

ELECTROCARDIOGRAM DERIVED RESPIRATION USING AN EVOLUTIONARY ALGORITHM

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Abstract: In this work we present a method to extract the respiratory signal from single lead ECG measurements, electrocardiogram derived respiration (EDR). The method is based on adaptive ECG modeling and respiratory signal estimation using an evolutionary algorithm fed with the model parameters. The evolutionary algorithm, which is allowed to employ a large constellation of functions, comes up with a set of relatively simple expressions (3-4 terms) describing valid relationships between ECG model parameters and the respiratory signal. In fact, the expressions mainly turn out to be linear combinations of the model parameters. Our preliminary experiments indicate that this method yields a robust EDR, and that this EDR correlates very well with a reference respiratory signal measurement. Correlation coefficients for the derived expressions lie around 0.95.

1 INTRODUCTION

Healthcare at Home is a field that will show significant growth over the next decades. This growth is mainly driven by economic issues and health related concerns (e.g. monitoring elderly people in their own homes). An expected consequence of this is an increase in the demand for telemedicine devices for remote monitoring of physiological parameters.

It is well known that a variety of physiological signals and parameters can be derived from ECG measurements, e.g. *Heart Rate Variability (HRV)*. Another derivation is the *respiratory signal*, on which we will focus in this work. Monitoring the respiratory signal can enable detection of sleep related symptoms such as central and mixed apnea, hypopnea, and tachypnea, see (Raymond et al., 2000).

Deriving as many physiological signals and parameters as possible from as few body sensors as possible is generally desirable. Primarily in order to minimize user discomfort but also in order to minimize cost and hardware complexity of the monitoring system.

Respiratory signals can be measured using dedicated devices but in order to keep the number of body sensors low it would be advantageous to simply derive the signal from ECG measurements using the existing ECG sensors.

Derivation of the respiratory pattern from the ECG

signal is possible when the ECG is directly available. For healthy subjects, the normal respiratory cycle modulates the heart rate, essentially determined as the RR-distance in successive PQRST complexes, and this modulation causes what is known as *Respiratory Sinus Arrhythmia (RSA)*, see (Clifford et al., 2006a) and (Grossman and Wientjes, 1986). Typically, inhalation leads to cardio-acceleration, i.e. a decrease in the RR rate of distance, and exhalation causes cardio-deceleration. Similarly, the morphology of the PQRST complex is also affected by the respiration, i.e. the wave amplitudes and the distances between the different waves oscillates synchronously with the respiration cycle.

In this work we will present a novel technique to extract the respiratory signal from single lead ECG measurements. Among other objectives, this technique aims at producing a robust RSA estimate as an input parameter to bio-feedback systems. For example, anxiety patients can make use of information about their respiration presented to them in real time in order to control the breathing. For patients suffering anxiety related disorders, controlled breathing can be an important tool in diminishing the psychological effects of sudden anxiety attacks.

2 ECG DERIVED RESPIRATION

It is well known that the respiration signal can be derived from the ECG signal. It is reported in the literature that respiration signal correlates to the changes in the heart rate as well as changes in the morphology of the PQRST complex. In the literature this is known as *ECG Derived Respiration (EDR)*. Many signal processing methods have been derived to calculate the EDR. For example in (Moody et al., 1985) the mapping from the ECG to the respiratory signal is given by the area of the normal QRS complex.

(Mazzanti et al., 2003) propose a method for EDR based on QRS areas in an 8 lead ECG measurement setup. They find some limitations in the validity of the EDR data, one important observation to mention is that the sampling frequency of the ECG signal has to be at least 500Hz, but still suggest the method as being effective, for example in telemetric monitoring.

Recently, (O'Brien and Heneghan, 2007) compared different algorithms for deriving the respiratory signal from single lead recorded ECGs compared to a reference respiratory signal measurement based on inductance plethysmography. One of the methods applies interpolation between R wave amplitudes in successive complexes. This technique is sensitive to baseline wander, however they find a correlation coefficient at 0.78 which indicates that the technique may be useful.

(Sobron et al., 2010) have also evaluated different methods for estimating EDR. Their comparative study included complex morphology such as the QRS area and amplitudes as well as heart rate variability. They suggest that combining EDR based on more of these ECG derivations gives the best respiratory frequency estimation.

This result probably does not come as a complete surprise, and hence leads us to take this combination method a step further, letting a evolutionary algorithm map a large set of parameters representing the ECG complexes into a respiratory signal.

3 EVOLUTIONARY ALGORITHM

Evolutionary algorithms have been known in the scientific community since the late 1960 early 1970, where John Holland introduced the basic idea. An evolutionary algorithm is a randomized population-based search technique, inspired by evolution principles from biology. Since its conception the paradigm has been widely used in engineering and computer science i.e. in computer programming, artificial intelligence and optimization.

A specialized implementation of evolutionary algorithms optimizes the symbolic regression problem. In this problem the search space consists of symbolic mathematical expressions, and the cost function for minimizing, is a chosen error metric. The error metric measures the residue between the estimate derived from the symbolic expression and the real data (Koza, 1992).

A symbolic regression solver has been implemented by (Schmidt and Lipson, 2009) in the application Eureka, which is freely available online on the web. In our work we used Eureka as a black box to model the mapping from the ECG to the respiration signal, in search for a more precise and robust estimate of the EDR mapping.

4 EXPERIMENTAL METHODS

The ECG signal and the respiratory signal are simultaneously recorded by a commercially available Zephyr Bioharness chest worn belt, (Zephyr Bioharness, nd). The respiratory signal is measured with a closed-source mechanical sensor. The sampling frequency for the respiratory signal is 17.86 Hz (T=56 ms). The ECG signal is sampled at 250 Hz. All signals are recorded with the software supplied with the Zephyr Bioharness. Some pre-processing of the ECG signal, i.e. amplification and filtering are done automatically by closed-source systems in the Zephyr device. All subsequent processing of the ECG and respiratory signals are carried out in MATLAB (MATLAB, 2010).

The ECG signal is often corrupted by small amounts of nonstationary 50 Hz interference. This noise is removed after signal acquisition with standard adaptive noise cancelling using a synthetic 50 Hz reference. Before modeling the ECG signal is segmented into heartbeats. The location of each heartbeat is found with an open source Pan-Tompkins algorithm (Clifford et al., 2006b). The 250 Hz sampling frequency of the ECG device is too low to ensure stable modeling of the QRS complex (Clifford et al., 2006a). This problem is counteracted by upsampling and interpolation of the ECG signal to 1500 Hz before modeling.

A typical heartbeat is shown in figure 1 along with the mathematical model discussed below. The QRS complex and the T wave are clearly visible. The P wave is normally barely visible above the noise floor on the recorded electrocardiograms. Therefore no attempt has been made of using information from the P wave in this work.

A large number of parameters can be extracted

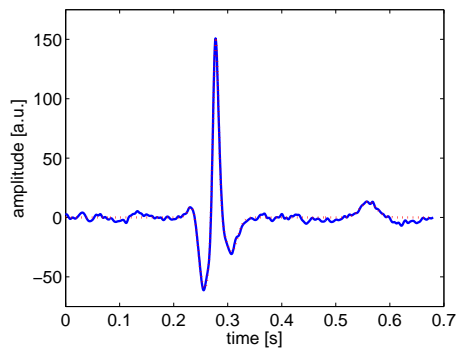


Figure 1: An example of a recorded heartbeat (blue) and the corresponding model (red).

from a single heartbeat i.e. amplitudes, areas and shapes of the individual waves in the heartbeat as well as the relative position between the waves. These parameters can be estimated directly from the recorded ECG signals. To minimize the influence of measurement noise each heartbeat is fitted to a model-heartbeat and the parameters are extracted from the mathematical model.

The mathematical model of the ECG signal consists of 3 Gaussians with positive amplitude and 2 Gaussians with negative amplitude. The two negative amplitude Gaussians model the Q and S wave. The positive amplitude Gaussians model the small peak preceding the Q wave and the R and T waves respectively. In related work (Clifford et al., 2006a) an asymmetric T wave is modeled with two positive Gaussian peaks. However, the T wave signal from the Zephyr Bioharness is quite symmetric and, except from a small baseline dip, well modeled by a single Gaussian. The parameters of the model are found by Levenberg-Marquardt fitting using MATLAB's Optimization Toolbox (MATLAB, 2010).

An example of a heartbeat and the corresponding model is shown in figure 1. The model captures the important features of the QRS complex and the T wave well and discards the major part of the noise. For each heartbeat a signal to noise ratio is measured with signal being defined as the energy in the model signal and noise being defined as the energy in the difference between the experimental signal and the model signal. The signal to noise ratio is normally found to be in the 70-130 range. If heartbeats with signal to noise ratios lower than 10 are found, they are labeled as noisy and discarded.

Each heartbeat is matched with the corresponding output from the respiratory sensor at the appropriate time. The maximum of the R wave is defined as the time zero for each heartbeat and the respiratory sample closest in time is chosen as the value of the respi-

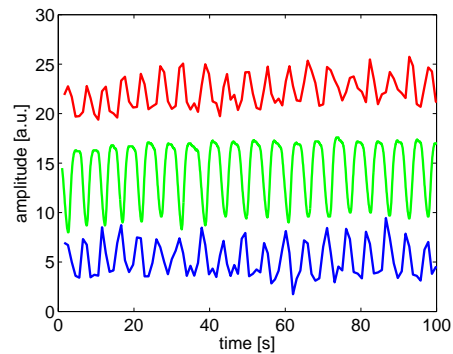


Figure 2: Examples of typical measurements. The data are vertically translated and scaled for clarity. The top curve (red) shows the the amplitude of the R wave, the middle curve (green) shows the respiratory signal, and the bottom curve (blue) shows the distance between the peaks of the R and S waves.

ratory signal. Due to the low sampling rate this procedure leads to small errors in the value of the respiratory signal when this signal is changing quickly. The maximum error is found to be smaller than 2%.

A number of parameters can be extracted from the mathematical model of the heartbeat. Many of these parameters will, however, be highly correlated. An example of this is shown in figure 2 where three parameters from a typical experiment are plotted; R wave amplitude, the distance between the maximum and minimum of the R and S waves and the respiratory signal. The R wave amplitude and R-S distance are seen to oscillate in anti-phase with the respiratory signal.

In this work where the goal is to let an evolutionary algorithm decide the optimum combination of ECG derived parameters for EDR the following parameters are extracted from each heartbeat: The amplitude, area and width, defined by full width at half maximum, for the Q, R, S and T waves together with the distances between the maxima of the Q and R waves, the R and S waves and the S and T waves as shown in table 1. Due to the low sampling rate and build-in filtering function of the Zephyr Bioharness no attempt have been made of extracting asymmetry parameters of the waves.

All the extracted parameters have non-zero mean values and numerically quite different values. All ECG derived parameters are put on equal footing before they are used in the evolutionary algorithm by subtracting their mean values and subsequently normalizing the maximum value to one. Similarly, the mean value is subtracted from the respiratory signal.

A number of possibilities exist for the fitness metric for the evolutionary algorithm i.e. mean absolute error, mean square error, correlation coefficient, me-

Table 1: List of model parameters derived from the ECG signal and the absolute value of the linear correlation with the respiratory signal.

Parameter	$ \rho $
Q_{amp}	0.43 ± 0.03
Q_{area}	0.31 ± 0.04
Q_{fwhm}	0.36 ± 0.01
R_{amp}	0.88 ± 0.01
R_{area}	0.83 ± 0.01
R_{fwhm}	0.17 ± 0.01
S_{amp}	0.21 ± 0.02
S_{area}	0.86 ± 0.01
S_{fwhm}	0.79 ± 0.01
T_{amp}	0.80 ± 0.01
T_{area}	0.81 ± 0.01
T_{fwhm}	0.08 ± 0.01
$QR_{distance}$	0.59 ± 0.01
$RS_{distance}$	0.67 ± 0.01
$ST_{distance}$	0.59 ± 0.02

dian error etc. In this work the optimization is done with respect to the correlation coefficient similar to the work of (O'Brien and Heneghan, 2007). The search for the optimized connection between the ECG derived parameters and the respiration signal can be restricted by only allowing the evolutionary algorithm to use a limited number of mathematical functions. In this work addition, subtraction, multiplication and division are used as building blocks unless otherwise specified. The evolutionary algorithm is run on a standard dual core 2 GHz pc and each search is typically run for 2-3 hours on data sets containing approximately 500 heartbeats.

The ECG and respiratory sensors in the Zephyr Bioharness are sensitive to movement artifacts, therefore, the subject under investigation is seated in a standard office chair, instructed to sit still, keep quiet and breathe steadily during the recording of the data. This procedure is found to be sufficient to minimize artifacts to below a visible threshold. This procedure also has the benefit of providing stationary data for the evolutionary algorithm to work with in this proof of concept investigation.

5 RESULTS

In a brute-force approach, all ECG derived parameters should be feed immediately to the evolutionary algorithm. It is, however, instructive to initially in-

clude only a limited amount of selected parameters and subsequently include further parameters. This approach allows for a comparison with different methods described in the literature and potentially a better understanding of the underlying mechanisms. In the following sections a number of increasingly complex optimization experiments are described.

5.1 Peak Amplitude

Under normal circumstances the peak amplitude of the ECG signal is given by the maximum of the R wave. This easily extracted parameter is known to be correlated with the respiratory signal and a number of authors have used this feature to form an EDR estimate, see e.g.(Clifford et al., 2006a) for a review. Figure 2 shows a similar correlation between the amplitude of the R wave and the respiratory signal in our experiments. Whether a higher degree of linear correlation can be found by some nonlinear function of the R wave amplitude isn't obvious. A nonlinear relation can originate in both the physical mechanisms connecting respiration and the heart beat morphology or in inherent nonlinearities in the sensors used to measure the ECG and respiratory signal.

For the particular dataset investigated the correlation coefficient between the normalized R wave amplitude, R_{amp} , and the respiratory signal is $|\rho| = 0.88 \pm 0.01$. The uncertainty is estimated by the difference of ρ for the two parts of the data set used for training and validation by the evolutionary algorithm.

When run with only addition, subtraction, multiplication and division as the mathematical building blocks for the evolutionary algorithm, the highest correlation found among the suggested solutions is $|\rho| = 0.89 \pm 0.01$ for the expression

$$EDR = -R_{amp} + \frac{1 + R_{amp}}{4 + 24R_{amp} + 108R_{amp}^2 + 216R_{amp}^3 + 162R_{amp}^4} \quad (1)$$

When the search space is increased to include constant values, power functions, exponential and logarithmic combinations and sine and cosine terms the solution with the highest correlation coefficient ($|\rho| = 0.90 \pm 0.01$) is given by the expression

$$EDR = \sin(0.335 - 2.22R_{amp}) \times \cos\left(\frac{-0.0477}{0.177 - 2.58R_{amp} + 5.91R_{amp}^2}\right) \quad (2)$$

The conclusion of this experiment is therefore that when only the R wave amplitude is available, no sim-

ple nonlinear function of this parameter gives a significantly better correlation with the respiratory signal than the R wave amplitude alone.

5.2 Peak-to-peak Amplitudes

A hardware based EDR technique has been presented by (Dobrev and Daskolov, 1998). The main idea is to find the maximum and minimum value of the ECG in each heartbeat, the rationale being that the maximum and minimum value can be found with standard electronic hardware. The two extremum values are subsequently squared, summed and smoothed by a low-pass filter to provide the EDR signal.

In the work by Dobrev and Daskalov the maximum and minimum of the ECG signal are found at the R wave and the S wave. However, the typical ECG signal recorded with the Zephyr Bioharness have its minimum at the Q wave and the optimization of a peak-to-peak based EDR signal should therefore done with the R and Q wave amplitudes.

When the evolutionary algorithm is run with R_{amp} and Q_{amp} as inputs the algorithm mainly evolves to a number of quite elongated expressions and one simple expression

$$EDR = R_{amp} + \frac{1}{3}Q_{amp} \quad (3)$$

With a correlation coefficient of $|\rho| = 0.90 \pm 0.01$ which is slightly better than the correlation between the respiratory signal and the R wave amplitude by itself. If the peak-to-peak amplitude, $R_{amp} + Q_{amp}$, is used directly to form the EDR estimate, the correlation diminishes to 0.75 ± 0.02 .

5.3 Peak Amplitudes

Previous work by (Raymond et al., 2000) have demonstrated that an EDR signal can be extracted from the T wave. The EDR estimate was derived from an averaged amplitude of the T wave. A natural extension of the peak-to-peak amplitude based EDR is a search where the input is the amplitude of all peaks present in the recorded signal i.e. the amplitude of the Q, R, S and T waves. The correlation coefficients between the different wave amplitudes and respiratory signal are shown in table 1.

The output from the evolutionary algorithm is again a number of primarily rather long expressions. However, one of the expressions is quite simple

$$EDR = Q_{amp} + 4R_{amp} + S_{amp} + T_{amp} \quad (4)$$

This EDR estimate has a correlation coefficient of 0.93 ± 0.01 and for this particular dataset we can con-

clude that the evolutionary algorithm devices an improved EDR estimate compared to the standard methods of both R wave and amplitude and peak to peak amplitude.

The improvement of the correlation if one of long expressions is used for the EDR estimate is insignificant and well within the uncertainty limits.

5.4 All Parameter Search

The final experiment is to feed all parameters derived from the ECG signal to the evolutionary algorithm. Due to the increased number of available parameters to combine, an improvement in the maximum correlation is anticipated for the longest expressions. The key issue is, however, whether a simple combination will improve the correlation coefficient.

The highest correlation coefficient is found to be $\rho = 0.97 \pm 0.01$ for an involved expression containing fractions and cubic terms. However, a few simple expressions also give high correlation coefficients i.e.

$$EDR = ST_{distance} - S_{area} - R_{area} \quad (5)$$

With $\rho = 0.95 \pm 0.01$ and

$$EDR = ST_{distance} + Q_{area} - R_{amp} - 2R_{area} \quad (6)$$

With $\rho = 0.96 \pm 0.01$.

These results shows that for the specific dataset used, a high correlation between a simple combination of ECG derived parameters and the respiratory signal can indeed be found by a computerized search. Both EDR estimates make use of $ST_{distance}$ and R_{area} suggesting that these two parameters are potentially robust EDR estimators.

5.5 Nonstationary Breathing

A first test of the robustness of the EDR estimate has been performed by recording a time series of ECG and respiratory signals containing periods of bated respiration resembling sleep apnea. An example of this is shown in figure 3.

The EDR estimate is calculated with Eq (6). From the figure it is evident that the EDR estimate captures the bated respiration. In particular, the stopped respiration and restart of respiration is immediately captured.

6 CONCLUSIONS

The results and their applicability are currently limited by two major factors. First of all, the study has not been carried out on a pool of patients. In order to

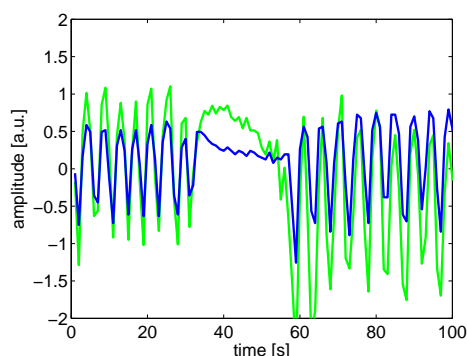


Figure 3: The graph shows the respiratory signal (blue) and the EDR signal (green) for a subset of a timeseries containing periods of deep breathing and periods with bated respiration.

demonstrate the robustness of this EDR approach the study must be extended to a cohort with different gender, age, etc. in different physical situations. Second, the signal recording devices were chosen because of availability rather than optimum superior signal quality. It is anticipated that better results could be obtained by using an ECG device with a higher sampling rate and full control of the amplification and filtering of the signal. In particular, the asymmetry of the T wave is suspiciously absent on our data generated with the Zephyr Bioharness. Likewise, no information from the P wave has been included.

Similarly, a more precise respiration sensor with higher sampling rate and larger immunity to movement artifacts would provide higher quality data to feed into the evolutionary algorithm.

The goal of this work has been to investigate the feasibility of optimizing EDR with an evolutionary algorithm and provide a proof of concept. More research remains to be done, but we have found that it is indeed possible to optimize EDR with an evolutionary algorithm and we believe that evolutionary algorithms will provide a fruitful tool for further studies in EDR and other biomedical signal processing problems.

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