

FORMALLY MODELING AND ANALYZING DATA-CENTRIC WORKFLOW USING WFCP-NET AND ASK-CTL

Zhaoxia Wang^{1,2,3,4,5}, Jianmin Wang^{2,4,5}, Lijie Wen^{2,4,5} and Guiming Luo^{2,4,5}

¹Department of Computer Science, Tsinghua University, Beijing, China

²School of Software, Tsinghua University, Beijing, China

³Department of Logistical Information Engineering, Logistical Engineering University, Chongqing, China

⁴Key Laboratory for Information System Security, Ministry of Education, Beijing, China

⁵National Laboratory for Information Science and Technology (TNList), Beijing, China

Keywords: Business Entity, Data-centric Workflow, WFCP-net, ASK-CTL, Workflow Modeling, Workflow Analyzing.

Abstract: Despite the abundance of workflow analysis techniques from control-flow perspective, there is hardly any method for workflow verification from data processing perspective. In this paper, we restrict the WFCP-net, a Colored Petri Net with WF-net structure, to formally describe the key business entities in a data-centric workflow model. Then, we use ASK-CTL logic to describe the workflow requirements on business data processing perspective. The model checking method is adopted into our verification approach, which can explore some of the business contraventions of data perspectives in the workflow models. The effectiveness of our works has been validated with the CPN Tools.

1 INTRODUCTION

In the past decade years, abundant analysis techniques have been developed to analyze workflow models (Aalst et al. 2008). These analysis techniques focus on verifying design errors (deadlock, livelock, etc.) from control-flow perspective. In addition to control-flow structure, data processing semantic is also a critical factor to guarantee the workflow correctness. Sometimes, improperly data processing may cause workflow structural errors. Further, misunderstanding data processing semantic may make the workflow model violating the business requirements of stakeholders. Unfortunately, there is lack of methods for workflow verification from data processing perspective. The main reason is that the traditional process-centric workflow modeling approach focuses on control-flow perspective rather than data processing.

Fig. 1 shows a simple customer order process. It is a classical example in UML textbook (Booch et al. 2005). When a customer *order* arrives, task *T1* receives the order. Subsequently, the order is accepted or rejected. Once the task *T3* rejects the order, the process is ended. Otherwise, the process goes to task *T2* to accept the *order*. After the task *T2*

is executed, a business entity *shiplist* is created. And then, the task *T4* and *T5* are executed. In the end, task *T5* is executed and the *order* is archived. Fig. 1(a) is a conceptual model only from the control-flow perspective and the model hasn't any design error from control-flow perspective.

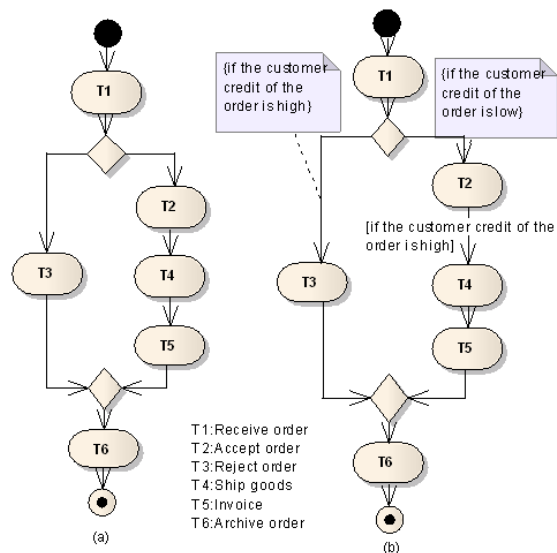


Figure 1: A customer order process example.

However, in real business context, process must deal with the data perspective. Fig. 1(b) shows process model with some data processing semantic. It is clear that improperly data processing semantic will cause the incorrectness of process.

Data-centric approach, as an extension of the traditional process-centric approach for workflow modelling, has been proposed over the past several years. The approach captures not only the control-flow but also the evolution of the key business entities's lifecycle in a workflow model (Bhattacharya et al. 2009). The data lifecycle specification describes the possible sequences of tasks that might occur to the business entity when it passes through the process.

Fig. 2 shows a data-centric workflow model for the customer order process. There are two key business entities: *order* and *shiplist*. The lifecycles of key business entities are described in the model. For example, the *order*'s lifecycle includes six stages: created, pending, accepted, completed, rejected, and archived.

It provides a possibility to verify the semantic correctness based on the data-centric workflow model. That is, to check whether the designed model meets some business requirements from business stakeholders. For instance, the typical business requirements of the customer order process are:

Requirement 1:

If the customer's credit of the order is high, the order is accepted.

Requirement 2:

If the customer's credit of the order is low, the order is rejected.

Requirement 3:

The goods shall be shipped after the order is paid.

In this paper, we restrict our previous WFCP-net, a Colored Petri Net with WF-net structure (Liu et al. 2002), to formally describe the key business entities

in a workflow model. Then, we use ASK-CTL logic (Cheng et al. 1996) to represent the business requirements. Finally, the model checking method is adopted to explore some of the business contraventions of data perspectives.

The remainder of this paper is organized as follows. Section 2 restricts the WFCP-net and uses the restricted WFCP-net to model the data-centric workflow. Section 3 focuses on analyzing the business contravention. Section 4 introduces the related work. Finally, conclusions and future work are presented in Section 5.

2 MODELING DATA-CENTRIC WORKFLOW

As a kind of workflow net, *WFCP-net* is proposed by D. Liu in (Liu et al. 2002). *WFCP-net* is a Colored Petri Net (*CP-net*) with *WF-net* structure. For a detailed introduction to *CP-net*, *WF-net* and *WFCP-net*, please refer to (Jensen 1997), (Aalst 1998) and (Liu et al. 2002) respectively. Here, we restrict the original *WFCP-net* in two facets: data type is described more clearly to express the sufficient data information. Re-defining the end place that there is only one unique end place.

Definition 1. (Restricted *WFCP-net*). A *CP-net* $\langle \Sigma, P, T, F, C, G, E, I \rangle$ is a *WFCP-net* if and only if:

(i) $\langle P, T, F \rangle$ is a *WF-net* with source place i and sink place o .

(ii) Σ : a finite set of non-empty types. $\Sigma = \{\Sigma_1, \dots, \Sigma_n\}$, with $\Sigma_i \cap \Sigma_j = \emptyset$ (we denote $i = \{1, \dots, n\}$ the ordered set of indexes); Σ_i is possibly partitioned in static subclasses: $\Sigma_i = \bigcup_{q=1}^{n_i} \Sigma_{i,q}$. Type is called *color set* in *CP-net*. A unique *color set* describes the structure of a business entity.

(iii) c is a color function. It is defined from P to Σ .

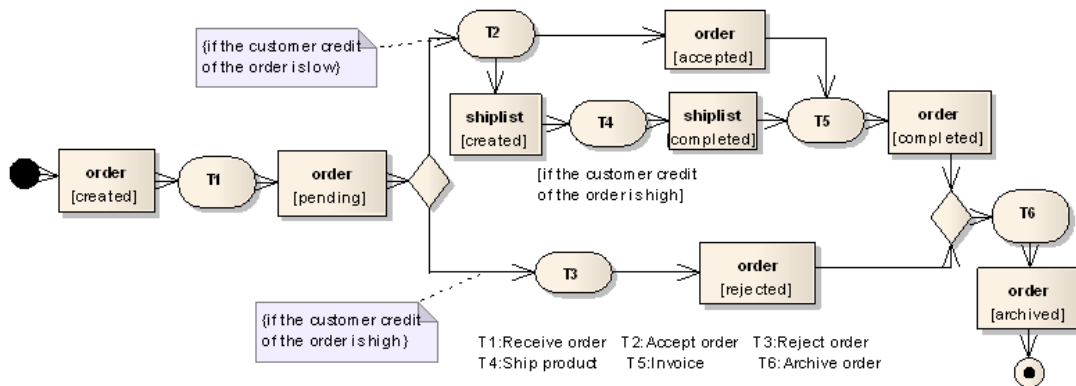


Figure 2: Data-centric workflow model of customer order process.

- (iv) G is a set of guard functions over Σ .
 (v) E is a set of arc expressions, which is defined from F into expressions, such that:

$$\forall f \in F: [Type(E(f)) = C(p(f)) \wedge Type(Var(E(f))) \subseteq \Sigma].$$

E maps each arc f into an expression which must be type of $C(p(f))$. This means that each evaluation of the arc expression must yield a data type over the *color set* that is attached to the corresponding place. And, the set of variable type in arc expression is a subset of Σ .

- (vi) The initialization function: $I = \begin{cases} \{e\}, e \in C(i), p = i \\ \emptyset, p \neq i \end{cases}$.

It is well known that in infinite domains (nets with infinite colors), many verification problems become undecidable (Aalst et al. 2008). For finite domains (finite colors), such nets can be *unfolded* to the ordinary WF-net. Then, verification problems become decidable (Aalst et al. 2008).

Based on the above restricted WFCP-net definition, we model the customer order process workflow shown in Fig. 3.

Here,

$$\Sigma = \{ORDER, SHIPLIST\}$$

ORDER is a *color set* which defines the data type of the business entity *order*.

$$ORDER = (orderid:I, customer_credit:CREDIT, good:I, currentstate:ORDERSTATE)$$

SHIPLIST is a *color set* which defines the data type of the business entity *shiplist*.

$$SHIPLIST = (shiplistid:I, customer_credit:CREDIT, good:I, currentstate:SHIPLISTSTATE)$$

The static subclasses of *ORDER*, *SHIPLIST* include *I*, *CREDIT*, *ORDERSTATE*, *SHIPLISTSTATE*:

$I = int$;

$CREDIT = \{with\ high|low\}$;

$ORDERSTATE = \{with\ Created|Pending|Rejected|Accepted|Completed|Archived\}$;

$SHIPLISTSTATE = \{with\ SLCreated|SLCompleted\}$;

I is integer type, $CREDIT$, $ORDERSTATE$ and $SHIPLISTSTATE$ are enumeration types.

$$G(t) = \begin{cases} Guard1(o1:ORDER), t = T2; \\ Guard2(o1:ORDER), t = T3; \\ Guard3(s1:SHIPLIST), t = T4; \\ True, otherwise. \end{cases}$$

$$E(f) = \begin{cases} Receiveorder(o1:ORDER), iff \in (T1, P2); \\ Acceptorder(o1:ORDER), iff \in (T2, P4); \\ Rejectorder(o1:ORDER), iff \in (T3, P3); \\ createsl(o1:ORDER), iff \in (dum2, P5); \\ \dots \end{cases}$$

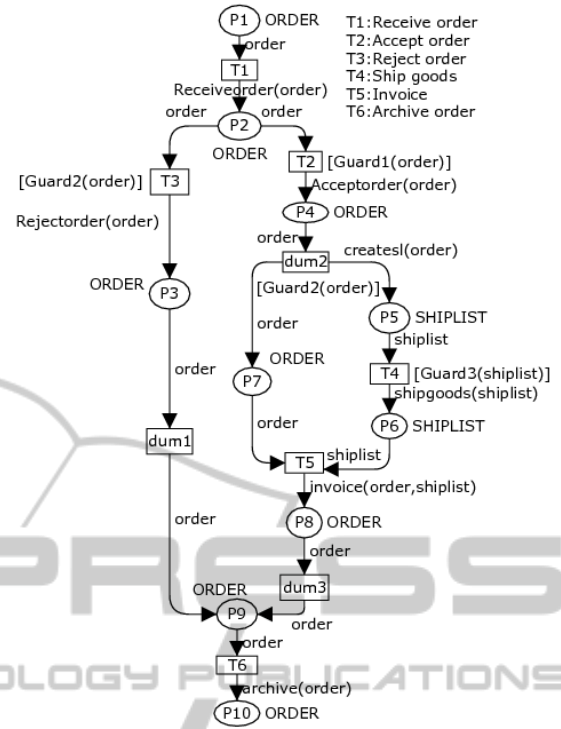


Figure 3: Data-centric model of customer order process.

3 ANALYZING DATA-CENTRIC WORKFLOW

The aim of this section is to check the business contravention in the workflow model with business entities.

In this section we firstly introduce a variant of Computation Tree Logic (CTL), ASK-CTL, proposed by (Cheng et al. 1996). Secondly, we formally describe the business requirements using ASK-CTL logic and rewrite ASK-CTL formula using *SML* (Standard ML) function. *SML* is a kind of formal programming language, which is put forward by (Harper 2005). Finally, the model checking method is used to analyze whether the workflow model matches the requirement.

3.1 ASK-CTL

In order to take into account both state (marking in state space) information and transition (edge in state space) information, ASK-CTL extends CTL. It has two categories of formulas: state and transition formulas respectively.

Definition 2. State formulas $\mathcal{A} ::= tt|\alpha|\neg\mathcal{A}|\mathcal{A}_1 \vee \mathcal{A}_2|\mathcal{A}_1 \wedge \mathcal{A}_2| < B > |EU(\mathcal{A}_1, \mathcal{A}_2)|AU(\mathcal{A}_1, \mathcal{A}_2)$, where:

\mathcal{A} is state formula, \mathcal{B} is transition formula.

tt is interpreted as the constant value *true*.

α is a function from marking set to Boolean set,

$\mathcal{M} \rightarrow IB$. α can be regard as atomic proposition.

\neg , \vee and \wedge are Boolean operators.

The $\langle \dots \rangle$ operator provides the possibility of changing between state and transition formulas. $\langle B \rangle$ means that we can find an immediate successor state from the current state and that B holds on the edge between the two states.

The standard temporal operator U (until) combined with the path quantifiers E and A (*exist* and *for-all* respectively).

The $EU(\mathcal{A}_1, \mathcal{A}_2)$ operator expresses the existence of a path from a given marking with the property that \mathcal{A}_1 holds until a marking is reached at \mathcal{A}_2 holds.

Dually, $AU(\mathcal{A}_1, \mathcal{A}_2)$ requires the property to hold along all paths from a given marking.

Definition 3. Transition formulas

$$\mathcal{B} ::= tt | \beta | \neg \mathcal{B} | \mathcal{B}_1 \vee \mathcal{B}_2 | \mathcal{B}_1 \wedge \mathcal{B}_2 | \langle A \rangle > | EU(\mathcal{B}_1, \mathcal{B}_2) | AU(\mathcal{B}_1, \mathcal{B}_2)$$

Where: β is a function from binding elements to Boolean set $BE \rightarrow IB$, and \mathcal{A} is a state formula.

Table 1 illustrates a part of SML syntactic sugar of state formulas supported by CPN tools.

Table 1: Syntactical sugar of state formulas.

ASK-CTL syntax	SML format Syntactical sugar
$\neg \mathcal{A}$	$NOT(\mathcal{A})$, \mathcal{A} is state formula
α	$NF(\langle message \rangle, \langle node function \rangle)$, is used to tell ASK-CTL that the proposition refers to node of state (eg. marking). Argument <i>node function</i> takes a state space node and returns a boolean. Argument <i>message</i> is used when a CTL formula evaluates to false.
$\mathcal{A}_1 \vee \mathcal{A}_2$	$OR(\mathcal{A}_1, \mathcal{A}_2)$, \mathcal{A}_1 and \mathcal{A}_2 are state formulas
$EU(\mathcal{A}_1, \mathcal{A}_2)$	$EXIST_UNTIL(\mathcal{A}_1, \mathcal{A}_2)$, used as a state formula, takes two arguments, \mathcal{A}_1 and \mathcal{A}_2 . The operator is true if there exists a path, starting from where we are now such that \mathcal{A}_1 is true for each state along the path until the last state on the path where \mathcal{A}_2 must hold.
$\neg EU(\neg \mathcal{A})$	$INV(\mathcal{A})$, as a state formula, is true if the argument \mathcal{A} is true for all reachable state, from the state we are at now. if, $\mathcal{A}: \mathcal{A}_1 \rightarrow \mathcal{A}_2$ is true. In ASK-CTL logic, $\mathcal{A}_1 \rightarrow \mathcal{A}_2$ denoted as $\neg \mathcal{A}_1 \vee \mathcal{A}_2$.

Here, we emphasize the SML function $eval_node \langle formula \rangle, \langle node \rangle$. It is a model checking function with two arguments: the CTL formula to be checked and a state from where the model checking should start.

3.2 Description of Business Entities Related Requirements

The ASK-CTL formal description of business requirement is the basic work for model checking. At first, we formally describe it as ASK-CTL formula. Subsequently, we rewrite the ASK-CTL formula into SML format. By this way, a concrete formalization of the business requirement is obtained. Now we deal with the business requirements proposed in the customer order process.

Requirement 1:

If the customer's credit of the order is high, the order is accepted.

Formula with ASK-CTL logic:

$$\neg EU(\neg(\neg \alpha_1 \vee \alpha_2))$$

The Atomic Proposition α_1

the customer's credit of the order is high

is interpreted through M :

Mark.example'P11 n=

$$I \{orderid=1, customer_credit=high, good=2, currentstate=created\}$$

It means to refer to the following token

$$I \{orderid=1, customer_credit=high, good=2, currentstate=created\}$$

on place $P1$.

The Atomic Proposition α_2

the order is accepted

is interpreted through M :

Mark.example'P4 1n=

$$I \{orderid=1, customer_credit=high, good=2, currentstate=Accepted\}$$

It means to refer to the following token

$$I \{orderid=1, customer_credit=high, good=2, currentstate=Accepted\}$$

on place $P4$.

Accordingly, the ASK-CTL formula can be rewritten with the SML format:

$$\neg EU(\neg(\vee(\neg \mathcal{A}_1, \mathcal{A}_2))) \Rightarrow INV(OR(NOT(\mathcal{A}_1), \mathcal{A}_2))$$

The concrete SML format description is:

```

fun Node1 n=(Mark.example'P1 1
n=I {orderid=1, customer_credit=high,
good=2, currentstate=Created});
fun Node2 n=(Mark.example'P4 1
n=I {orderid=1, customer_credit=high,
good=2, currentstate=Accepted});
val A1=NF("order is created",Node1);
val A2=NF("order is accepted",Node2);
val myASKCTLformula=INV(OR(NOT(A1), A2));
    
```

`eval_node myASKCTLformula InitNode;`

It is noted that the term *InitNode* means initial marking of the state space.

Analogously, requirement 2 and requirement 3 are also rewritten as SML format. Please see the left parts of Fig.4 (b) and (c) respectively.

3.3 Model Checking

Here, we adopt model checker function provided by CPN Tools to check whether the model meet the above business requirements.

Firstly, the occurrence graph of the CPN model and the strongly connected components graph of the CPN model are generated step by step.

Secondly, ASK-CTL module should be loaded in CPN Tools. The command is shown as follows.

```
use (ogpath^"ASKCTL/BitArray.sml");
use (ogpath^"ASKCTL/ASKCTL.sml");
open ASKCTL;
```

In the end, the Evaluate ML option in the simulation tool palette is clicked and the checking result is shown in the right parts of Fig. 4. The results of model checking indicate that this model does not satisfy the requirement 1, 2 and 3. As to requirement 1 and 2, there are errors related to

business entity *order*. As to requirement 3, there is inconsistency between key business entities *order* and *shiplist*.

4 RELATED WORK

A research area related to our work is formally modeling of data-centric workflow. The UML activity diagram is adopted popularly to describe the data-centric workflow (Nigam et al. 2003). However, the formal expression power of UML activity diagram is weak in some sort. Ref. Bhattacharya et.al 2007 proposes declarative language for formal modeling of data-centric workflow. Declarative language is good at logic reasoning rather than expression directly. There are well-developed formalisms for workflow modeling based on Petri nets. A typical example is WF-net proposed by Aalst (Aalst 1998).

However, most of them focus on control flow perspective. Ref. Liu et.al 2007 develops a computational model for artifact-centric operational models based on CP-nets.

<pre>fun Node1 n=(Mark.example'P1 1 n=1 {orderid=1,customer_credit=high, good=2,currentstate=Created}); fun Node2 n=(Mark.example'P4 1 n=1 {orderid=1,customer_credit=high, good=2,currentstate=Accepted}); val A1=NF("order is created",Node1); val A2=NF("order is accepted",Node2); val myASKCTLformula=INV(OR(NOT(A1), A2)); eval_node myASKCTLformula InitNode;</pre>	<pre>val Node1 = fn : Node -> bool val Node2 = fn : Node -> bool val A1 = NF ("order is created",fn) : A val A2 = NF ("order is rejected",fn) : A val myASKCTLformula = NOT (EXIST_UNTIL (TT, NOT (OR (NOT (NF ("order is created",fn)),NF ("order is rejected",fn)))))) : A val it = false : bool</pre>
--	--

(a) the checking result of requirement 1

<pre>fun Node1 n=(Mark.example'P1 1 n=1 {orderid=1,customer_credit=low, good=2,currentstate=Created}); fun Node2 n=(Mark.example'P3 1 n=1 {orderid=1,customer_credit=low, good=2,currentstate=Rejected}); val A1=NF("order is created",Node1); val A2=NF("order is rejected",Node2); val myASKCTLformula=INV(OR(NOT(A1), A2)); eval_node myASKCTLformula InitNode;</pre>	<pre>val Node1 = fn : Node -> bool val Node2 = fn : Node -> bool val A1 = NF ("order is created",fn) : A val A2 = NF ("order is rejected",fn) : A val myASKCTLformula = NOT (EXIST_UNTIL (TT, NOT (OR (NOT (NF ("order is created",fn)),NF ("order is rejected",fn)))))) : A val it = false : bool</pre>
--	--

(b) the checking result of requirement 2

<pre>fun Node1 n=(Mark.example'P4 1 n=1 {orderid=1,customer_credit=high, good=2,currentstate=Accepted}); fun Node2 n=(Mark.example'P5 1 n=1 {shiplistid=1,customer_credit=high, good=2,currentstate=SLCreated}); val A1=NF("order is accepted",Node1); val A2=NF("shiplist is created", Node2); val myASKCTLformula= EXIST_UNTIL(A1, A2); eval_node myASKCTLformula InitNode;</pre>	<pre>val Node1 = fn : Node -> bool val Node2 = fn : Node -> bool val A1 = NF ("order is accepted",fn) : A val A2 = NF ("shiplist is created",fn) : A val myASKCTLformula = EXIST_UNTIL (NF ("order is accepted",fn),NF ("shiplist is created",fn)) : A val it = false : bool</pre>
---	--

(c) the checking result of requirement 3

Figure 4: The results of model checking.

However, the computational model only summarizes few operational patterns to some extent and does not concern how to describe the static structure of the artifact in the model. A WFD net is proposed to extend WF-net with data elements in (Trcka 2009). However, it considers isolated data element only from local view rather than global view. Our work is different from theirs in that we integrate the data structure, data utility and control-flow into a unified model. Hence, data evolvement is toughly related to the control-flow. Accordingly, the model is suitable for formal analysis from data processing perspective.

Another related area is formal analysis of data-centric workflow. There are some researches focusing on the correctness analysis of artifact-centric system (Bhattacharya 2007 and Deutsch 2009). Above works only prove theoretically that the decidability of problems (e.g. reachability, complete execution and dead end) caused by infinite domain of data can be solved by adding some restrictions. Our work focuses on a global data view which pays attention to the evolvement of single business entity and the dependencies among business entities in business process. In addition, we highlight to verify the business contravention between business requirement of business stakeholder and the designed model.

5 CONCLUSIONS

In this paper, we propose a formal approach to model and analyze data-centric workflow using restricted WFCP-net. The approach supports modelling data-centric workflow integrating control flow and data flow and analyzing the correctness of workflow model with respect to the business requirement.

Our future works are as follows: (1) Investigate the expressive power of data structure for business entity in detail; (2) Consider more common solution strategy for infinite state problem caused by the infinite domain of data type.

ACKNOWLEDGEMENTS

This work is supported by the 973 Project of China (No. 2009CB320700, 2007CB310802), the 863 High-Tech Development Program of China (No. 2008AA042301, 2007AA040607, 2007AA040602), and the National Science Foundation (90718010, 61003099).

REFERENCES

- W. M. P. van der Aalst, K.M. van Hee, A. H. M. ter Hofstede, N.Sidorova, H. M. W. vwerbeek, M. Voorhoeve, and M. T. Wynn, "Soundness of Workflow Nets: Classification, Decidability, and Analysis," BPM Center Report BPM-08-02, BPMcenter.org, 2008.
- G. Booch, J. Rumbaugh, I. Jacobson, *The unified modeling language user guide*, Addison-Wesley, 2005.
- A. Nigam, N.S. Caswell, "Business artifacts: An approach to operational specification," *IBM Systems Journal*, 42(3), pp.428-445, 2003.
- K. Bhattacharya, R. Hull, and J. Su, "A data-centric design methodology for business processes," in *handbook of research on business process management*, 2009.
- W. M. P. van der Aalst, "The Application of Petri Nets to Workflow Management," *The Journal of Circuits, Systems and Computers*, 8(1), pp.21-66, 1998.
- K. Jensen, *Colored Petri Nets: basic concepts, analysis methods and practical use. Basic Concepts*, Vol. 1, Berlin: Springer Verlag, 1997.
- D. Liu, J. Wang, S.C.Chan, J. Sun, and L. Zhang, "Modeling workflow processes with Colored Petri nets," *Computers in Industry*, 49(3), pp. 267-281, 2002.
- A. Cheng, S. Christensen, and K.H. Mortensen, "Model Checking Coloured Petri Nets Exploiting Strongly Connected Components," In *Proceedings of International Workshop on Discrete Event Systems*, 1996, pages 169-177.
- R. Harper, *Programming in Standard ML*. Carnegie Mellon University, 2005.
- R. Liu, K. Bhattacharya, F.Y. Wu, "Modeling Business Contexture and Behavior Using Business Artifacts," In *Proceedings of CAiSE 2007*, pp.324-339.
- K. Bhattacharya, C.E. Gerede, R. Hull, R. Liu, and J. Su, "Towards formal analysis of artifact-centric business process models," In *Proceedings of International Conference on Business Process Management 2007*, LNCS, 2007, 288-304.
- A. Deutsch, R. Hull, F. Patrizi, and V. Vianu, "Automatic verification of data-centric business processes," In *Proceedings of the 12th international Conference on Database Theory*, ACM, New York, 2009, pp. 252-267.
- S. Christensen and K. H. Mortensen. *Design/CPN ASK-CTL Manual (1996)*. [Online], Available: http://www.daimi.au.dk/cpntools-help/_files/manual.pdf.
- K. Jensen, S. Christensen and L. M. Kristensen. *CPN Tools State Space Manual. (2006)*, [Online], Available: http://www.daimi.au.dk/cpntools-help/_files/manual.pdf.
- N. Trcka, W.M. P. van der Aalst, N. Sidorova, "Data-Flow Anti-patterns: Discovering Data-Flow Errors in Workflows," In *Proceedings of CAiSE 2009*, pp. 425-439, 2009.