

Modelling Excitement as a Reaction to a Virtual 3D Face

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Abstract: This paper introduces a comparison of a linear and nonlinear one step predictive models that were used to describe the relationship between human emotional signal – excitement – as a reaction to a virtual 3D face feature – distance between eyes. An input-output model building method is proposed that allows building a stable model with the least output prediction error. Validation was performed using the recorded signals of six volunteers and the following measures: prediction error standard deviation, relative prediction error standard deviation, and average absolute relative prediction error. Validation results of the models showed that both models predict excitement signal in relatively high prediction accuracy.

1 INTRODUCTION

Lots of systems and classification methods are used for emotion recognition problem, but not so many systems and methods are used for emotion control in virtual environment. For this purpose plenty of bio-signals are used for human state monitoring. We use EEG-based signals because of their reliability and quick response (Sourina and Liu, 2011; Hondrou and Caridakis, 2012).

We have investigated linear input-output structure models for exploring dependencies between virtual 3D face features and human reaction to them in Vidugirienė et al. (2013) and Vaškevičius et al. (2014). Four reaction signals were used: excitement, meditation, frustration, and engagement/boredom. It was shown that features of a virtual face have the largest influence to human excitement signal from the previously mentioned four human reaction signals (Vaškevičius et al., 2013).

In this investigation we compare a linear and one type nonlinear input-output models to describe the dependencies between human reaction – excitement signal – to a virtual 3D face feature – distance-between-eyes.

2 OBSERVATIONS AND DATA

A virtual 3D face with changing distance between eyes was used for input as stimulus (shown in a monitor) and EEG-based pre-processed excitement

signal of a volunteer was measured as output (Figure 1). The output signals were recorded with Emotiv Epoc device that records EEG inputs from 14 channels (according to international 10-20 locations): AF3, F7, F3, FC5, T7, P7, O1, O2, P8, T8, FC6, F4, F8, AF4 (Emotiv Epoc specifications). A dynamic stimulus was formed from a changing woman face. One 3D face created with Autodesk MAYA was used as a “neutral” one (Figure 1, left). Other 3D faces were formed by changing distance-between-eyes in an extreme manner (Figure 2).

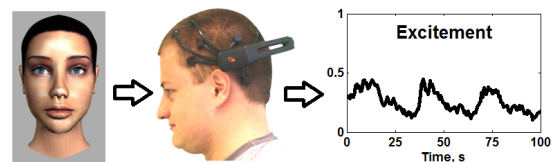


Figure 1: Input-Output scheme for the experiments.



Figure 2: A 3D virtual face with the smallest (left), normal (middle) and the largest (right) distance-between-eyes.

The transitions between normal and extreme

stages were programmed.

Experiment plan for input is shown in Figure 3. At first “neutral” face (Figure 2, middle) was shown for 5 s, then the distance-between-eyes was increased continuously and in 10 s the largest distance between eyes (Figure 2, right) was reached, then 5 s of steady face was shown and after that the face came back to “normal” in 10 s. Then “normal” face was shown for 5 s, followed by 10 s long continuous change to the face with the smallest distance between eyes (Figure 2, left), again 5 s of steady face was shown and in the next 10 s the face came back to “normal”. Then everything was repeated from the beginning using 3 s time intervals for steady face and 5 s for continuous change. “Neutral” face has 0 value, largest distance-between-eyes corresponds to value 3 and smallest distance-between-eyes corresponds to value -3.

Values of the output signal – excitement – vary from 0 to 1. If excitement is low, the value is close to 0 and if it is high, the value is close to 1. The signals were recorded with the sampling period of $T_0=0.5$ s.

Six volunteers (three females and three males) were tested. Their excitement signals are shown in Figures 4-5.

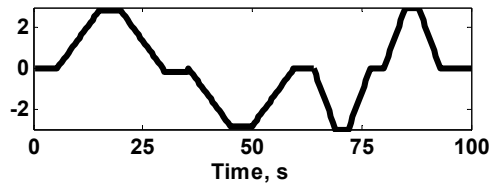


Figure 3: Input signal: experiment plan.

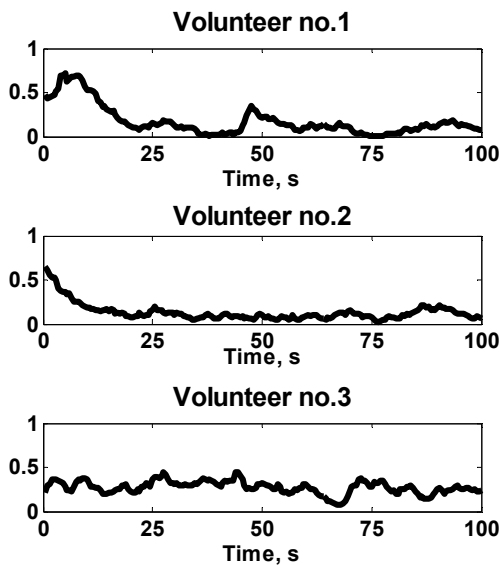


Figure 4: Excitement signal, volunteers no. 1-3 (females).

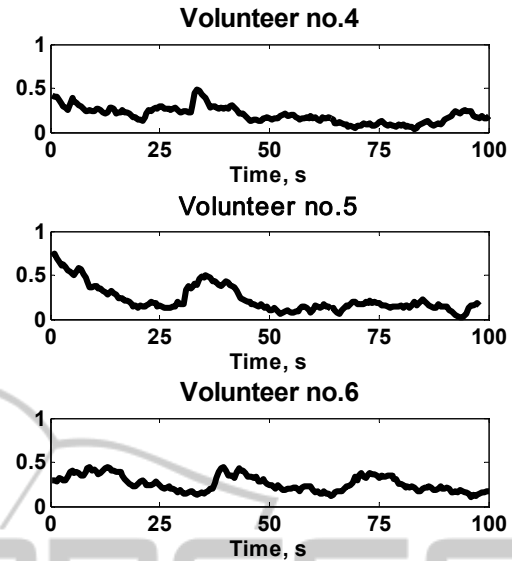


Figure 5: Excitement signal, volunteers no. 4-5 (males).

Each volunteer was watching one animated scene of approximately 100 s, and EEG-based signals were measured and recorded simultaneously.

3 BUILDING OF MATHEMATICAL MODELS

Dependency between virtual 3D face feature (distance-between-eyes) and human excitement is described by input-output structure linear and nonlinear models (Kaminskas, 1982) in (1) and (2) correspondingly:

$$A(z^{-1})y_t = \theta_0 + B(z^{-1})x_t + \varepsilon_t \quad (1)$$

and

$$A(z^{-1})y_t = \theta_0 + B(z^{-1})|x_t| + \varepsilon_t \quad (2)$$

where

$$B(z^{-1}) = \sum_{j=0}^m b_j z^{-j}, \quad (3)$$

$$A(z^{-1}) = 1 + \sum_{i=1}^n a_i z^{-i}$$

y_t is an output (excitement), x_t is an input (distance-between-eyes) signal respectively expressed as

$$y_t = y(tT_0), \quad x_t = x(tT_0) \quad (4)$$

with sampling period T_0 , θ_0 is a constant value, ε_t corresponds to noise signal, and z^{-1} is the backward-

shift operator ($z^{-1}x_t = x_{t-1}$). A sign $| \cdot |$ denotes absolute value.

These type of models were chosen to examine if a volunteer reacts to the changes of a 3D face (increase or decrease of distance-between-eyes) directly (model 1) or he/she reacts to the absolute values of the changes (model 2).

Parameters (coefficients of the polynomials (3)), orders (degrees m and n of the polynomials (3)) and constant θ_0 of the models (1) or (2) are unknown. They have to be estimated according to the observations obtained during the experiments with the volunteers.

Eqs. (1) and (2) can be expressed in the following forms:

$$y_t = \theta_0 + \sum_{j=0}^m b_j x_{t-j} - \sum_{i=1}^n a_i y_{t-i} + \varepsilon_t, \quad (5)$$

$$y_t = \theta_0 + \sum_{j=0}^m b_j |x_{t-j}| - \sum_{i=1}^n a_i y_{t-i} + \varepsilon_t, \quad (6)$$

It is not difficult to see that eqs. (5) and (6) can be expressed as the linear regression equations:

$$y_t = \beta_t^T c + \varepsilon_t \quad (7)$$

where

$$\beta_t^T = [1, x_t, x_{t-1}, \dots, x_{t-m}, -y_{t-1}, \dots, -y_{t-n}] \quad (8)$$

for model (1),

$$\beta_t^T = [1, |x_t|, |x_{t-1}|, \dots, |x_{t-m}|, -y_{t-1}, \dots, -y_{t-n}] \quad (9)$$

for model (2), and

$$c^T = [\theta_0, b_0, b_1, \dots, b_m, a_1, a_2, \dots, a_n], \quad (10)$$

for both models, and T is a vector transpose sign.

For the estimation of unknown parameter vector c we use a method of least squares (Kaminskas, 1982):

$$\hat{c} = Q^{-1}q, \quad (11)$$

where Q and q are expressed as follows

$$Q = \sum_{t=1}^M \beta_t \beta_t^T, \quad (12)$$

$$q = \sum_{\tau=1}^M y_\tau \beta_\tau, \quad (13)$$

and M is a number of observation values that are used to build a model.

After calculating the estimates of model parameters, model's stability condition is verified (Kaminskas, 1982). It means that the roots

$$z_i^A: \hat{A}_M(z) = 0, i = 1, 2, \dots, n \quad (14)$$

of the following polynomial

$$\hat{A}_M(z) = z^n \hat{A}_M(z^{-1}) = z^n + \sum_{i=1}^n \hat{a}_i z^{n-i} \quad (15)$$

have to be in the unit disk

$$|z_i^A| \leq 1. \quad (16)$$

Estimates of the model orders – \hat{m} and \hat{n} – are defined from the following conditions (Kaminskas, 1982):

$$\hat{n}: \left| \frac{\sigma_\varepsilon[m, n+1] - \sigma_\varepsilon[m, n]}{\sigma_\varepsilon[m, n]} \right| \leq \delta, \quad (17)$$

$n = 1, 2, \dots$

$$\hat{m}: \left| \frac{\sigma_\varepsilon[m+1, n] - \sigma_\varepsilon[m, n]}{\sigma_\varepsilon[m, n]} \right| \leq \delta, \quad (18)$$

$m = 0, 1, \dots, n$

where

$$\sigma_\varepsilon[m, n] = \sqrt{\frac{1}{N} \sum_{t=1}^N \hat{\varepsilon}_t^2[m, n]} \quad (19)$$

is one step output prediction error standard deviation,

$$\hat{\varepsilon}_t[m, n] = y_t - \hat{y}_{t|t-1}[m, n] \quad (20)$$

is one step output prediction error,

$$\hat{y}_{t|t-1} = \hat{\theta}_0 + z[1 - \hat{A}_M(z^{-1})]y_{t-1} + \hat{B}_M(z^{-1})x_t \quad (21)$$

is one step forward output prediction in the case of model (1) and

$$\hat{y}_{t|t-1} = \hat{\theta}_0 + z[1 - \hat{A}_M(z^{-1})]y_{t-1} + \hat{B}_M(z^{-1})|x_t| \quad (22)$$

in the case of model (2) (Kaminskas, 2007), z is the forward-shift operator ($zy_t = y_{t+1}$), and $\delta > 0$ is a chosen constant value. Usually in the practice of identification $\delta \in [0,001 \div 0,01]$ what corresponds to a relative variation of prediction error standard deviation from 0,1% to 1%.

This way stable input-output models are built that ensure the best one step output signal prediction.

4 VALIDATION OF PREDICTIVE MODELS

Validation of the models (1) and (2) was performed for each of six volunteers (three female and three male).

Figs. 6-9 demonstrate prediction error standard deviations for an input-output pair when $n=1, 2$ and $m=0, 1$, for one male (volunteer no.4) and one female (volunteer no.2) using model (1) and model (2).

Each model is selected from four possible models (when $n=1, 2; m=0, 1$) using the rules (17) and (18).

The analysis of two volunteers' data showed that relations between distance-between-eyes input and excitement output signal can be modelled when model order is $\hat{m} = 0$, and $\hat{n} = 1$.

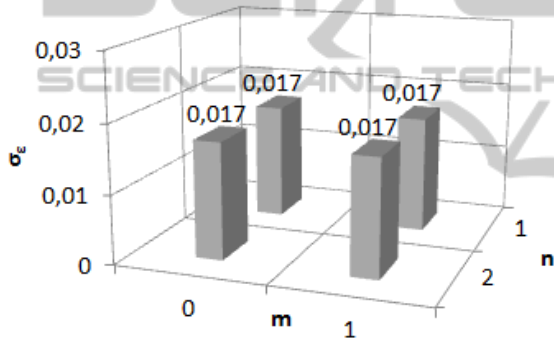


Figure 6: Prediction error standard deviations with different model (1) orders for a volunteer no. 2 (female).

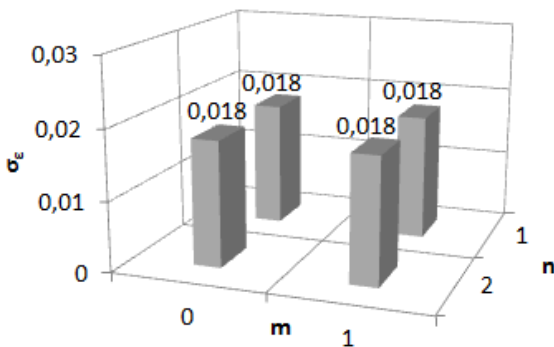


Figure 7: Prediction error standard deviations with different model (2) orders for a volunteer no. 2 (female).

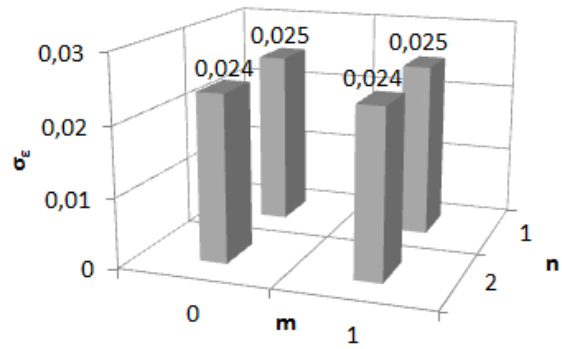


Figure 8: Prediction error standard deviations with different model (1) orders for a volunteer no. 4 (male).

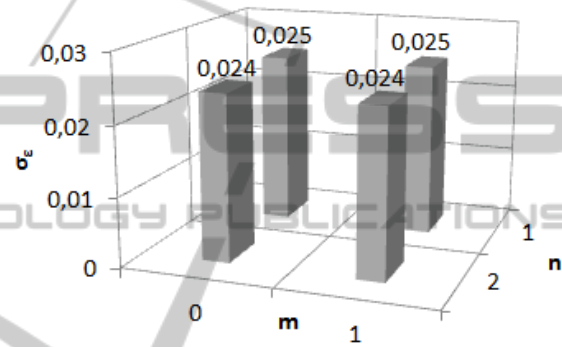


Figure 9: Prediction error standard deviations with different model (2) orders for a volunteer no. 4 (male).

The predicted output signals of every model have the following expressions (Kaminskas, 1982)

$$\begin{aligned} \hat{y}_{t+1|t} &= \hat{\theta}_0 + z[1 - \hat{A}(z^{-1})]y_t + \\ &+ \hat{B}(z^{-1})x_{t+1} = \\ &= \hat{\theta}_0 - \hat{a}_1 y_t + \hat{b}_0 x_{t+1} \end{aligned} \quad (23)$$

in the case of model (1) and

$$\begin{aligned} \hat{y}_{t+1|t} &= \hat{\theta}_0 + z[1 - \hat{A}(z^{-1})]y_t + \\ &+ \hat{B}(z^{-1})|x_{t+1}| = \\ &= \hat{\theta}_0 - \hat{a}_1 y_t + \hat{b}_0 |x_{t+1}| \end{aligned} \quad (24)$$

in the case of model (2).

Prediction accuracies were evaluated using the following measures:

- prediction error standard deviation

$$\sigma_\varepsilon = \sqrt{\frac{1}{N} \sum_{t=0}^{N-1} (y_{t+1} - \hat{y}_{t+1|t})^2}, \quad (25)$$

- relative prediction error standard deviation

$$\tilde{\sigma}_\varepsilon = \sqrt{\frac{1}{N} \sum_{t=0}^{N-1} \left(\frac{y_{t+1} - \hat{y}_{t+1|t}}{y_{t+1}} \right)^2} * 100\%, \quad (26)$$

– and average absolute relative prediction error

$$|\bar{\varepsilon}| = \frac{1}{N} \sum_{t=0}^{N-1} \left| \frac{y_{t+1} - \hat{y}_{t+1|t}}{y_{t+1}} \right| * 100\%. \quad (27)$$

Predictions were performed using the observation data that were used to build a model (M=124, in (12) and (13)) and the additional ones that were not used to build a model (N=200, in (25)-(27)). Prediction accuracies and parameters of the models are provided in Table 1 and Table 2 for female and male volunteers respectively.

Table 1: Prediction errors and model parameter estimates for the volunteers no. 1-3 (females).

Volunteer no.	Model	σ_ε	$\tilde{\sigma}_{\varepsilon, \%}$	$ \bar{\varepsilon} , \%$	b_0	a_1	θ_0
1	1	0.0246	4.46	6.59	-0.0014	-0.9856	0.0006
	2	0.0246	4.47	6.57	-0.0018	-0.9822	0.0036
2	1	0.0174	3.51	5.63	0.0007	-0.9097	0.0085
	2	0.0176	3.55	5.69	-0.0006	-0.9099	0.0093
3	1	0.0271	5.23	7.94	-0.0002	-0.8676	0.0399
	2	0.0275	5.32	8.13	-0.0029	-0.8574	0.0469

Figures 10-15 show prediction results when using linear model (1) for all six volunteers. Thin solid line denotes an observed signal and thick dotted line denotes predicted signal.

Table 2: Prediction errors and model parameter estimates for the volunteers no. 4-6 (males).

Volunteer no.	Model	σ_ε	$\tilde{\sigma}_{\varepsilon, \%}$	$ \bar{\varepsilon} , \%$	b_0	a_1	θ_0
4	1	0.0248	4.64	7.21	0.0012	-0.9139	0.0189
	2	0.0253	4.75	7.43	-0.0042	-0.8898	0.0303
5	1	0.0258	5.12	8.26	0.0005	-0.9594	0.0066
	2	0.0260	5.19	8.68	-0.0088	-0.9362	0.0251
6	1	0.0245	4.80	7.94	-0.0001	-0.9674	0.0079
	2	0.0249	4.91	8.09	-0.0040	-0.9869	0.0079

Vertical thin dotted line denotes M position as model parameters were estimated in the interval from 0 to M (that is equal to 124). As the signal was measured with the sampling period of $T_0=0.5$ s, M value corresponds to 62 s.

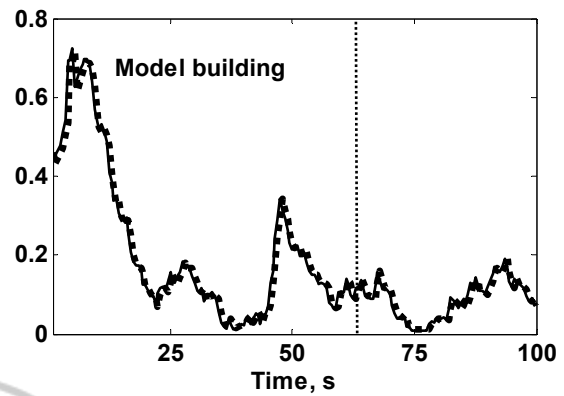


Figure 10: Prediction error standard deviations for volunteer no. 1 (female). Thin solid line denotes a real observed signal and thick dotted line denotes predicted signal. Vertical thin dotted line denotes M position.

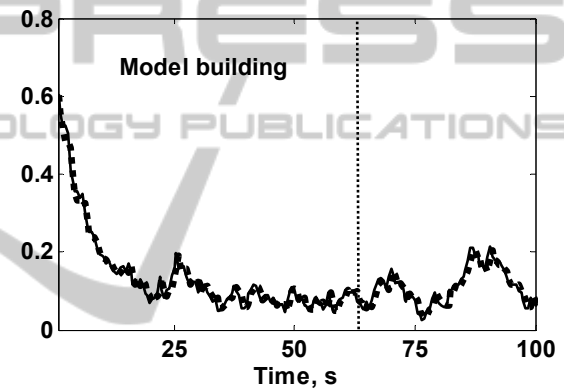


Figure 11: Prediction error standard deviations for volunteer no. 2 (female). Thin solid line denotes a real observed signal and thick dotted line denotes predicted signal. Vertical thin dotted line denotes M position.

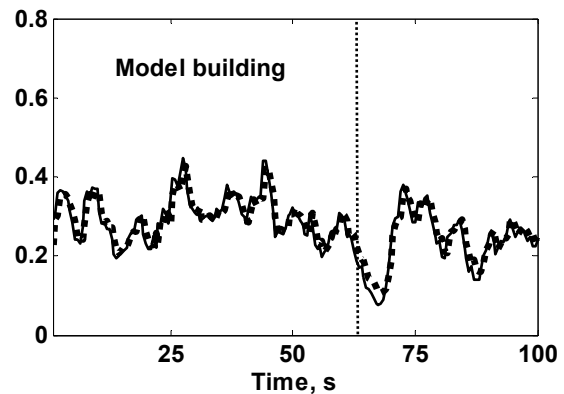


Figure 12: Prediction error standard deviations for volunteer no. 3 (female). Thin solid line denotes a real observed signal and thick dotted line denotes predicted signal. Vertical thin dotted line denotes M position.

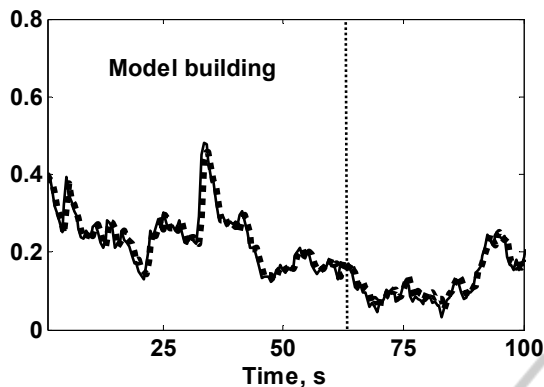


Figure 13: Prediction error standard deviations for volunteer no. 4 (male). Thin solid line denotes a real observed signal and thick dotted line denotes predicted signal. Vertical thin dotted line denotes M position.

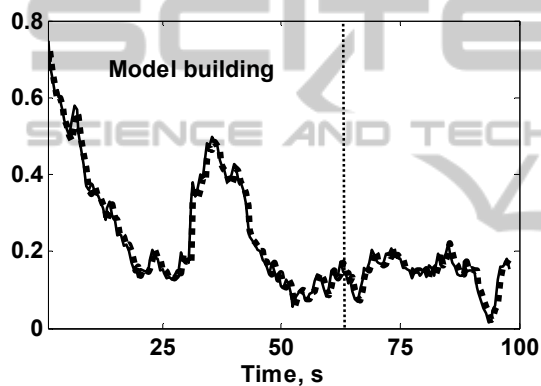


Figure 14: Prediction error standard deviations for volunteer no. 5 (male). Thin solid line denotes a real observed signal and thick dotted line denotes predicted signal. Vertical thin dotted line denotes M position.

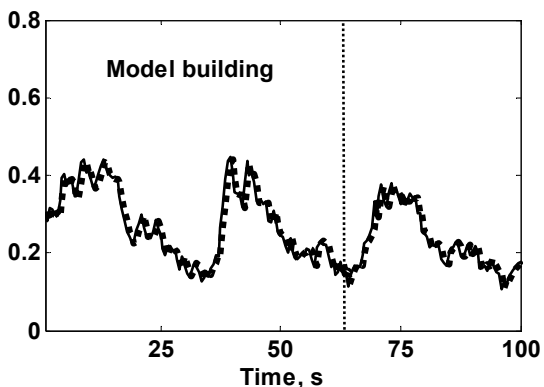


Figure 15: Prediction error standard deviations for volunteer no. 6 (male). Thin solid line denotes a real observed signal and thick dotted line denotes predicted signal. Vertical thin dotted line denotes M position.

5 CONCLUSIONS

Two alternative predictive models – linear and nonlinear – were proposed to describe the dependencies between 3D face feature (distance-between-eyes) and excitement. The first model describes the reaction of a volunteer to the direct changes of a 3D face (increase or decrease of distance-between-eyes). The second describes the reaction of a volunteer to the absolute values of the changes of a 3D face.

A method for building input-output models was proposed that allows building stable models for the predictions of excitement signals with the least prediction error.

Validation of the models showed that each volunteer has an individual reaction to the given stimuli, and the reactions can be described using first order ($n=1$, $m=0$) models. The absolute relative predictions errors for the excitement signals are between 5.5 % and 8.5 % in both model cases.

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