

# A MULTI-AGENT MODEL FOR SIMULATING THE IMPACT OF SOCIAL STRUCTURE IN LINGUISTIC CONVERGENCE

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**Abstract:** Baronchelli (Baronchelli et al., 2006) introduced a very simple model for simulating language emergence in communities of agents without any predetermined protocol. Brigatti (Brigatti, 2008) introduced the notion of Reputation in Baronchelli's model, demonstrating how this parameter has an impact in the final results of the process. In a previous paper, we have shown that reputation is a key element in the coevolution of language and social structures in societies with asymmetrically distributed reputation. This paper presents a system for simulating linguistic convergence in static and dynamic populations with asymmetrically distributed reputation and a graphical representation of such process.

## 1 INTRODUCTION

This paper investigates the relationship between social parameters and language evolution by means of simulation of linguistic convergence. The questions the paper address are the following: Has reputation a crucial role in convergence time? Is there any coevolution of social structures and language? Can social structure block linguistic convergence?

To develop the topic, we use an algorithm that allow a community of agents to agree about naming an object without any preestablished protocol. In this algorithm we give a key role to reputation in the starting of communication. Simulations with this algorithm try to establish the main parameters of  $t_{conv}$ ,  $t_{max}$ ,  $W_{max}$ ,  $W_{dif}$ . The program gives also the output of a graph structure that represents a social network built up from successful linguistic interactions. These graphs can be analysed from a mathematical point of view.

The paper is structured as follows: in Section 2 we introduce the main algorithm and the concepts we are dealing with. Section 3 explains the main results obtained with the model. Finally, Section 4 gives some discussion and ideas for future research.

## 2 MODEL

The model is based in the one introduced by (Baronchelli et al., 2006). Baronchelli's model is a

variant of the naming game (Steels, 1997) and its design tries to be as simple as possible, assuming the cognitive deficiencies this implies. In Baronchelli's system, a number of agents have to agree in naming an object with no preestablished protocol. Two chief features of the design are that: a) the agents have nothing in the beginning, and b) when two agents agree in a word, they delete everything else they have stored. Mathematical and physical results obtained by this model seem to show that language convergence and evolution follow some rules that can be computationally approached and simulated.

After Baronchelli's work, Brigatti introduced the concept of reputation in the process of linguistic convergence, pointing out the possibility of analysing the influence of such parameter in language evolution.

The present paper modifies the original model in a way that two agents are allowed to communicate only under several circumstances, if their reputations are "compatible". We start imagining a society divided in two different social groups. Each one of this groups has a reputation  $R$ . The group with the highest reputation is called  $H$ , and the group with the lower reputation is called  $L$ .  $R_H \neq R_L$  and by definition  $R_H > R_L$ .  $\delta = R_H - R_L$ .  $\delta$  has an important impact in the convergence process, but for simplicity, in this paper, we are using only  $\delta/20$ , focusing in the role some other parameters have in the evolution.

Our system will simulate a population of 100 agents, divided into two different groups  $H$  and  $L$ , so as  $|H| + |L| = 100$ . The way to describe a population

will be  $H\%/L\%$ . In the initial configuration agents do not have any linguistic knowledge. The final goal is to reach, for the whole population a common meaning for an object  $M$ , in a way that, at the end, every agent will have only one word stored, and this word will be the same for every agent. The system does not stop if such configuration is not reached.

The main protocol for every step of communication is:

- i. Select randomly a speaker  $S$ . Select randomly a hearer  $H$ , so as  $H \neq S$ .
- ii. **if**  $S$  and  $H$  compatible, **then**:
  - $S$  selects a word
    - **case**  $H$  does not have any word stored, it invents one,  $W_i$ .
    - **case**  $H$  has some words stored, it chooses one,  $W_i$ .
  - $S$  send  $W_i$  to  $H$ .
  - **if**  $W_i$  was already in  $H$  **then**:
    - *success*.  $S$  and  $H$  delete everything keeping only  $W_i$ .
    - FINISH
  - **else**:
    - *failure*.  $H$  stores  $W_i$ .
    - FINISH
- iii. **else**: FINISH.

We imagine two types of societies in what refers to protocols of communication:

- Societies where group communication is allowed. In these societies, members of  $L$  can communicate between them, and members of  $H$  can communicate between them. The communication is allowed if  $R_S \geq R_H$ .
- Societies where group communication is not allowed. In these societies, it is required for communication that  $R_S > R_H$ .

From the point of view of reputation, we consider two different types of societies:

- Dynamic populations: those in which reputation varies as a result of communication (Dynamic R).
- Static populations: those in which reputation does not change (Static R).

From here, there are four main cases which are considered in this paper:

- $R_S \Rightarrow R_H$  and static R (GS)
- $R_S \Rightarrow R_H$  and dynamic R (GD)
- $R_S > R_H$  and static R (NGS)
- $R_S > R_H$  and dynamic R (NGD)

In each one of these cases, the following parameters will be studied:

- The convergence, or not, of the language of the population
- $t_{conv}$ , the total time the system takes to reach the convergence.
- $W_{max}$ , the maximum number of words the system reaches at time  $t_{max}$
- $W_{dif}$ , the maximum number of different words
- $t_{max}$ , the time where the system gets  $W_{max}$
- The graph configuration.

In a precedent paper (submitted), it has been demonstrated that some of the best results are obtained in populations 20/80 and  $\delta 20$ . The configuration used for simulations, with populations of 100 agents, takes also  $\delta 20$  and the every distribution of population from 10/90 to 90/10.

For a sake of simplicity - to get understandable graphs - simulations with graphs have been designed with only 20 agents and the same configuration 20/80 with  $\delta 20$

### 3 DESCRIPTION AND BEHAVIOUR OF THE SYSTEMS

In this section describe in more detail the structure of every one of the classes mentioned above (GS, GD, NGS, NGD) and explore the results with every type of society arisen from the previous one: GS, GD, NGS, NGD. Later, we compare this results to understand what of the configurations is optimal, in terms of time and space, to generate consensus words.

#### 3.1 Systems with Static R and Group Communication: GS Societies

These systems correspond to a population with two different social groups where individuals of each one of them are allowed to communicate to others in the same group, and the individuals of  $L$  can only hear/learn - but not speak to - individuals of  $H$ . On the contrary, members of  $H$  speak to  $L$ , but they never learn or listen them. However, when  $S$  and  $H$  belong to the same group, no restrictions about the roles are established.

To design the program to simulate such behaviour, we take the general algorithm with a modification in line [ii], which finally will be as follows:

- ii. **if**  $R_S \geq R_H$ , **then**:

### 3.1.1 Results

The results with  $R_S \geq R_H$ ,  $R = \delta 20$ , and different configurations of  $H/L$ , are the following (Table 1):

Table 1: Results for populations with static R and group communication: GS.

GS	$t_{conv}$	$t_{max}$	$W_{max}$	$Wd_{max}$
10/90	14435	708	398	51
20/80	5066	743	385	52
30/70	4421	753	378	51
40/60	3923	790	375	50
50/50	3678	779	367	49
60/40	3238	764	368	48
70/30	3207	753	371	47
80/20	2887	702	377	47
90/10	2680	685	389	48

Table 1 explains that, for societies in which it is allowed to communicate between the individuals of the same group and R does not change, the best configuration for reaching a consensus language in both, time and number of words, is 90/10. This is the optimal configuration, mainly in what refers to parameter  $t_{conv}$ . Like in other societies with reputation, 10/90 has extremely bad results for  $\delta 20$ . However, every parameter optimises with 90/10. Regarding to  $t_{max}$ ,  $W_{max}$  and  $Wd_{max}$ , they also have the best behaviour with 90/10, although their improvements are smaller than in  $t_{conv}$ .

Such systems generate a graph similar to the one in Figure 1.

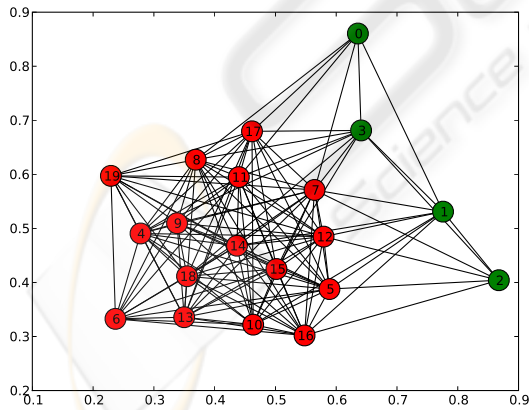


Figure 1: Graph at  $t_{conv}$  in societies with static R and group communication: GS.

## 3.2 Systems with Dynamic R and Group Communication: GD

This case refers societies where, in principle, every type of communication is allowed. In addition, these societies have the capacity to evolve, creating new groups of reputation or simply not forbidding individuals to change. To obtain this systems, we need to implement some changes in the points [ii.] and [iii.] of the general algorithm, in order to introduce the parameter of dynamic R.

We see in the algorithm how the only reputation that varies at each communication act is speaker's reputation, as (Brigatti, 2008) suggested in his paper.

- ii. **if**  $R_S \geq R_H$ , **then:**
  - S selects a word
  - S send  $W_i$  to H.
  - **if**  $W_i$  was already in H **then:**
    - *success.* S and H delete everything keeping only  $W_i$ .
    - $R=R+1$
    - FINISH
  - **else:**
    - *failure.* H stores  $W_i$ .
    - $R=R-1$
    - FINISH
- iii. **else**
  - $R=R-1$
  - FINISH

### 3.2.1 Results

Comparing Table 1 and Table 2 we can see how, for  $t_{conv}$ , the results in GD are more stable for every configuration of H/L. Some variation exists, but it is smaller. For  $t_{conv}$  90/10 is still the best group distribution, like in GS, but for  $t_{max}$  and  $W_{max}$  the tendency is to increase the complexity with greater groups  $H$ . The number of different words generated by the system remains almost the same for every H/L.

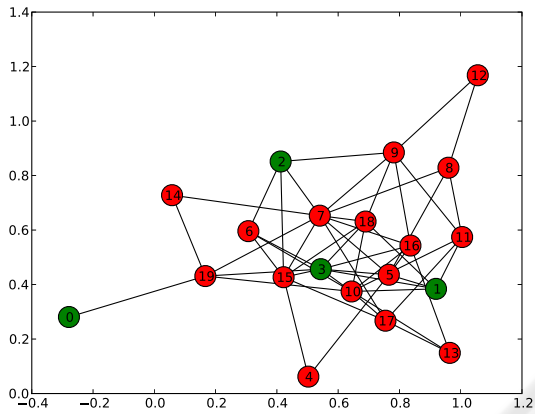
Such systems generate graphs with the one in Figure 2.

## 3.3 Systems with Static R Without Group Communication: NGS

Societies with static R without group communication are not able to converge, unless the total number of agents in H is 1. This means that, for societies with 100 agents, we need the configuration 1/99, and for 1000 agents 0.1/99.9.

Table 2: Results for populations with dynamic R and group communication: GD.

GD	$t_{conv}$	$t_{max}$	$W_{max}$	$Wd_{max}$
10/90	5320	986	400	61
20/80	5881	1024	387	59
30/70	5758	993	382	58
40/60	5121	1048	384	57
50/50	4901	1063	385	56
60/40	4935	1056	391	55
70/30	4993	1101	400	55
80/20	5049	1139	416	57
90/10	4656	1101	420	59

Figure 2: Graph at  $t_{conv}$  in societies with dynamic R and group communication: GD.

The protocol is modified from the general one in a way that it says:

ii. if  $R_S > R_H$ , then:

This prevents individuals from the same group to communicate.

### 3.3.1 Results

After a number of communication steps, the society reaches a star graph. This is typically produced by non convergent populations in which agents are only allowed to speak with the ones with lower capacity. So, a great part of the population cannot produce any word. Communication with agents with the same reputation is forbidden. This implies that the only possible communication is from agents in H as speakers to agents in L as hearers. Therefore, no word generated by an individual from L can be spread. Agents in L can never have a successful communication as a speakers.

Provided that convergence is not possible, the program tries to find the number of communication steps that are necessary to reach the final stable star config-

uration  $t_{star}$ , and the number the number of words in  $t_{star}$ . The results showed in Table 3 are obtained with only one run, so as they are only indicative. Nevertheless, looking at the results for  $t_{star}$  – about 100 times slower that  $t_{conv}$  in GS, GD, NGD – it is easy to see how difficult is, for such populations, to evolve. The number of words in  $t_{star}$ ,  $W_{star}$  is very similar to  $W_{max}$  in the other systems, what suggests that the stable configuration is achieved close to  $t_{max}$ .

Table 3: Results for populations with dynamic R and group communication: NGS.

NGS	$t_{star}$	$W_{star}$
10/90	425226	259
20/80	478117	325
30/70	576348	322
40/60	787554	335
50/50	657670	301
60/40	848112	333
70/30	1024541	235
80/20	1203182	228
90/10	864363	183

The resultant star graph is found in 3. In it,  $\forall i \in H$ ,  $deg(i) = |L|$ , and  $\forall ij \in L$ ,  $deg(j) = |H|$ .

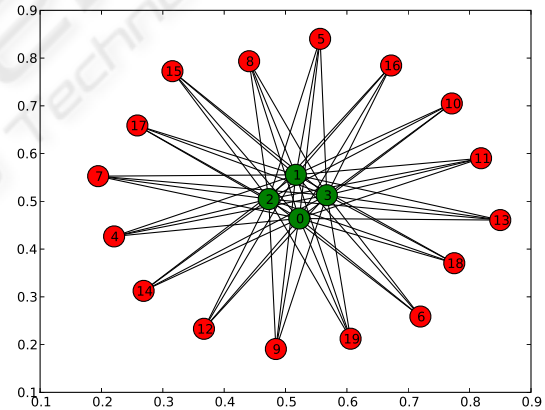


Figure 3: Star society in populations with static R and non group communication: NGS.

### 3.4 Systems with Dynamic R without Group Communication: NGD

On the contrary than NGS, populations with non group communication but with dynamic reputation, are able to converge. The general procedure is modified as follows:



- ii. **if**  $R_S = R_H$ , **then**:
  - S selects a word
  - S send  $W_i$  to H.
  - **if**  $W_i$  was already in H **then**:
    - *success*. S and H delete everything keeping only  $W_i$ .
    - $R=R+1$
    - FINISH
  - **else**:
    - *failure*. H stores  $W_i$ .
    - $R=R-1$
    - FINISH
- iii. **else**
  - $R=R-1$
  - FINISH

### 3.4.1 Results

Following the tendency of *GD* systems, *NGD* there is an improvement in  $t_{conv}$  from 10/90 to 90/10, but the system is more efficient in configurations 10/90 as for  $t_{max}$ ,  $W_{max}$ . The number of different words seems to increase from 10/90 to 90/10, with a central depression, centered in 40/60. This can be seen in Table 4.

Table 4: Results for populations with dynamic reputation without group communication: *NGD*.

<i>NGD</i>	$t_{conv}$	$t_{max}$	$W_{max}$	$Wd_{max}$
10%	6243	1162	362	60
20%	6731	1199	360	56
30%	6372	1267	374	54
40%	6134	1302	384	55
50%	5959	1320	399	57
60%	6070	1324	410	60
70%	5956	1421	417	64
80%	5761	1455	430	67
90%	5855	1448	434	69

Figure 4 shows a graph with 20 agents generated for *NGD* systems with a 20/80 distribution.

## 4 GENERAL RESULTS

The most important result achieved in this paper is that populations with non-group communication and static R (*NGS*) do not converge. However, they form stable types of social structures, that slowly evolve up to reach a star configuration that does not change. If external factors do not apply, such societies will compute for ever without any consensus, but with a strong stable configuration.

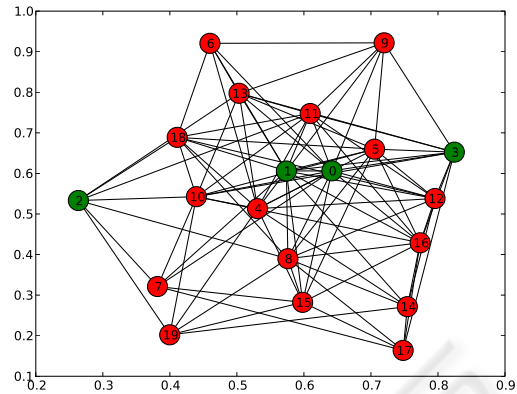


Figure 4: Graph at  $t_{conv}$  in societies with dynamic R without group communication.

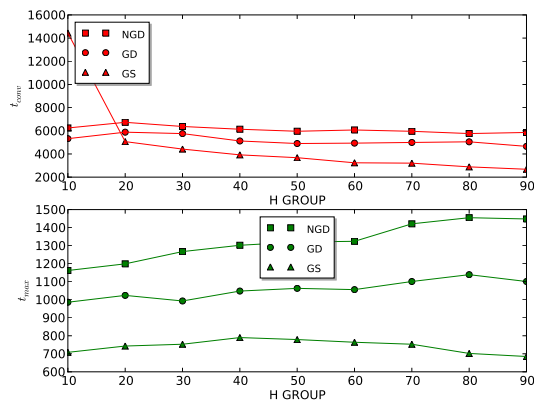
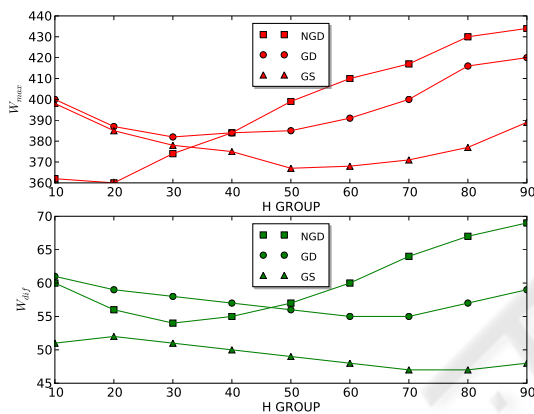
The other types of societies (*GS*, *GD* and *NGD*) converge, although they have different behaviours, that can be seen in Figure 5 for time, and Figure 6 for space (words).

Regarding convergence time (Figure 5), the results are clear. With the exception of configuration 10/90 in *GS* systems, by difference the worst possible one, it seems that *GS* always has better results than *GD*, and *GD* always is faster than *NGD*. This means that systems with group communication obtain always better results than societies without group communication. On the other hand, societies with static R seem to be faster to reach the convergence than societies with dynamic R. The first affirmation seems trivial and was expected. The second one is surprising. Finally the combination of the fastest option – static – with the variant of non-group communication is not even able to converge.

As for  $t_{max}$  (Figure 5), the results are not so different. The exception is that the configuration 10/90 for *GS* works in a regular way.

Figure 6 shows how the results for time and space are quite different. Regarding the maximum number of words in the system, *GS* and *GD* follow curve distributions, with similar results in both extremes and a depression in the center, with minimum results in balanced distributions H/L. However *NGD* obtains clearly more efficient results with configurations 10/90 and 20/80, and then starts increasing. As a consequence, being *NGD* the configuration with the best results for low values of H, this is the group that needs a greater amount of words with  $H \geq 50$ .

$Wd_{max}$  has a similar distribution for *GS* and *GD*. But *NGD* does not have the optimal results it obtained with low values of H. Therefore, static societies with group communication always need the lowest number of different words to converge.

Figure 5:  $t_{conv}$  and  $t_{max}$  for GS, GD and NGD.Figure 6:  $W_{max}$  and  $W_{d_{max}}$  for GS, GD and NGD.

## 5 CONCLUSIONS

This paper is a preliminary approach with some partial results about the role of dynamic/static reputation in societies, in combination with the parameter of group communication. The first results show that computational simulation of linguistic processes related with social issues can be very fruitful, since we have obtained surprising results in this first approach.

Among the issues that should be investigated in this line of research, we can remark:

- the impact of different values of  $\delta$ , since this paper is based on simulations performed with  $\delta=20$ ;
- the study of the configuration of the graphs;
- testing of the program with large populations;
- the evolution of reputation in dynamic populations.

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