

# EXTENDED VISUAL CRYPTOGRAPHY SCHEME FOR COLOR IMAGES WITH NO PIXEL EXPANSION

Xiaoyu Wu, Duncan S. Wong and Qing Li

*Department of Computer Science, City University of Hong Kong, Tat Chee Avenue, Hong Kong, China*

Keywords: Information hiding, Extended visual Cryptography, Secret sharing.

Abstract: A  $k$ -out-of- $n$  Extended Visual Cryptography Scheme (EVCS) is a secret sharing scheme which hides a secret image into  $n$  shares, which are also some images. The secret image can be recovered if at least  $k$  of the shares are superimposed, while nothing can be obtained if less than  $k$  shares are known. Previous EVCS schemes are either for black-and-white images or having pixel expansion. In this paper, we propose the first  $k$ -out-of- $n$  EVCS for color images with no pixel expansion. The scheme also improves the contrast of the  $n$  shares and the reconstructed secret image (i.e. the superimposed image of any  $k$  or more shares) by allowing users to specify the level of each primary color (i.e. Red, Green and Blue) in the image shares as well as the reconstructed secret image.

## 1 INTRODUCTION

In (Naor and Shamir, 1994), Naor and Shamir introduced the notion of Visual Cryptography Scheme (VCS) which allows an image to be encrypted so that the decryption can be done simply by the human visual system without any other computation. A  $k$ -out-of- $n$  VCS splits an image to  $n$  shares so that they look indistinguishable from random noise. These shares are then printed on transparencies as images. From any less than  $k$  shares, nothing (other than the size) of the secret image can be obtained. Only by superimposing  $k$  or more shares, the secret image will become visible.

In (Naor and Shamir, 1994), an extension of VCS called Extended Visual Cryptography Scheme (EVCS) was also introduced. In an EVCS, besides generating  $n$  shares for a secret image, these  $n$  shares also carry  $n$  meaningful and independently chosen images. To generate these shares, a user arbitrarily chooses  $n$  meaningful images which have the same size as the secret image. Then the user splits the secret image and embed the share information into the  $n$  meaningful images in such a way that given any  $k - 1$  or less shares, no information about the secret image can be obtained, while given any  $k$  or more shares, the secret image will be revealed when the shares are superimposed. In (Ateniese et al., 1996), Ateniese et al. proposed the first  $k$ -out-of- $n$  EVCS for black-and-white images using the hypergraph coloring method.

It is for black-and-white images. Since then, there have been some other EVCS schemes proposed, e.g. (Nakajima and Yamaguchi, 2002; Wang et al., 2009; Sirhindi et al., 2009). To the best of our knowledge, there is no EVCS for color images that supports the general  $k$ -out-of- $n$  secret sharing while having no pixel expansion, that is, the pixel expansion rate being equal to one.

In this paper, we solve this problem by proposing the first  $k$ -out-of- $n$  EVCS for color images *without* pixel expansion. We use a probabilistic technique (Yang, 2004) for achieving no pixel expansion. The scheme also allows a user to choose the number of color levels for each primary color (i.e. Red, Green and Blue) that the reconstructed image and each share image could have. The reconstructed image refers to the image obtained by imposing  $k$  or more share images. We find that this 'tunable' feature is very useful (in practice), as the user is able to use it for maximizing the quality of the reconstructed image, given that different types of images may best appear with different color levels (more details will be given in the later part of the paper).

## 2 A BRIEF REVIEW OF $K$ -OUT-OF- $N$ BLACK-AND-WHITE VCS

In this section, we briefly review a generic representation of the  $k$ -out-of- $n$  VCS scheme for black-and-

white images(Naor and Shamir, 1994). A  $k$ -out-of- $n$  VCS scheme for black-and-white images is represented by two collections of  $n \times l$  boolean matrices. The two collections are denoted by  $C_0$  and  $C_1$ . Matrices in  $C_0$  (resp.  $C_1$ ) are obtained by permuting all the columns of a *Basic Matrix*  $B_0$  (resp.  $B_1$ ). Formally,  $C_0$  and  $C_1$  are represented as follows.

$C_0 = \{\text{matrices obtained by permuting the columns of}$

$$B_0 = \begin{bmatrix} p_{0,0}^0 & p_{0,1}^0 & \cdots & p_{0,l-1}^0 \\ \vdots & \vdots & \ddots & \vdots \\ p_{n-1,0}^0 & p_{n-1,1}^0 & \cdots & p_{n-1,l-1}^0 \end{bmatrix},$$

$C_1 = \{\text{matrices obtained by permuting the columns of}$

$$B_1 = \begin{bmatrix} p_{0,0}^1 & p_{0,1}^1 & \cdots & p_{0,l-1}^1 \\ \vdots & \vdots & \ddots & \vdots \\ p_{n-1,0}^1 & p_{n-1,1}^1 & \cdots & p_{n-1,l-1}^1 \end{bmatrix},$$

where  $p_{i,j}^0, p_{i,j}^1 \in \{0, 1\}$  for  $0 \leq i \leq n - 1$  and  $0 \leq j \leq l - 1$ .

Due to the page limitation, we refer readers to (Naor and Shamir, 1994) for details of the representation. In the next section, we use a black-and-white VCS described above as a building block to build a  $k$ -out-of- $n$  color EVCS which does *not* have pixel expansion. Note that the pixel expansion rate of the VCS above is  $l > 1$ .

### 3 OUR $K$ -OUT-OF- $N$ EVCS FOR COLOR IMAGES

We now propose a  $k$ -out-of- $n$  EVCS for color images. The scheme is the first EVCS for color images with *no* pixel expansion. For a color secret image, suppose that  $n$  meaningful images have already been chosen. These images are color images chosen arbitrarily and will be used for generating  $n$  share images. Also, the choosing processing is totally independent as long as the image size is the same as that of the secret image since our scheme does not have any pixel expansion. Our scheme consists of the following steps: 1. Histogram Generation; 2. Color Quality Determination; 3. Grouping; 4. Share Creation. These steps are elaborated in detail as follows.

#### 3.1 Histogram Generation

For the secret image and each of the  $n$  images which will be used as share images, we first generate three primary-color (i.e.  $R, G, B$ ) component images for

each of them and then create a histogram for each primary-color component image. As an example, suppose that the secret image is the Lena image which is encoded in 24-bit RGB. Figure 1 shows the secret image (Lena) and the three RGB primary-color component images of it. In each component image, there are 256 levels of intensity of the corresponding primary color. Figure 2 shows the histogram of the red component generated in this step. In the histogram of  $R$  (resp.  $G$  and  $B$ ), the horizontal axis represents the intensity of  $R$  (resp.  $G$  and  $B$ ) ranging from 0 to 255 and the vertical axis represents the number of pixels in the  $R$  (resp.  $G$  and  $B$ ) component image that have the intensity value.

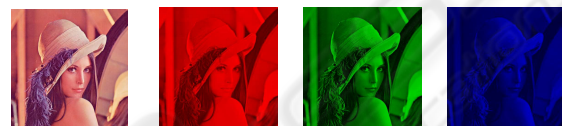


Figure 1: The secret image (Lena) and its RGB component images.

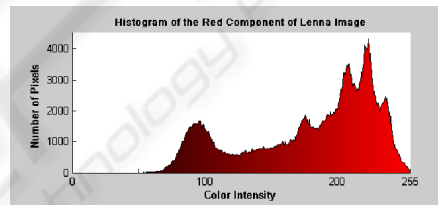


Figure 2: Histogram of the red component image.

#### 3.2 Color Quality Determination

In this step, the user is to choose the number of intensity levels that the reconstructed image will have when at least  $k$  share images are superimposed and the number of intensity levels of each share image. First, the user is to determine the number of intensity levels for maximizing the quality of the reconstructed image or shares. Let  $N$  be the number of intensity levels that the reconstructed image will have. As the reconstructed image has three primary-color components, we set  $N = N_R \times N_G \times N_B$ , where  $N_X$  denotes the number of the intensity levels of  $X \in \{R, G, B\}$  primary-color component of the reconstructed image. For the  $n$  share images, let  $M_i$  be the number of intensity levels of the  $i$ -th share image (for  $i = 1, \dots, n$ ), where  $M_i = M_{iR} \times M_{iG} \times M_{iB}$ , where  $M_{iX}$  denotes the number of intensity levels of  $X \in \{R, G, B\}$  component of the  $i$ -th share. In Sec. 4, we provide more discussions on how to choose the number of color levels.

### 3.3 Grouping

As of the previous step, this step is carried out on each of the  $n$  share images as well as the secret image. In the following, we use the secret image as an example to describe how the grouping works. For each primary color  $X \in \{R, G, B\}$ , we partition the histogram of  $X$  of the secret image into  $N_X$  groups so that each group has the same area as other groups on the histogram, where  $N_X$  is the number of color intensities for the  $X$  component of the (to-be)-reconstructed secret image determined in the previous step. By the same area on a histogram, it implies that there will be an equal number of pixels in each of the  $N_X$  groups on the histogram. Figure 3 shows the histogram of the red primary-color component images of Lena after grouping where  $N_R = 4$ . In the figure, we use different color intensities to represent different groups.

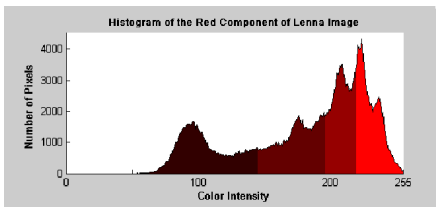


Figure 3: Histogram of  $R$  illustrating the  $4 \times 4 \times 4$  color levels.

### 3.4 Share Creation

The final step of the scheme is to create the  $n$  share images. To create these shares, we start with by creating  $n$  shares for each primary color. After creating all the shares of the three primary colors, we then superimpose the three shares corresponding to the three primary colors of the  $i$ -th share,  $1 \leq i \leq n$ , for forming the  $n$  final shares. In the following, we describe how the  $n$  shares of each primary color  $X \in \{R, G, B\}$  are created.

1. We first construct a  $k$ -out-of- $n$  black-and-white EVCS. The construction can be viewed as an extension of the  $k$ -out-of- $n$  black-and-white VCS reviewed in Sec. 2. The extension is similar to the method due to Wang, Yi and Li (Wang et al., 2009).
  - (a) Take a  $k$ -out-of- $n$  black-and-white VCS which satisfies the conditions in Sec. 2. Let the Basic Matrices  $B_0$  and  $B_1$  are of dimension  $n \times l$ .
  - (b) Then, we construct  $2^n$  boolean matrices denoted by  $A^{c_1, \dots, c_n}$  for  $c_1, \dots, c_n \in \{b, w\}$ , where  $b$  stands for *black* and  $w$  stands for *white*. Each of  $A^{c_1, \dots, c_n}$  will be  $n \times t$  for some integer  $t \geq \lceil \frac{n}{k-1} \rceil$ . In each row of  $A^{c_1, \dots, c_n}$ , for example, the

$i$ -th row, all the  $t$  bits but one must be 1. The remaining bit is 1 if  $c_i = b$  and is 0 if  $c_i = w$ . We denote this bit as  $*$  in the following. In other words, each row of  $A^{c_1, \dots, c_n}$  has only one  $*$ . Besides, the number of  $*$  in each column of  $A^{c_1, \dots, c_n}$  should be at most  $k-1$ .

- (c) The  $k$ -out-of- $n$  black-and-white EVCS is defined as the following Basic Matrices:  $T_0^{c_1, \dots, c_n} = B_0 \circ A^{c_1, \dots, c_n}$  and  $T_1^{c_1, \dots, c_n} = B_1 \circ A^{c_1, \dots, c_n}$  for  $c_1, \dots, c_n \in \{b, w\}$ . Therefore, there are altogether  $2^{n+1}$  Basic Matrices and they can be considered as two sets of Basic Matrices, that is,  $\{T_0^{c_1, \dots, c_n}\}_{c_1, \dots, c_n \in \{b, w\}}$  and  $\{T_1^{c_1, \dots, c_n}\}_{c_1, \dots, c_n \in \{b, w\}}$ , each set has  $2^n$  Basic Matrices. Each of these matrices is  $n \times m$  where  $m = l + t$  where  $B_0$  and  $B_1$  are  $n \times l$  and  $A^{c_1, \dots, c_n}$  are  $n \times t$ . We refer readers to (Wang et al., 2009) for the details of how this  $k$ -out-of- $n$  black and white EVCS works.

In the next step, we use the Basic Matrices  $T_0^{c_1, \dots, c_n}$  and  $T_1^{c_1, \dots, c_n}$  in a *probabilistic* way on each RGB primary-color component image so that the share images created will have the same size as the original secret image (i.e. no pixel expansion or having the optimal pixel expansion rate of 1).

2. This step is carried out pixel by pixel for the secret image. For each primary color  $X \in \{R, G, B\}$  of a pixel in the secret image, we carry out the following steps:
  - (a) On the  $X$  histogram of the secret image, suppose that the color intensity of the pixel with respect to primary color  $X$  is in the  $k$ -th group (where  $0 \leq k \leq N_X - 1$ ). We compute a probability value  $P_X = k / (N_X - 1)$  which determines the likelihood of going through one of the following steps.
  - (b) With probability  $P_X$ , we carry out the following two steps:
    - We look into  $n \times l$  Basic Matrix  $B_0$  of the  $k$ -out-of- $n$  black-and-white VCS and the general form  $A^{c_1, \dots, c_n}$ .
    - With probability  $P_1$ , which is determined by the user as follows, we randomly pick a column from  $B_0$ ; The trade-off between the quality of share images and the reconstructed image is the result of adjusting the value of  $P_1$ . The greater (less) the  $P_1$  is, the higher (lower) the quality of the reconstructed image would be and the lower (higher) the quality of the share images would be.
    - With probability  $1 - P_1$ , suppose the color intensity of the  $X$  primary-color component

of the corresponding pixel in the  $i$ -th meaningful image is in the  $k_{i_X}$ -th group (where  $0 \leq k_{i_X} \leq M_{i_X} - 1$  and  $1 \leq i \leq n$ ), we compute a probability value  $Q_{i_X} = k_{i_X} / (M_{i_X} - 1)$ . We then set the  $*$  in the  $i$ -th row of the general form  $A^{c_1, \dots, c_n}$  to 0 with the probability  $Q_{i_X}$  and to 1 with the probability  $1 - Q_{i_X}$  and randomly choose a column from it.

- Consider the column chosen as an  $n$ -bit vector. For the first bit, we assign the black color (i.e. 0 color intensity) if the bit is 1, otherwise we assign  $X$  primary color (i.e. 255 color intensity) to the corresponding pixel in the first share image. This continues until we have assigned colors to the corresponding pixel on all the  $n$  share images.
- (c) With the probability  $1 - P$ , we carry out similar steps to the above, but change  $B_0$  to  $B_1$ .
3. Finally, we superimpose the  $i$ -th  $R$  share with the  $i$ -th  $G$  share and the  $i$ -th  $B$  share, for  $i = 1, \dots, n$ , to form the final  $i$ -th color share image.

#### 4 DETERMINING THE NUMBER OF COLOR LEVELS

In this section, we discuss how to choose the number of color levels (i.e.  $N = N_R \times N_G \times N_B$ ) in the reconstructed secret image and the share images. As the scheme allows a user to arbitrarily choose the number of color levels, we observe that the number of color levels has a significant impact on the quality of the reconstructed image and the share images. The number of color levels should be chosen depending on the number of colors of the original  $n + 1$  images. In the following, we take the reconstructed image as an example.

We first identify the secret image as belonging to one of the following two categories: in category 1, the number of levels of a particular primary color is small, for example, less than 4; and in category 2, the number is large, say at least 4. For images in category 1, if the image on a particular primary color  $X \in \{R, G, B\}$  is  $OriginalN_X$ , since  $OriginalN_X$  in this case is small, there is no need to try with different color levels. We should just set  $N_X$  to  $OriginalN_X$ . Images that fall into this category could be texts or logos. Figure 4 and Figure 5 show the images of text, their corresponding shares and the reconstructed image (Lena) for the case of 2-out-of-2 EVCS,  $N_R = N_G = N_B = M_{i_R} = M_{i_G} = M_{i_B} = 2$  (where  $i = 1, 2$ ).

For images in category 2, one may try the color level  $N_X$  from a small value, say 2 or 4, to the “full”

**Secret Sharing**      **Extended Scheme**

Figure 4: The images of the text.

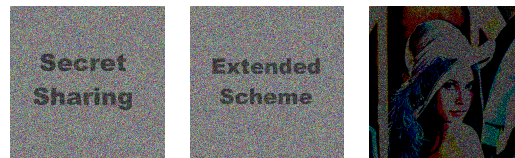


Figure 5: The two shares and the reconstructed image of the text.

level, i.e.  $OriginalN_X$ . Based on our experimental results, we observe that for photos or color cartoon images with large number of color levels, trying these three values (namely 2, 4 or  $OriginalN_X$ ) for the value of  $N_X$  can already attain one of the best results in the reconstructed images.

#### REFERENCES

Ateniese, G., Blundo, C., Santis, A. D., and Stinson, D. R. (1996). Visual cryptography for general access structures. *Inf. Comput.*, 129(2):86–106.

Nakajima, M. and Yamaguchi, Y. (2002). Extended visual cryptography for natural images. *Journal of WSCG*, 10(2):303–310.

Naor, M. and Shamir, A. (1994). Visual cryptography. In *Advances in Cryptology - EUROCRYPT '94*, pages 1–12. Lecture Notes in Computer Science, Vol. 950.

Sirhindi, R., Afzal, M., and Murtaza, S. (2009). An extended secret sharing scheme for colour images with fixed pixel expansion. *International Journal of Electronic Security and Digital Forensics*, 2(1):58–67.

Wang, D., Yi, F., and Li, X. (2009). On general construction for extended visual cryptography schemes. *Pattern Recognition*, 42(11):3071–3082.

Yang, C. N. (2004). New visual secret sharing schemes using probabilistic method. *Pattern Recognition Letters*, 25(4):481–494.