from a large quantity, i.e. 3.000.000.

Activity B. Movement task. The subject imagines moving their limbs or hands, but without actually doing so. It is movement imagery.

Activity C. Relax. The subject relaxes.

3 DESCRIPTION OF THE CLASSIFIER

3.1 Introduction

In Figure 4 is shown the block diagram of the algorithm for the proposed classifier.

In it can be appreciated how the classification of the considered segment of the EEG signal is obtained after the evaluation of the probability generation of

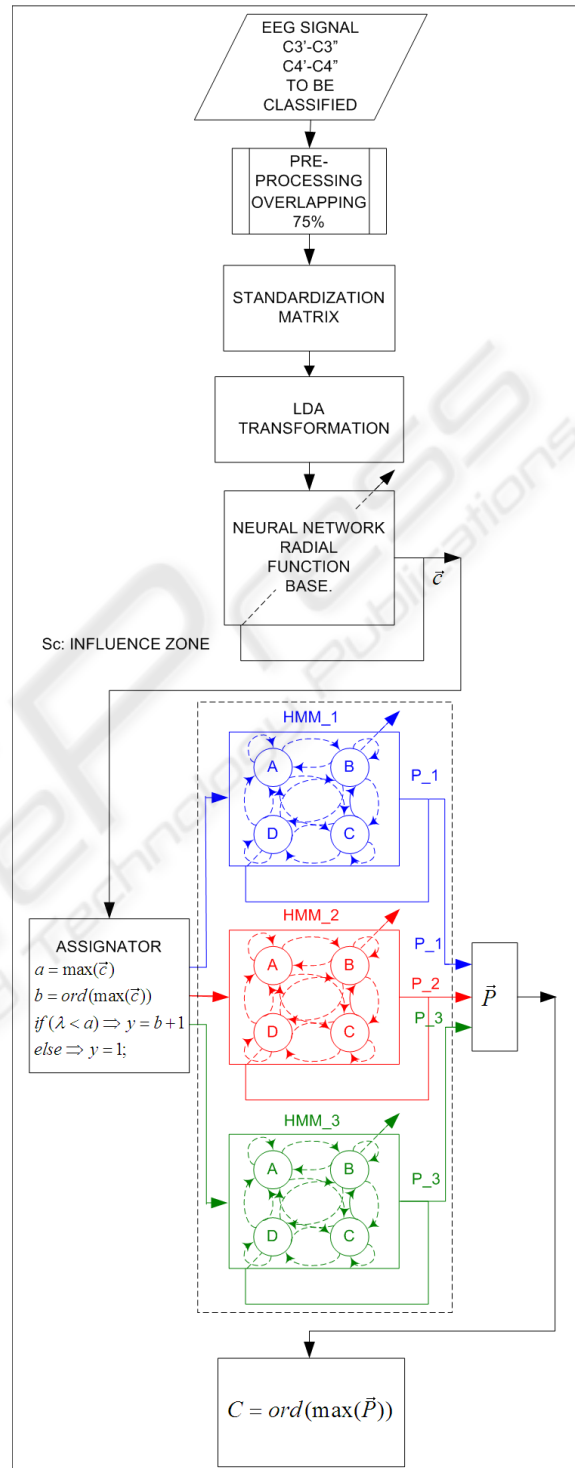


Figure 4: Block diagram of the classifier.

the pre-assignment sequence provided by three Hidden Markov Models.

There are as many Hidden Markov Models as cognitive activities to be considered for the classification,

each model is trained with pre-assignment sequences of data of the cognitive activity associated to it.

The pre-assignment sequence of data are provided by a neural network, which inputs are the vectors of features obtained after the preprocessing of the segment of EEG signal, as it is described in the following subsections.

3.2 Preprocessing

On Figure 5 is depicted the operations associated to the preprocessing phase.

In a first step the EEG signal coming from both electroencephalographic channels C3'-C3'' and C4'-C4'' are sampled and quantified at $f_s = 384\text{Hz}$.

In the next step the samples are bundled in package of $N_w = 128$ samples, it is equivalent to $T_w = 1/3s$. Each group of samples is normalized, in order to obtain homogenous groups of transformed samples with zero mean value and unity as standard deviation.

$$x'_i = \frac{x_i - \mu}{\sigma} \quad (1)$$

This transformation does not affect the frequency properties of the signal, but allows the comparison of groups of samples in the same session or between sessions, it avoids that changes in the impedance of the electrodes or skin conductivity affect the next procedures.

After this the samples are processed by a pass band Butterworth filter of order $n = 6$, with lower and higher frequencies of $f_1 = 4\text{Hz}$ and $f_2 = 40\text{Hz}$ (Proakis and Manolakis, 1997); frequencies outside this band are not common in sane conscious users.

In the next step the filtered samples are convoluted with a Tukey's window of length $N = 128$, this attenuates the leakage effect associated to the package procedure, see Figure 6. Previous studies allow to conclude that the convolution of the signal with this kind of window increase the discrimination capability that the one obtained with other kind of windows as for example: rectangular, triangular, Blackman's, Hamming's, Hanning's or Kaiser's (Martinez, J.L.; Barrientos, A., 2006).

After the convolution, the Fast Fourier Transform, eq.2, is applied in order to obtain the spectral power estimation, eq.3; the obtained frequency resolution is in eq.4.

$$X(k) = \sum_{j=1}^N x(j)w_N^{(j-1)(k-1)}; \quad w_N = e^{-\frac{2\pi j}{N}} \quad (2)$$

$$P(k) = \frac{X(k)^2}{N} \quad (3)$$

$$\Delta f = \frac{f_s}{N_w} = \frac{384}{128} = 3\text{Hz} \quad (4)$$

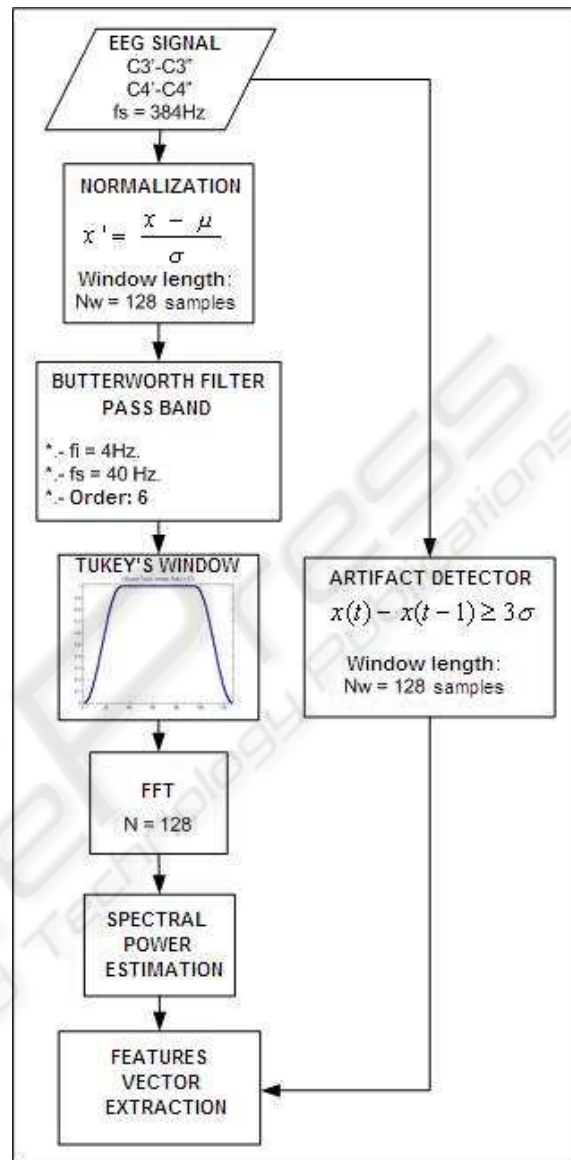


Figure 5: Block diagram for the preprocessing phase.

After the estimation of each frequency band, it is computed the vector of features considering the power average of the involved bands as it is shown on Table 1.

In case of presence of artifacts the algorithm detects them and during the learning phase it substitutes its value by the average value of the samples in that package, if the artifacts are detected in the on-line phase, it instructs the classifier to discard that group of samples.

A group of samples is considered with artifacts if one sample differs more than three standard deviations from the previous one.

Table 1: Feature vector.

| Index | Denomination. | Frequency (Hz). |
|-------|---------------|-----------------|
| 1 | θ . | 6 - 8 |
| 2 | α_1 . | 9 - 11 |
| 3 | α_2 . | 12 - 14 |
| 4 | β_1 . | 15 - 20 |
| 5 | β_2 . | 21 - 29 |
| 6 | β_3 . | 30 - 38 |

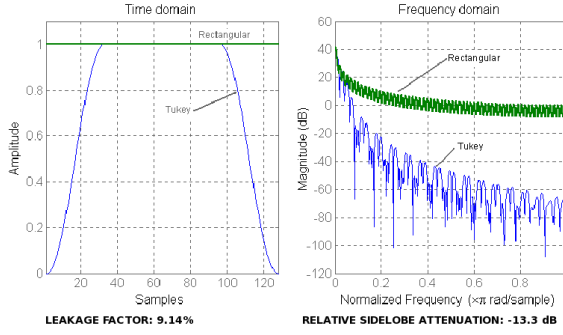


Figure 6: Frequency leakage effect.

3.3 Training of the Neural Network

The considered neural network is the type of Radial Function Basis. This type of neural network is characterized by the learning of the position of the samples in the training set and by the interpolation capability between them (Ripley, 2000).

In Figure 7 is represented the architecture of this type of neural network.

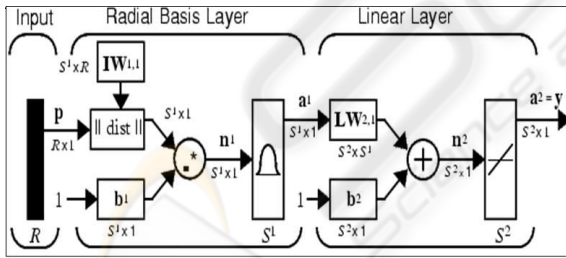


Figure 7: Architecture of the RBF neural network.

From previous studies it has been concluded that this type of neural network behaves better than other types of neural networks, as for example Multi-Layer Perceptrons or Probabilistic Neural Networks (Martinez, J.L.; Barrientos, A., 2008).

The activation function is:

$$\text{radbas}(x) = e^{-x^2}; \quad x = (\vec{w} - \vec{p}) * S_c \quad (5)$$

In where \vec{w} and S_c are respectively the weights and influence zone constant of each neuron, and \vec{p} is the position of the considered sample.

During the learning phase the neurons of the hidden layer learn the position of the samples of the learning set, \vec{w} ; during the test phase when a new sample \vec{p} is presented, it is computed the distance between the sample and the learned positions, the nearest neurons to the sample will proportionate higher activation values than the rest of the neurons.

For the learning process are considered vectors of features from the EEG signal, acquired when the user was performing one of the different cognitive activities considered for the classification. The learning set is composed by the 75% of all the sample set, and the other 25% is considered for validation. After the determination of the learning and validation sets, the input vectors to the neural network are normalized, and with LDA technique is reduced their dimensionality projecting the original input vectors in the direction of the highest discrimination capability (Martinez, J.L.; Barrientos, A., 2007).

In order to minimize the over-learning effect, the RBF learning process allows a dynamic growth of the number of neurons in the hidden layer. In the output layer are considered as many linear neurons as cognitive activities between discriminate. Finally in the assignation block on Figures 4, it is weighted the output vector of the neural network and it assigns the input vector to the activity with highest output value provided it is higher than a threshold λ , on the contrary if the value is lower than λ , the input vector is labeled as unclassified.

On operation, once the neuronal network has been trained, when a new vector is presented the cognitive activity, with samples nearer to it, will provide a higher activation level, and the corresponding output will have a higher value than the others cognitive activities.

3.4 Description of Hidden Markov Models

A Hidden Markov Model is a double stochastic statistical model, it consists of a Markov process with unknown and non-observable parameters, and a observed model which parameters depend stochastically from the hidden states. A stochastic process is called a Markovian process if the future does not depend from the past, only from the known present; considering the stochastic variable $q(t-1)$ the transition probability in the instant t is defined as $P(q_t = \sigma_t | q_{t-1} = \sigma_{t-1})$. A Markov chain is formally defined with the pair (Q, A) , where $Q = \{1, 2, \dots, N\}$ are the possible estates of the chain and $A = [a_{ij}]$ is the transition matrix of the model, with the constrains:

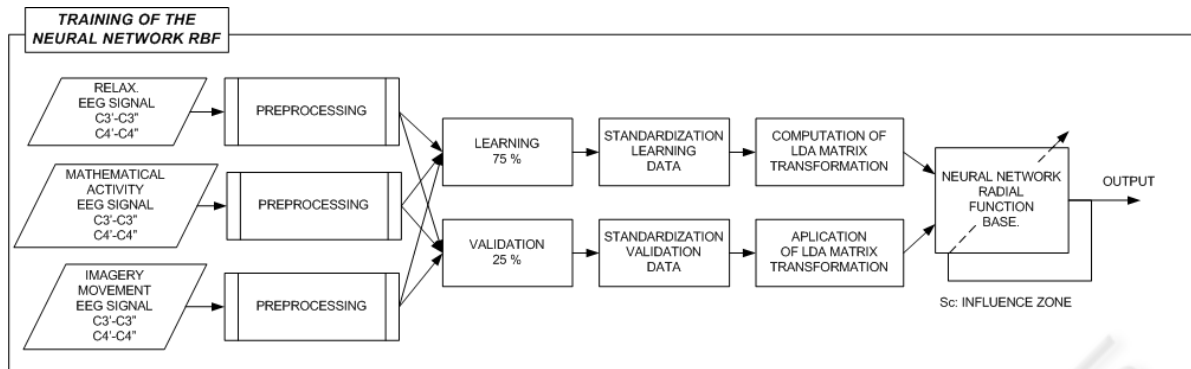


Figure 8: Training of the RBF neural network.

$$0 \leq a_{ij} \leq 1; \quad 1 \leq i, j \leq N \quad (6)$$

$$\sum_{j=1}^N a_{ij} = 1; \quad 1 \leq i \leq N \quad (7)$$

The transition and emission probabilities depends from the actual estate and no from the former estates.

$$P(q_t = j | q_{t-1} = i, q_{t-2} = k, \dots) = P(q_t = j | q_{t-1} = i) = a_{ij}(t) \quad (8)$$

Formally a discrete HMM of first grade is defined by the 5-tuple: $\lambda = \{Z, Q, A, B, \pi\}$, in where:

- $Z = \{V_1, V_2, \dots, V_M\}$ is the alphabet or discrete set of M symbols.
- $Q = \{1, 2, \dots, N\}$ is the set of N finite estates.
- $A = [a_{ij}]$ is the transition matrix of the model.
- $B = (b_j(Q_t))_{N \times M}$ is the matrix of emission symbols, also known as observation matrix.
- $\pi = (\pi_1, \pi_2, \dots, \pi_N)$ is the prior probability vector of the initial estate.

The parameters of a HMM are $\lambda = \{A, B, \pi\}$. There are three types of canonic problems associated to HMM (Rabiner, 1989)(Rabiner and Juang, 1986):

1. Given the parameters of the model, obtain the probability of a particular output sequence. This problem is solved through a forward-backwards algorithm.
2. Given the parameters of the model, find the most probable sequence of hidden estates, that could generate the given output sequence. This problem is solved through the use of Viterbi algorithm.
3. Given an output sequence, find the parameters of the HMM. This problem is solved through the use of Baum-Welch algorithm.

The HMM have been applied specially in speech recognition an generally in the recognition of temporal sequences, hand written, gestures, and bioinformatics (Rabiner and Juang, 1986).

3.5 Training of the Hidden Markov Models

The HMM's are trained with sequences of pre-assignments coming from the EEG samples, as it is shown in the Figure 9.

For each cognitive activity a particular HMM, with the following characteristics, is trained:

- Number of hidden estates: 4.
- Number of different observable objects: 4

In the training phase, chains of nine pre-assignments were used. In a previous experiment with synthetic samples, it was concluded that for the proposed architecture of Hidden Markov Models the highest percentage of correct classifications were obtained with chains of nine elements.

After the training or solution of the third canonic problem, the probability matrices of state transitions and observation matrices are determined. The Viterbi algorithm is used in order to determine the probability that a model generates the proposed sequence.

4 RESULTS

In order to test the behavior of the proposed algorithm, the influence of the threshold assignment parameter (λ), and the influence zone of the neuron (S_c), the EEG samples of the session tests from the volunteers were used as follows:

4.1 Evaluation of the Learning Capability

With a subset of 75% of the all EEG samples the algorithm was trained with different λ and S_c values:

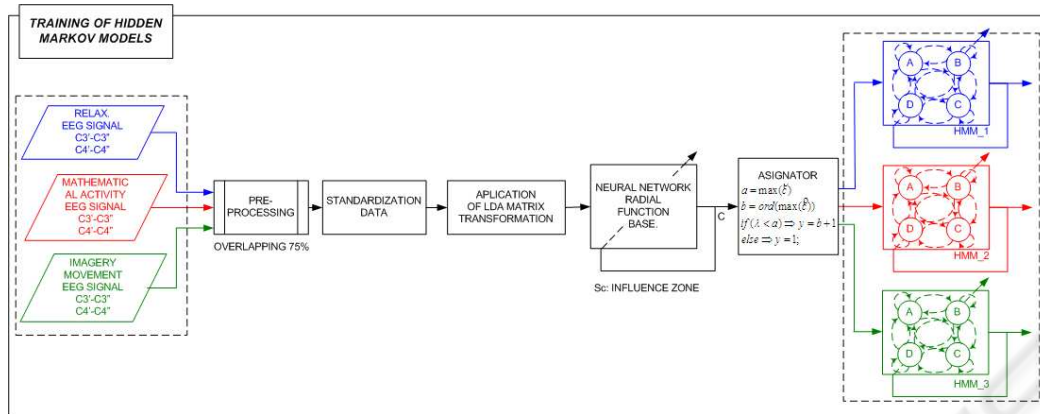


Figure 9: Training of the HMM.

| | | | |
|-------------|------|------|-----|
| $\lambda =$ | 0.55 | 0.65 | 0.8 |
| $S_c =$ | 0.5 | 0.95 | |

These values have been fixed after a seek in wide with the samples of the first volunteer.

After the learning, the same samples were processed with the trained algorithm, and a comparison between the results obtained with the algorithm and the ones employed for the learning was done, in all cases a 100% of correct classification has been obtained.

4.2 Evaluation of the Generalization Capability

After the good results obtained from the learning phase, a cross-validation methodology is used to estimate the generalization capability. From the whole ten sessions, nine are used for learning and one is used for validation, the process is repeated ten times changing each time the session used for validation.

In the following tables are shown the results obtained for each volunteer, considering the λ and S_c parameters.

Table 2: Volunteer: Al01.

| $S_c = 0.5$ $\lambda = 0.65$ | | | $S_c = 0.95$ $\lambda = 0.55$ | | | $S_c = 0.5$ $\lambda = 0.55$ | | | $S_c = 0.95$ $\lambda = 0.80$ | | |
|---------------------------------|-----|-----|----------------------------------|-----|----|---------------------------------|----|----|----------------------------------|----|-----|
| 94 | 103 | 103 | 94 | 81 | 87 | 93 | 92 | 87 | 86 | 97 | 81 |
| +4 | +14 | +14 | +4 | -10 | -3 | +3 | +2 | -3 | -4 | +8 | -10 |

Table 3: Volunteer: Ro01.

| $S_c = 0.5$ $\lambda = 0.65$ | | | $S_c = 0.95$ $\lambda = 0.55$ | | | $S_c = 0.5$ $\lambda = 0.55$ | | | $S_c = 0.95$ $\lambda = 0.80$ | | |
|---------------------------------|----|----|----------------------------------|-----|-----|---------------------------------|----|----|----------------------------------|-----|-----|
| 103 | 97 | 92 | 118 | 109 | 118 | 97 | 87 | 86 | 117 | 106 | 110 |
| +14 | +8 | +2 | +31 | +21 | +31 | +8 | -3 | -4 | +30 | +18 | +22 |

For each combination, the process is replicated three times. In the upper row it is shown the number of correct classifications. In the lower row it is

Table 4: Volunteer: Ja01.

| $S_c = 0.5$ $\lambda = 0.65$ | | | $S_c = 0.95$ $\lambda = 0.55$ | | | $S_c = 0.5$ $\lambda = 0.55$ | | | $S_c = 0.95$ $\lambda = 0.80$ | | |
|---------------------------------|----|-----|----------------------------------|----|-----|---------------------------------|-----|-----|----------------------------------|-----|-----|
| 106 | 97 | 110 | 87 | 90 | 107 | 99 | 106 | 107 | 98 | 108 | 99 |
| +18 | +8 | +22 | -3 | 0 | +19 | +10 | +18 | +19 | +9 | +20 | +10 |

Table 5: Volunteer: Da01.

| $S_c = 0.5$ $\lambda = 0.65$ | | | $S_c = 0.95$ $\lambda = 0.55$ | | | $S_c = 0.5$ $\lambda = 0.55$ | | | $S_c = 0.95$ $\lambda = 0.80$ | | |
|---------------------------------|-----|-----|----------------------------------|----|----|---------------------------------|----|-----|----------------------------------|----|----|
| 109 | 102 | 104 | 83 | 92 | 92 | 106 | 91 | 110 | 86 | 87 | 92 |
| +21 | +13 | +15 | -8 | +2 | +2 | +18 | +1 | +22 | -4 | -3 | +2 |

Table 6: Volunteer: Ra01.

| $S_c = 0.5$ $\lambda = 0.65$ | | | $S_c = 0.95$ $\lambda = 0.55$ | | | $S_c = 0.5$ $\lambda = 0.55$ | | | $S_c = 0.95$ $\lambda = 0.80$ | | |
|---------------------------------|----|-----|----------------------------------|----|-----|---------------------------------|-----|-----|----------------------------------|-----|-----|
| 106 | 97 | 110 | 87 | 90 | 107 | 99 | 106 | 107 | 91 | 76 | 99 |
| +18 | +8 | +22 | -3 | 0 | +19 | +10 | +18 | +19 | +1 | -15 | +10 |

Table 7: Volunteer: Ra02.

| $S_c = 0.5$ $\lambda = 0.65$ | | | $S_c = 0.95$ $\lambda = 0.55$ | | | $S_c = 0.5$ $\lambda = 0.55$ | | | $S_c = 0.95$ $\lambda = 0.80$ | | |
|---------------------------------|-----|----|----------------------------------|-----|-----|---------------------------------|-----|----|----------------------------------|-----|----|
| 102 | 102 | 98 | 102 | 107 | 114 | 103 | 105 | 96 | 116 | 99 | 98 |
| +13 | +13 | +9 | +13 | +19 | +26 | +14 | +16 | +6 | +29 | +10 | +9 |

shown the percentage of improvement against a naive classifier.

5 DISCUSSION

From the results of the proposed classification algorithm, it is observed that:

- The learning capability is better that the one achieved only with the RBF neural network (Martinez, J.L.; Barrientos, A., 2008).
- From the analysis of the results of the replicas it has been detected that the variability in the percentage of correct classifications is caused by the HMM's, both in the learning and validation phases. The sequences of pre-assignments pro-

vided by the neural network were stable, but the generation probabilities of the HMM's changed in each replica. In the learning phase the HMM's probabilities allowed a perfect classification, but they were not maintained in the cross validation phase; for this stage a lower percentage of correct classification was obtained, as it is summarized in the tables 2 to 7. But until in this case, almost in all replicas, the cross-validation test results were better than the ones hoped from a naive classifier.

- The values of correct classifications depend highly from the user. There has not been identified a pair of λ and S_c values which proportionate the highest percentage of correct classification for all users. The discrepancy in the results between RA1 and RA2 is explained by the user's learning process, session RA1 is previous to RA2.

6 CONCLUSIONS

The information inside the pre-assignment sequences improves the classification capability, therefore the Hidden Markov Model technique is useful for the extraction and use of this information in an On-line BCI device.

The scattering of the maximum values, of the correct classifications obtained from the cross-validation tests, shows that the combination of λ and S_c parameters are highly dependent on the user, for this reason a BCI device based in this kind of algorithm should have a setup stage, that allows to initialize correctly these parameters.

On the other hand, the algorithm behaves better than a naive algorithm, but it is not as good as it should be taking into account the good results obtained during the learning phase. The size of the learning data set is critical in the results obtained during the validation phase. With a bigger learning data set the validation results will improve, because of the minimization of the overlearning.

In future applications the algorithm presented in this paper will be used as kernel for an on-line classifier embedded in a BCI device. The on-line use of this device will allow to assess how the different kinds of user's feedbacks modify the classification capability.

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