

Experimental Evaluation of a Modified Obstacle Based Potential Field Algorithm for an Off-road Mobile Robot

Rickard Nyberg, George Nikolakopoulos and Dariusz Kominiak

*Control Engineering Group, Department of Computer Science, Electrical and Space Engineering,
Luleå University of Technology, Luleå, Sweden*

Keywords: Off Road Mobile Robot, Artificial Potential Fields, Visual Feedback, Depth Image, Obstacle Detection.

Abstract: This article presents an experimental evaluation of a modified obstacle based artificial potential field algorithm for an off-road mobile robot. The first contribution of the presented approach concerns the transformation of the artificial potential field method for the guidance of the vehicle and obstacle avoidance, in order to make it suitable for utilising a visual feedback. The visual feedback is relying on a depth image, provided by the low cost kinect sensor. The second contribution concerns the proposal of a novel scheme for the identification and perception of obstacles. Based on the proposed methodology, the vehicle is capable of categorising the obstacles based on their height in order to alter the calculated forces, for enabling a cognitive decision regarding their avoidance or the driving over them, by utilising the robot's off road capabilities. The proposed scheme is highly suggested for off road robots, since in the normal cases, the existence of small rocks, branches, etc. can be accidentally identified as obstacles that could make the robot to avoid them or block its further movement. The performance of the proposed modified potential field algorithm has been experimentally applied and evaluated in multiple robotic exploration scenarios, where from the obtained results the efficiency and the advantages of such a modified scheme have been depicted.

1 INTRODUCTION

Autonomous off-road vehicles have a vast variety of potential applications in a lot of different domains such as exploration, search and rescue, environmental management and forest machinery. Transforming an off-road vehicle into fully autonomous to reliably navigate and avoid obstacles, still remains a major challenge in robotics. To complete such a vision, a mobile robot system needs to be equipped with reliable sensors to percept the environment, build environmental maps and planning safe paths through the cruising terrain, while it would be ideal if the onboard sensors and perception systems would be able to handle very rugged and uneven terrains. An ability which comes in contrast to the more conventional robotic systems, being operated in simpler and more structured environments.

One of the main problems in off-road vehicle navigation is obstacle detection and avoidance, mainly due to the wide diversity of appearance of potential obstacles, different shapes and varying height that make this problem very challenging. In the related scientific literature, several approaches have been pro-

posed to address these problems. In some cases, the focus have been more towards designing special off-road robotic platforms, instead of focusing on autonomous navigation. Such an example is the rover Shrimp presented in (Siegwart et al., 2002), which is a six-wheeled rover with a special spring suspension to guarantee optimal ground contact of all wheels at any time. Another example is the HELIOS-VI (Hirose et al., 2001), a terrain adaptive crawler. Many efforts have tried to solve the problem relying on several sensors, including laser range finder and radar (Matthies et al., 1995), while other approaches include the utilization of stereo vision technique (Broggi et al., 2005). Active sensors make the problem considerably easier, but there are always a trade off in cost and power consumption. In the area of image processing for robotic guidance, there has been a tremendous growth in the latest years. Some indicative research efforts have been reported in (Zhang et al., 2010), where a visual SLAM algorithm has been introduced that utilizes stereo vision to estimate a 3D map representation of the environment. The research in (Valavanis et al., 2000) presents a method for vision guided navigation for non-holonomic robots, by using only

quantities that can be directly measured in the image and thus bypassing the pose estimation phase. Other research groups used image processing to control a robot to stay on a desired path (Schlengel et al., 1997). Image processing has also been used for exploration purposes, where the robot is driven towards areas that are informative for navigation by utilizing a monocular pan-tilt camera.

In the area of obstacle avoidance and guidance in exploration robotic tasks, one of the most popular and experimentally applied method is the one of the Artificial Potential Fields (APF) (Khatib, 1986), while a lot of modifications and improvements can be located in (Guo et al., 2013) and (Vadakkepat et al., 2000). The main contribution of this article is dual. First the transformation of the APF method to make it suitable for utilizing visual feedback will be presented. Until now, it should be highlighted that the majority of the APF implementations utilize sonar sensors or infra red sensors to measure only the distance to obstacles. With visual feedback and a camera as a sensor it is possible to retrieve more information about the environment and the obstacles, while increasing the sensing robustness and the overall flexibility of the robotic platform. Secondly, a novel scheme for identification and perception of obstacles, which not only considers the distance to the obstacles but also their height, will be presented. The cognitive categorisation of obstacles will feed the APF scheme, while directly affecting the guidance of the vehicle in order to overcome small obstacles.

This article is structured as it follows. Section ?? presents the basic theory of the APF method and establishes the image processing algorithm for identifying and measuring obstacles based on depth images. In Section 3, the modification of the APF based on the kinematic model of the robot and on the identified height of obstacles will be presented. The overall experimental setup and an overview of the suggested overall modified APF will be presented in Section 4. The evaluation of the proposed methodology is being performed by multiple experimental scenarios, presented in Section 5, while the conclusions are drawn in Section 6.

2 OBSTACLE DETECTION AND AVOIDANCE

2.1 Artificial Potential Fields

The basic principle behind the APF methodology is that obstacles that should be avoided, are surrounded

by repulsive potentials, while the goal point is surrounded by an attractive potential. As a result, the robot at the q -point will navigate in the direction of the resulting force U , computed by summing the set of all the repulsive forces U_{rep} , with the set of all the attractive forces U_{att} as:

$$U(q) = U_{att}(q) + U_{rep}(q)$$

For computing the repulsive and attractive potentials, $U_{att}(q)$ and $U_{rep}(q)$, multiple methods can be found in the related literature.

One popular methodology, which is the one adopted in this research, is to measure a scaled distance to the goal, $U(q) = \zeta d(q, q_{goal})$ with ζ the scaling factor, utilized to scale the effect of the attractive potential, and thus the attractive force can then be expressed as (Choset et al., 2005):

$$U_{att} = \frac{1}{2} \zeta d^2(q, q_{goal}),$$

while the gradient becomes:

$$\nabla U_{att}(q) = \nabla \left(\frac{1}{2} \zeta d^2(q, q_{goal}) \right) = \zeta d(q - q_{goal})$$

and thus in this case, if the robot starts at any point, other than the goal, and by following the negative gradient, it will follow a path to the goal. A combination of the quadratic and conic potential is utilized to escape the problem, which the quadratic potential can generate, to high velocities close to the goal, as follows (Choset et al., 2005):

$$U_{att}(q) = \begin{cases} \frac{1}{2} \zeta d^2(q, q_{goal}), & d(q, q_{goal}) \leq d_{goal}^* \\ d_{goal}^* \zeta d(q, q_{goal}) - \frac{1}{2} \zeta (d_{goal}^*)^2, & d(q, q_{goal}) > d_{goal}^* \end{cases}$$

where the gradient is defined by:

$$\nabla U_{att}(q) = \begin{cases} \zeta d(q - q_{goal}), & d(q, q_{goal}) \leq d_{goal}^* \\ \frac{d_{goal}^* \zeta d(q - q_{goal})}{d(q, q_{goal})}, & d(q, q_{goal}) > d_{goal}^* \end{cases}$$

with d_{goal}^* the threshold distance from the goal, where the algorithm switches between conic and quadratic potentials.

The next step is to calculate the repulsive potential. The repulsive potential keeps the robot away from the obstacles and the strength of the repulsive potential depends on how close the robot is to the obstacle. The repulsive potential is defined in terms of distance to the closest obstacle $D(q)$, defined as (Choset et al., 2005):

$$U_{rep}(q) = \begin{cases} \frac{1}{2} \eta \left(\frac{1}{D(q)} - \frac{1}{Q^*} \right)^2, & D(q) \leq Q^* \\ 0, & D(q) > Q^* \end{cases}$$

whose gradient is

$$\nabla U_{rep}(q) = \begin{cases} \eta \left(\frac{1}{D(q)} - \frac{1}{Q^*} \right) \frac{1}{D^2(q)} \nabla D(q), & D(q) \leq Q^* \\ 0, & D(q) > Q^* \end{cases}$$

The utilization of the Q^* factor allows the robot to ignore obstacles that are sufficiently far away, while η can be considered as a gain on the repulsive gradient. In case that these algorithmic formulations are being applied, it is possible to produce a path, which it might oscillate around points that are equally distant in both directions from the obstacles. To avoid these oscillations, the repulsive potential can be defined in terms of distances to individual obstacles, instead of just the closest obstacle. Then each obstacle has its own potential function as (Choset et al., 2005):

$$U_{rep_i}(q) = \begin{cases} \frac{1}{2}\eta \left(\frac{1}{d_i(q)} - \frac{1}{Q_i^*} \right)^2, & \text{if } d_i(q) \leq Q_i^* \\ 0, & \text{if } d_i(q) > Q_i^* \end{cases} \quad (1)$$

where Q_i^* defines the size of the domain of influence for obstacle i . Then the total repulsive field becomes:

$$\sum_{i=1}^n U_{rep_i}(q). \quad (2)$$

An significant advantage of the APF method is the fact that it could be realised also for controlling the velocity of the robot. In this approach, the translation velocities (v_x, v_y) can be set proportional to the force $F(q)$ that is generated by the potential field as:

$$F(q) = -\nabla U_{att}(q) - \nabla U_{rep}(q) \quad (3)$$

An object in the physical environment often consists of a regular shape and material. The problem in detecting obstacles is how the obstacles should be distinguished from the environment, and how to determine where the obstacle begins and where the ground begins.

2.2 Depth Image Pre-filtering Process

The depth image from the kinect is somewhat unstable and flickery, since in some regions the depth camera cannot read any depth values, which are presented as completely black regions in Fig. 2, marked by red rectangulars. Moreover, these regions are changing over the time, a fact that causes the video to flicker. Thus the depth sequential frames from the kinect should be processed to filter and exclude this flickering and also to extract the necessary information needed for detecting obstacles. Since the kinect gives depth values in the range 0.5m - 3m, the first step is to filter out values larger than a certain threshold. The reason for this is the fact that obstacles being far away as 3m from the robot should not have an influence on the robot's movement. Thus after thresholding the acquired depth image is being filtered to display values only in the region of 0.5m - 1.5m. This

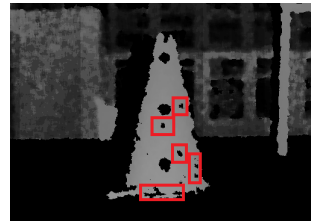


Figure 1: Depth image before image processing with dead regions marked with red squares.

filtering has also a direct effect on the processing time due to the less data needed to be processed.

For avoiding the flickering effect, mentioned earlier, a median filter has been utilized and applied through every depth image acquisition, where is image entry is being replaced by the median of the neighbouring entries (Justusson, 1981). A comparison among the original sampled depth image and after the application of the median filtering is being presented in Fig. 2.

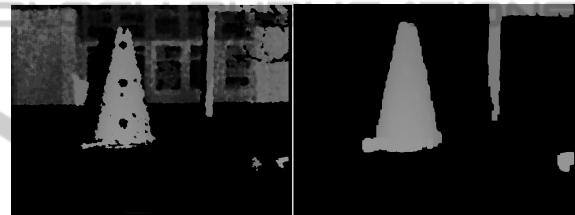


Figure 2: Depth image before (left) and after (right) image processing.

Finally to determine where an obstacle boarder begins and ends edge detection can be used. The detection is made by identifying points in the depth image frames, where the brightness changes sharply. The edge detection algorithm used in this research is the Canny edge detection (Francis, 1983).

2.3 Depth Image based APF

Often, when the APF method is implemented on mobile robots, the sensor used is some type of distance sensor; sonar or laser range (Kalmegh et al., 2010),(Sercan and Hakan, 2011), while very little work has been done where the APF method is implemented with a camera as a sensor. With this type of imaging sensor, new problems arise during the implementation of the APF method. Since the camera faces forward in the robots moving direction, the angles to all the obstacles is harder to obtain. Also since the depth data are filtered and only obstacles in the desired region can be seen, the depth values of the open regions between obstacles can not be taken into account when calculating the forces.

The first step in implementing the APF with a depth camera is to determine a Region Of Interest (ROI). This will make the image processing faster, while the robot does not have to consider the whole environment, but only an important part of it. The ROI should be selected in a way such that the robot can detect relevant obstacles and not lose too much information about its surroundings and thus a trade off should be applied. The kinect sensor provides the depth values as the distance from an imaginary plane, going through the kinect, and this z-value can then be used as r_y , while the x-value can be utilized as r_x . The robot's direction of movement is then calculated by applying (3) to each pixel in the ROI and then each force component is summed up to result in the overall force vector F_{res} in which the robot should move. The left and right wheel speeds are determined by normalizing the resulting force vector as:

$$\hat{F}_{res} = \frac{F_{res}}{\|F_{res}\|} \quad (4)$$

The resulting force vector will then end up on a circle with maximum radius equal to one. If the resulting force is pointing at 90° the robot should move straight forward and with a force pointing at 0° , the robot should turn right in-place and between these extremes do varying degrees of turning.

3 NAVIGATION BASED ON MODIFIED APF

In the presented approach it is assumed that the robot knows neither the map of the environment nor the start or goal position (free exploration mission). This introduces a problem when it comes to calculating the attractive potential. Since there is no point that attracts the robot, the attractive potential must be based on something else than a goal position. This can be solved by making the robot attracted by open spaces, or equivalently distance measurements greater than a certain threshold value are considered as attractive forces to the robot. With this approach in mind, the force in (3) can be rewritten as (Kalmegh et al., 2010):

$$F_i = k \left(\frac{1}{t^2} - \frac{1}{|r_\theta|^2} \right) \cdot \hat{r}_\theta, \quad (5)$$

where t is the threshold distance. Equation (5) is the force produced by the measured distance r_θ , and if r_θ is larger than the threshold distance the force becomes attractive and the opposite occurs if r_θ is smaller than the threshold. The total force is then the sum of all the forces:

$$F_{tot} = k \sum_{\theta=0}^{2\pi} \left(\frac{1}{t^2} - \frac{1}{|r_\theta|^2} \right) \cdot \hat{r}_\theta, \quad (6)$$

where:

$$r_\theta = \begin{bmatrix} r_x \\ r_y \end{bmatrix} = \begin{bmatrix} r \cdot \cos \theta \\ r \cdot \sin \theta \end{bmatrix}. \quad (7)$$

and

$$|r_\theta|^2 = r_x^2 + r_y^2 \quad (8)$$

$$\hat{r}_\theta = \frac{r_\theta}{\|r_\theta\|}. \quad (9)$$

Equations (8), (9) are then used together with equation (6) to calculate the total force vector acting on the robot. The robot is then steered in the direction of the resulting force, and driving with a velocity proportional to the magnitude of the force, while the overall concept is presented in Figure 3.

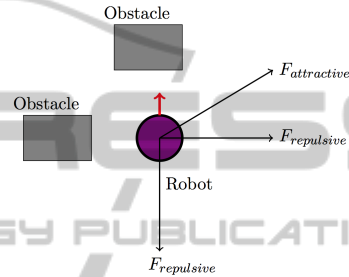


Figure 3: Basic principle of APF method with attraction to open spaces.

3.1 Kinematic model of the robot

In this research effort, the robot is considered as a rigid body on wheels, operating on a horizontal plane. The position of the robot can be expressed as vector, q , with respect to the global reference frame as (Sercan and Hakan, 2011):

$$q_I = [x \quad y \quad \theta]^T$$

Where x , y and θ represents the position and orientation of the robot respectively. The transformation between the local velocities and the generalized velocities can be calculated as (Sercan and Hakan, 2011):

$$\begin{bmatrix} \dot{x} \\ \dot{y} \\ \dot{\theta} \end{bmatrix} = \begin{bmatrix} \cos(\theta) & \sin(\theta) & 0 \\ -\sin(\theta) & \cos(\theta) & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} v_x \\ v_y \\ \omega \end{bmatrix} \quad (10)$$

while, for preventing lateral slip, the following non-holonomic constraints must be applied as:

$$v_y - \omega \cdot d = 0 \quad (11)$$

$$[\sin(\theta) \quad \cos(\theta) \quad -d] \cdot [\dot{x} \quad \dot{y} \quad \dot{\theta}]^T = A(q)\dot{q} = 0 \quad (12)$$

where d is defined as the distance between the robot's center of mass and center of geometry. Then (10) can be rewritten as:

$$\dot{q} = S(q) \cdot u \quad (13)$$

$$S(q) = \begin{bmatrix} \cos(\theta) & -d \sin(\theta) \\ \sin(\theta) & d \cos(\theta) \\ 0 & 1 \end{bmatrix}, u = [v_x \ \omega]^T \quad (14)$$

Which represents the kinematic model of the robot with u the control input.

3.2 Height Measurement

With a camera as a sensor it is quite straight forward to obtain the height of an object in the field of view, with the help of some basic geometry.

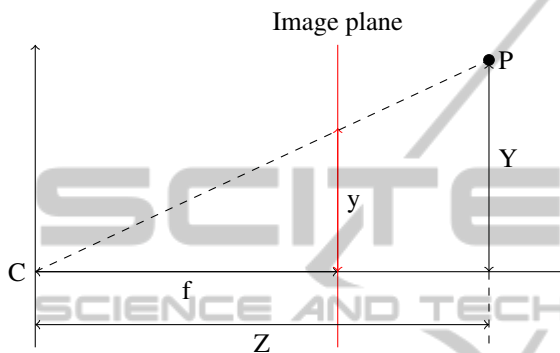


Figure 4: Definitions of image and real world coordinated.

From Figure 3 and the utilization of similar triangles principle the following relationships can be obtained as:

$$\frac{y}{f} = \frac{Y}{Z} \longrightarrow Y = Z \cdot \frac{y}{f} \quad (15)$$

where f is the focal length obtained from camera calibration, y is the y -coordinate of point P , Y is the real world y -coordinate of point P and Z is the depth value of point P . Both f and y are in pixels and Z is given in meters. With equation (4.32) it is possible to determine the real world height of an object in the field of view. To simplify the calculations, only the height of the closest obstacle is considered. A scenario that can cause problems, even though the obstacle might be low enough for the robot to pass over, is when the whole obstacle appears between the wheels as illustrated in Fig. 5.

When both points P_1 and P_2 are inside the danger zone, the robot should avoid the obstacle. By extracting the depth value to the obstacles center point, from the depth sequential frames, (7) can be utilized to calculate the repulsive force generated by the obstacle and the robot can safely avoid it.

4 EXPERIMENTAL SETUP

The platform used in this research is a robotic vehicle called "Wild Thumper" (WT). This platform is spe-

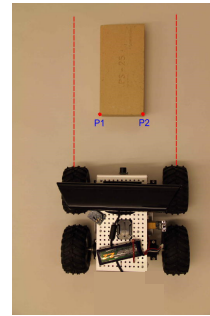


Figure 5: Danger zone for obstacles.

cially made to drive in rough environments. The WT has big wheels with very rough patterning, and it has four DC-motors, one for each wheel, that makes it possible to drive each wheel separately. This property is useful when not all wheels are in contact with an obstacle, since the speed on each wheel can be controlled separately. The special super-twist suspension on each wheel makes the platform good for driving in very uneven terrain, while it guarantees that always one wheel will be in contact with the ground.

The main processing unit on the robot is the Arduino Due microcontroller. This board is based on the Atmel SAM3X8E ARM Cortex-M3 CPU and the main benefit of this board is the computational speed. The motor controller board used here is the Rover 5 motor driver board for driving each motor and also to receive the data generated from the encoders. The communication between the main computer and the Arduino board is done with an XBee-link. XBee is a form factor compatible radio module that uses Zig-Bee protocol. Two XBees are needed for this setup for a bi-directional communication link; one mounted on the Arduino board and one connected to the main computer. To measure the rotational speed of the wheels, four rotary magnetic encoders are mounted on each motor shaft. The resolution of the encoders is 2000 pulses per revolution. All these additional electromechanical components have been properly mounted on the WT robot as it has been depicted in Fig. 6.

The overall proposed modified APF algorithm is being presented in Fig. 7. The procedure is divided into two main parts; one in which the artificial forces from each pixel in the ROI are calculated and one where the artificial forces depending on the obstacle height are calculated. The first step in both parts is to convert the image coordinates into real world coordinates and also to convert the RGB depth image into an intensity image. To extract the correct x and z values corresponding to the ROI, a filter is used and to eliminate the flickering a median filter is used on the depth image. The main calculations then uses these

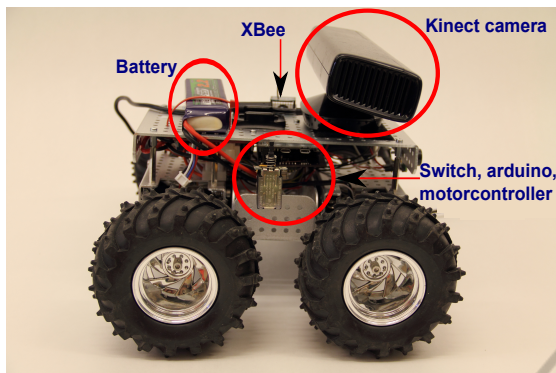


Figure 6: Side view.

filtered x and z values and the ROI-image to calculate the total resulting force. This is done by looping through each pixel in the ROI and calculating and saving the force components. The calculations for height requires the y values to be in pixels to be able to calculate the real world height of the obstacles. A blob analysis is made on the processed image and from this the coordinates of the detected blobs corners are sent to the force calculations. When the height of the closest obstacle is determined the next step is to determine if it is lower than the threshold and also if it is inside the danger zone. Depending on if the obstacle is low enough and if it lies inside the danger zone the force from that obstacle is either calculated as F_{height} or set to zero. Finally, in the last step F_{height} is added to the force calculated from the ROI. The corresponding left and right wheel speeds are sent to the Arduino via the XBee link and directed to the motor controller, which in turn sends the commands to the motors. The speeds of each motor is then measured with the encoders and sent back to the Arduino in which an internal PI-controller is utilized for each motor speed.

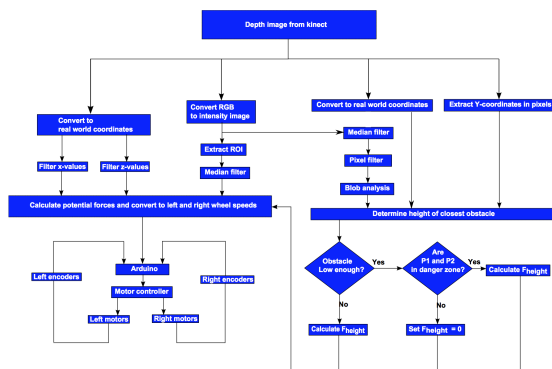


Figure 7: Overall Flow Chart of the Proposed Modified APF.

5 EXPERIMENTAL RESULTS

The evaluation of the overall proposed scheme has been carried in experimental studies, while investigating the behaviour of the robot in different scenarios. The first group of tests were made without considering the height of the obstacles and the second group of tests the height consideration were added to the calculation of the APF forces in order to directly evaluate the efficiency of the proposed scheme.

The first experimental test was carried with respect to the S-shaped obstacle course as it is being presented in Fig 8. The path of the robot was recorded



Figure 8: S-shaped obstacle position.

with odometry and is presented in Fig. 9, where the blue rectangles represent the real obstacles. From the

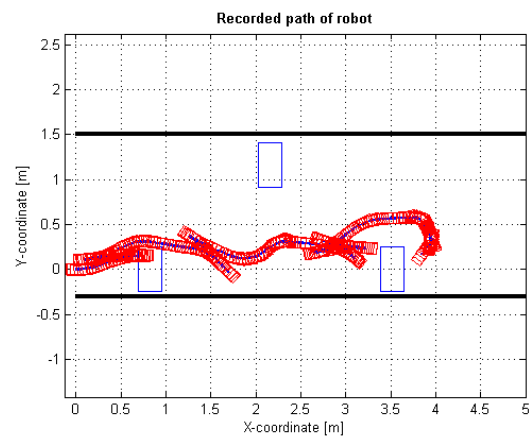


Figure 9: Recorded path of robot.

obtained results it is obvious that the robot is capable of detecting properly the obstacles and transverse towards the no obstacle-empty space. The acquired depth images and the selected ROI and filtering processes are sufficient capable of driving backward and forward the robot, while once more it should be highlighted that the robot is not aware of the starting and finishing goal.

The second test was conducted in order to evaluate the performance of the robot navigation, when obstacles of low height have been inserted in the robots path, as it is being presented in Fig. 10. As before, the path of the robot has been recorded by odometry and the results are presented in Fig. 12 from a side view. From the obtained results it is obvious that the

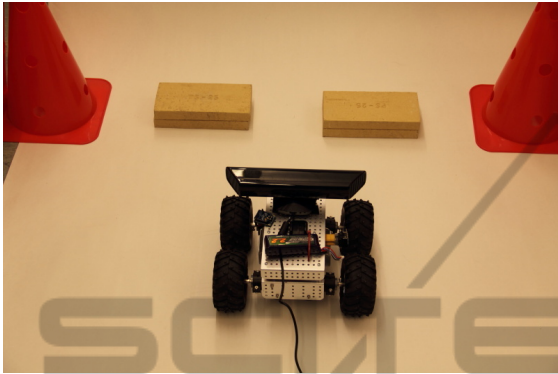


Figure 10: Terrain with obstacles of various sizes.

robot, based on the supplied depth images, is able to detect the obstacles, while is not able to recognise the corresponding height of them and thus the robot is performing continuous forward and backward moves, without managing to overcome the obstacles. However, in case that the consideration of the height measurement as a factor for altering the calculation of the potential fields, as it is being presented in Fig. 12 it is clear that the robot manages to overcome the small scale obstacles by driving over them.

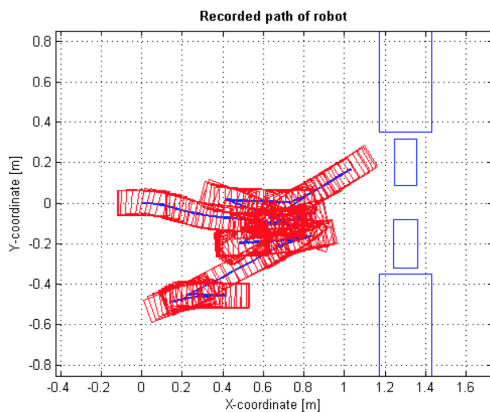


Figure 11: Recorded path of the robot for the terrain with obstacles of various sizes, without the modified APF for considering the height of obstacles.

In the case of off-road terrains, characterised by numerous small obstacles, the presented modified APF methodology would have a significant impact, since it will enable the direct driving of the robot, while avoiding false path alterations being initiated

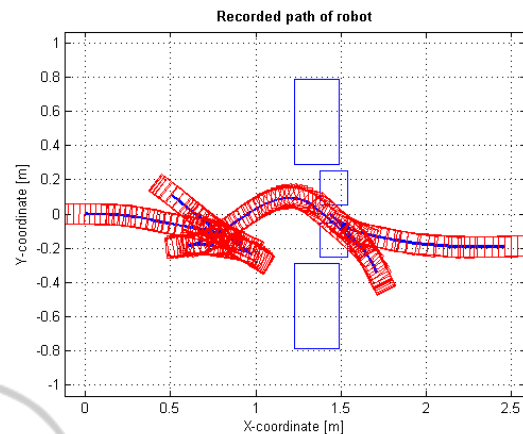


Figure 12: Recorded path of the robot for the terrain with obstacles of various sizes, with the modified APF for considering the height of obstacles.

by the existence of small scale obstacles that could be easily ignored and bypassed by the robot.

6 CONCLUSIONS

In this article an experimental evaluation of a modified obstacle based artificial potential field algorithm for an off-road mobile robot has been presented. The modification relied on altering the APF algorithm in order to make it suitable for utilising a visual feedback and proposing a novel scheme for the identification and perception of obstacles. Based on the proposed methodology, the vehicle was capable of categorising the obstacles based on their height in order to alter the calculated forces, for enabling a cognitive decision regarding their avoidance or the driving over them. The performance of the proposed modified potential field algorithm has been experimentally applied and evaluated in multiple robotic exploration scenarios, where from the obtained results the efficiency and the advantages of such a modified scheme have been depicted.

REFERENCES

- Broggi, A., Caraffi, C., Fedriga, R., and Grisleri, P. (2005). Obstacle detection with stereo vision for off-road vehicle navigation. *IEEE Computer Society Conference on Computer Vision and Pattern Recognition*.
- Choset, H., Lynch, K., S.Hutchinson, Kantor, G., Burgard, W., Kavraki, L., and Thrun, S. (2005). Principles of robot motion; theory, algorithms and implementations. *MIT Press*.
- Francis, C. J. (1983). Finding edges and lines in images. *Massachusetts Inst. of Tech. Report 1*.

- Guo, J., Gao, Y., and Guangzhao, C. (2013). Path planning of mobile robot based on improved potential field. *Information Technology Journal*, 12.
- Hirose, S., Fukushima, E., Damoto, R., and Nakamoto, H. (2001). Design of terrain adaptive versatile crawler vehicle helios-vi. *International Conference on Intelligent Robots and Systems*, pages 1540–1545.
- Justusson, B. (1981). Median filtering: Statistical properties. *Springer*.
- Kalmegh, S., Samra, D., and Rasegaonkar, N. (2010). Obstacle avoidance for a mobile exploration robot using a single ultrasonic range sensor. *International Conference on Emerging Trends in Robotics and Communication Technologies*, pages 8–11.
- Khatib, O. (1986). Real-time obstacle avoidance for manipulators and mobile robots. *International Journal of Robotics Research*, 5:500–505.
- Matthies, L., Gat, E., Harrison, R., Wilcox, B., Volpe, R., and Litwin, T. (1995). Mars microrover navigation: Performance evaluation and enhancement. *Autonomous Robots*, 2:291–311.
- Schlengel, N., Kachroo, P., Ball, J., and Bay, S. (1997). Image based control for scaled automated vehicles. *IEEE Conference on Transportation System*.
- Sercan, A. and Hakan, T. (2011). Robust motion control of a four wheel drive skid-steered mobile robot. *7th international conference on electrical and electronics engineering*.
- Sieglwart, R., Lamon, P., Estier, T., Lauria, M., and Piguat, R. (2002). Wireless sensor networks: a survey. *Computer Networks*, 38(4):393–422.
- Vadakkepat, P., T., K., and Ming-Liang, W. (2000). Evolutionary artificial potential fields and their application in real time robot path planning. *Proceedings of the 2000 Congress on IEEE Evolutionary Computation*, 1.
- Valavanis, K., Hebert, T., Kolluru, R., and Tsouverloudis, N. (2000). Obstacle avoidance for a mobile exploration robot using a single ultrasonic range sensor. *Systems, Man and Cybernetics, Part A: Systems and Humans, IEEE Transactions on*, 30:187–198.
- Zhang, T., Yi, Z., and Jingyan, S. (2010). Real-time motion planning for mobile robots by means of artificial potential field method in unknown environment. *Industrial Robot: An International Journal*, pages 384–400.