

# Compressive Video Sensing with Adaptive Measurement Allocation for Improving MPEGx Performance

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**Abstract:** Remote imaging systems, such as unmanned aerial vehicles (UAVs) and terrestrial-based visual sensor networks, have been increasingly used in surveillance and reconnaissance both at the civilian and battleground levels. Nevertheless, most existing solutions do not adequately accommodate efficient operation, since limited power, processing and bandwidth resources is a major barrier for abandoned visual sensors and for light UAVs, not well addressed by MPEGx compression standards. To cope with the growing compression ratios, required for all remote imaging applications to minimize the payloads, existing MPEGx compression profiles may result in poor image quality. In this paper, the inherent property of compressive sensing, acting simultaneously as a sensing and compression framework, is exploited to build a compressive video sensing (CVS) system by modifying the standard MPEGx structure, such as to cope with the limitations of a resource-restricted visual sensing system. Besides, an adaptive measurement allocation mechanism is introduced, which is combined with the CVS approach achieving an improved performance when compared with the basic MPEG-2 standard.

## 1 INTRODUCTION

Modern high-resolution visual sensing devices, with processing and communication capabilities, largely based on the seminal Shannon and Nyquist studies, have enabled the acquisition, storage, and transmission of ever increasing amounts of visual data. However, the increasing demand for higher acquisition rates and even improved resolution is placing significant burden on existing hardware architectures.

An area which could benefit significantly by the introduction of efficient computational models is video acquisition. A characteristic example is the design of remote imaging systems, such as unmanned aerial vehicles (UAVs) and terrestrial visual sensor networks, which have been increasingly used in surveillance and reconnaissance applications. Recent technological advances enable the design of low-cost devices that incorporate multimodal sensing, processing, and communication capabilities. At the same time, the limited resources of the compression hardware still is a major issue for such light-weight remote imaging systems. To cope with such growing compression ratios existing MPEGx techniques may result in poor image quality.

The framework of *compressive video sensing* (CVS) was introduced recently as an extension of *compressive sensing* (CS) theory (Candès et al., 2006). In particular, CVS methods aim at enabling low-complexity onboard remote image acquisition and compression using a reduced amount of linear incoherent random projections, while maintaining a similar reconstruction performance when compared to standard video compression techniques.

In existing CVS methods, a non-overlapping block splitting is applied first for each frame, followed by full sampling of the reference frames and CS-based acquisition of the non-reference frames. Then, the reconstruction is performed separately (Stanković et al., 2008), or jointly by either considering a joint sparsity model as in (Kang and Lu, 2009), or by designing an adaptive sparsifying basis using neighboring blocks in previously reconstructed frames (Do et al., 2009; Prades-Nebot et al., 2009). The major drawback in the first case is that, since potential spatio-temporal redundancies are not exploited, the corresponding CVS methods usually result in higher bit-rates, while also being sensitive to reconstruction failures. The propagation of reconstruction errors along the video sequence is also a common charac-

teristic of CVS methods performing joint decoding, since inter-frame correlations are still not considered at the encoder.

An efficient video representation must remove potential spatio-temporal redundancies, which is an important issue towards the reduction of the transmitted information. In recent studies (Marcia and Willett, 2008; Jacobs et al., 2010; Park and Wakin, 2009), a first attempt was made to account for inter-frame correlations expressed via the estimated motion between consecutive frames. However, these approaches still suffer from several drawbacks, such as the separate encoding of each frame, thus without removing a significant part of the inherent temporal redundancy, or the attainment of a satisfactory performance only for video sequences with slowly varying content.

In the present work, we address the above drawbacks by introducing a CVS scheme, which combines the advantages of MPEGx in traditional video compression along with the power of CS in representing and reconstructing highly sparse signals with increased accuracy. The performance of our method is further enhanced by introducing a simple, yet very efficient, adaptive measurement allocation mechanism. We demonstrate that the proposed approach satisfies the restrictions of a remote imaging system with limited resources, while outperforming the standard MPEGx implementation under certain conditions. We emphasize though that the present study does not intend to compete optimally designed MPEGx-based industrial solutions, but to highlight the potential of embedding CS-based modules in existing MPEGx standards towards improving the overall performance of the combined system.

The paper is organized as follows: in Section 2, the CS frame acquisition model is reviewed. Section 3 describes in detail the structure of the proposed CVS system, along with key-factors that affect its robustness, and compares its performance against the standard MPEG-2 approach. Finally, conclusions and further extensions are outlined in Section 4.

## 2 CS FRAME MODEL

For convenience, we consider the case of  $N \times N$  frames, with the main disadvantage being the high computational and memory expense when we deal with high resolutions, which may be prohibitive for a system with limited capabilities. A straightforward solution is to proceed in a non-overlapping block-wise fashion. In the proposed CVS system, each frame is divided into equally-sized  $n_B \times n_B$  non-overlapping blocks. Then, a random measurements

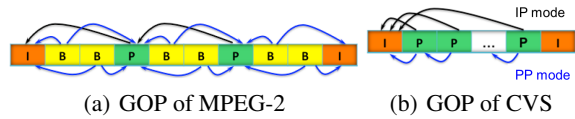


Figure 1: GOP formations for MPEG-2 and CVS.

vector  $\mathbf{g}_j$ ,  $j = 1, \dots, B$ , is generated for each one of the  $B$  blocks by employing a suitable measurement matrix  $\Phi$  (for simplicity the same matrix is used for each block) as follows,

$$\mathbf{g}_j = \Phi(\Psi_c \mathbf{x}_j), \quad (1)$$

where  $\mathbf{x}_j \in \mathbb{R}^{n_B \times n_B}$  denotes the  $j$ -th block of frame  $\mathbf{x}$  using a predetermined enumeration pattern,  $\Psi_c \in \mathbb{R}^{n_B \times n_B}$  is a *coding transform* basis and  $\Phi \in \mathbb{R}^{M_B \times n_B^2}$  is a random measurement matrix with  $M_B \ll n_B^2$ . Notice that  $\Phi$  is applied on a vectorized version of  $\Psi_c \mathbf{x}_j$ , which is reshaped into an  $n_B^2 \times 1$  column vector. If the  $j$ -th block has a  $K$ -sparse representation in an appropriate sparsifying transform domain, and if the measurement operator along with the sparsifying transformation satisfy a sufficient incoherence condition, then  $\mathbf{x}_j$  can be recovered from  $M_B \gtrsim O(2K \log n_B)$  measurements by solving the following optimization problem,

$$\min_{\mathbf{w}_j} (\|\mathbf{w}_j\|_1 + \tau \|\mathbf{g}_j - \Phi \Psi_s^{-1} \mathbf{w}_j\|_2^2), \quad (2)$$

where  $\Psi_s$  is an appropriate *sparsifying transformation*, such as an orthonormal basis (e.g., discrete wavelet transform (DWT)) or an overcomplete dictionary (e.g., undecimated DWT (UDWT)),  $\mathbf{w}_j$  is the transform-domain representation of  $\mathbf{x}_j$  in  $\Psi_s$ , and  $\tau$  is a regularization parameter that controls the trade-off between the achieved sparsity (first term) and the data fidelity (second term). If  $\Psi_s$  is different than the identity, then the reconstruction of the  $j$ -th block is first performed in the transform domain,  $\hat{\mathbf{w}}_j$ , followed by an inversion to obtain the final spatial-domain estimate,  $\hat{\mathbf{x}}_j = \Psi_s^{-1} \hat{\mathbf{w}}_j$ . Otherwise, the spatial-domain solution is obtained directly, that is,  $\hat{\mathbf{x}}_j \equiv \hat{\mathbf{w}}_j$ .

In a remote imaging system, some additional requirements should be posed on the choice of the measurement matrix  $\Phi$ , such as the use of a minimal number of compressed measurements, as well as their fast and memory-efficient computation along with a “hardware-friendly” implementation. A class of matrices satisfying these requirements, the so-called *structurally random matrices*, was introduced in (Do et al., 2008). The block Walsh-Hadamard (BWHT) operator is a typical member of this class, which is employed in our proposed method.

### 3 PROPOSED CVS SYSTEM

In this section, our proposed CVS system is introduced and analyzed with respect to various key-factors that affect its performance. We start with a brief review of the core components of MPEG-2, to which we compare in the rest of the paper.

#### 3.1 Overview of MPEG-2

At the core of all MPEGx coding standards is the exploitation of spatio-temporal redundancies among adjacent frames. Focusing on MPEG-2, each frame is divided in non-overlapping  $8 \times 8$  blocks. Compression along the temporal dimension is achieved using *motion estimation* (ME) and *motion compensation* (MC), followed by a 2-D DCT applied on each block to account for spatial redundancies. The encoding process is completed with the quantization of DCT coefficients, followed by Huffman coding. The video sequence is viewed as a set of consecutive groups-of-pictures (GOPs), consisting of I, B, and P frames, as shown in Fig. 1(a). More specifically, I-frames are fully sampled and encoded using a standard compression algorithm, such as JPEG. On the other hand, P-frames are encoded with prediction from previous I or P frames, while B-frames are encoded using prediction from both previous and subsequent I and/or P frames, depending on their position in the GOP.

During the ME step, the best match, under a minimum mean absolute error (MAE) or mean squared error (MSE) criterion, of each block in the current frame is searched among the blocks in a previously stored reference frame (or frames). The success of MPEGx is primarily based on the use of the (highly) *sparse residual* frames, which are simply the prediction errors between the predicted and the actual block. Motivated by this, we exploit directly the inherent sparsity of the residual-frame domain in the framework of CS for the design of our proposed CVS system. Besides, note that the GOP formation used in MPEG-2 is not suitable for remote imaging systems with limited memory resources, since the frames must be stored in a buffer and reordered in order to compute the residuals. An alternative and more memory-efficient GOP formation is used in our CVS system, which consists of I and P frames only, and thus it requires a single-frame buffer (ref. Fig. 1(b)). Doing so, there are two options: either estimate the residuals between the current P and the previous I frame (IP mode), or between two adjacent frames (PP mode). To avoid the error propagation, which is inherent in the PP mode, the IP mode is employed instead.

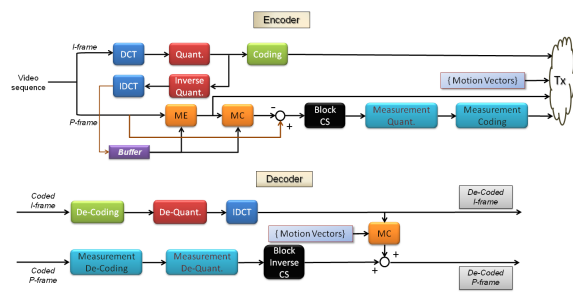


Figure 2: Proposed CVS system.

#### 3.2 Proposed CVS System Structure

The structure of our proposed CVS scheme is shown in Fig. 2. Specifically, it consists of an encoder - decoder pair, where appropriate CS-based modules are embedded in both sides of an MPEGx architecture.

In the subsequent analysis, the similarity between two frames, and also the reconstruction quality, is measured in terms of the *structural similarity index* (SSI), which resembles more closely the human visual perception than the commonly used *peak signal-to-noise ratio* (PSNR). For a given pair of images  $I, \hat{I}$  the SSI is defined by,

$$SSI(I, \hat{I}) = \frac{(2\mu_I\mu_{\hat{I}} + c_1)(2\sigma_{\hat{I}\hat{I}} + c_2)}{(\mu_I^2 + \mu_{\hat{I}}^2 + c_1)(\sigma_I^2 + \sigma_{\hat{I}}^2 + c_2)}, \quad (3)$$

where  $\mu_I, \sigma_I$  are the mean and standard deviation of the luminance of image  $I$  (similarly for  $\hat{I}$ ),  $\sigma_{\hat{I}\hat{I}}$  denotes the correlation coefficient of the two images, and  $c_1, c_2$  stabilize the division with a weak denominator. In particular, when SSI is equal to 0 the two images are completely distinct, while when the two images are matched perfectly SSI is equal to 1.

##### 3.2.1 CVS Encoder

In this section, the main constituent parts of the proposed CVS encoder are described, along with the parameters affecting their performance.

*a) Motion Estimation.* The reconstruction quality of our CVS system depends highly on the achieved sparsity of the residual frames, controlled by the ME process. To this end, we tested the efficiency of well-established ME algorithms, each one differing from the others in the way the neighborhood of the current block is scanned to find the best match. Among them, the Adaptive Rood Pattern Search (ARPS) (Nie and Ma, 2002) was shown to follow closely the optimal Exhaustive Search (ES) approach, while also performing a minimum average number of search steps in the neighborhood of the current block until the best matching is found. Based on that, ARPS was chosen in our proposed CVS system.

We note that the experimental evaluations in the rest of the paper are performed on the *luminance component* of three infrared (IR) videos of distinct content<sup>1</sup>: i) iruw02 (static background, moving foreground), ii) irw06 (static background, moving foreground), and iii) UAV (complex motion content).

*b) Block Size.* Two distinct types of blocks must be distinguished clearly. The first is related to the ME process, for which we adopt the option of MPEG-2 setting the block-size equal to  $8 \times 8$  and performing the ME on macro-blocks of size  $16 \times 16$ . The second is related to the CS measurement acquisition and controls the degree of sparsity of a residual frame. We found experimentally that a satisfactory trade-off between the CS block-size and the achieved sparsity is obtained for blocks of size  $32 \times 32$ .

*c) Sampling Operator.* The sampling operator in (1) is determined by the coding transformation  $\Psi_c$  and the measurement matrix  $\Phi$ . Common choices for  $\Psi_c$  are the *discrete cosine transform* (DCT) and the DWT (with the 9/7 wavelet as in JPEG2000), which have been shown to achieve a high degree of sparsity for a broad range of images, while  $\Phi$  is chosen to be a BWHT matrix, which is computationally efficient, as it was mentioned in Section 2.

*d) Quantization & Coding.* The simple uniform quantizer used in MPEG-2 is also adopted by the quantization module of our system, so as to make a fair comparison between the two architectures. The quantized CS measurements for all blocks of the current residual frame are then encoded using an improved Huffman coding scheme using recursive splitting (Skretting et al., 1999). Fig. 3 shows the average SSI as a function of the number of quantization bits for the three video sequences. First, we observe that CVS outperforms MPEG-2 as the number of quantization levels decreases, that is, as the resolution of the available information at the decoder becomes coarser. This difference is more prominent for the UAV sequence, whose motion content is more complex when compared with iruw02 and irw06.

*e) CS Sampling Ratio.* The reconstruction quality improves with an increasing CS sampling ratio ( $r = M_B/n_B^2$ ) of the acquired CS measurements ( $M_B$ ) over the CS block-size ( $n_B \times n_B$ ), but at the cost of higher bit-rates. A reduction of the total bit-rate is achieved by designing an *adaptive measurement allocation* approach, as it is described in Section 3.3.

<sup>1</sup>iruw02 and irw06 were obtained from <http://www.cse.ohio-state.edu/otcbvs-bench/>; UAV was provided by SAGEM.

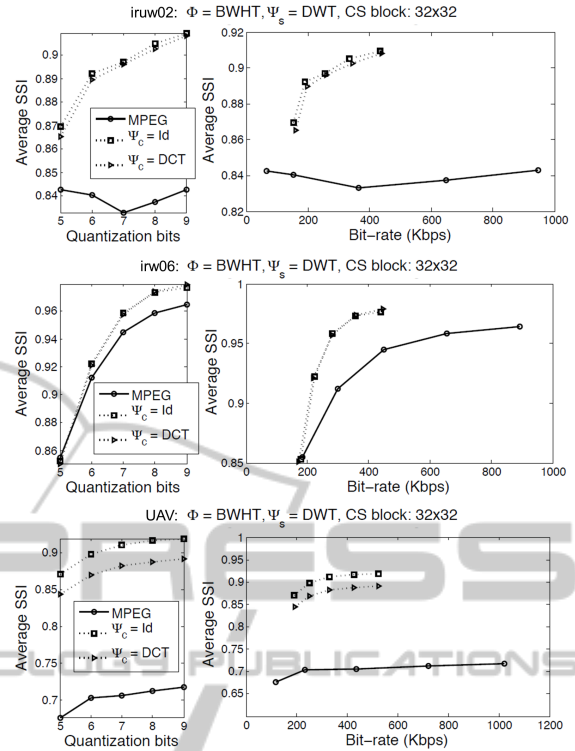


Figure 3: Reconstruction performance as a function of quantization levels.

### 3.2.2 CVS Decoder

At the decoder side, the main components along with the associated factors affecting their performance are analyzed below.

*a) Sparsifying Transformation.* In general, the sparsifying transformation  $\Psi_s$  used in (2) can be different from the coding transformation  $\Psi_c$ . In the later case, an orthonormal basis is preferred for the coding of the residual blocks, whereas in the former case the sparsifying transformation can be either a basis or an *overcomplete dictionary*, such as an UDWT. In fact, an overcomplete dictionary usually results in sparser representations, and consequently in an improved reconstruction quality at lower bit-rates, but at the cost of increased decoding time.

*b) Reconstruction Algorithm.* In our implementation, the TwIST<sup>2</sup> algorithm is used to solve the optimization problem (2), since it was shown to achieve a good trade-off between the computational complexity and the resulting reconstruction quality. However, a more thorough study concerning the optimal choice of the reconstruction method is left as a future work.

*c) Noisy Data.* In practice, we deal with data

<sup>2</sup>Matlab code and paper: <http://www.lx.it.pt/~bioucas/TwIST/TwIST.htm>.

corrupted by noise (e.g., instrumental, quantization, and channel). In the noisy case, an MPEGx-based approach requires denoising of at least the I and P frames in each GOP, since they are used together with the reconstructed residuals to obtain the rest of the P and B frames. On the other hand, one of the main advantages of CS is its inherent property to act as a denoising process by suppressing the reconstructed non-sparse part of the residual introduced by the noise. Thus, in our CVS system the denoising of only the I-frames should suffice. For the denoising, a double-density dual-tree complex DWT thresholding technique was employed<sup>3</sup>. The same denoising method is also used for the I and P frames of the MPEG-2 system for a fair comparison.

Fig. 4 compares for the three videos the average SSI between the proposed CVS system and the MPEG-2 approach, as a function of the input SNR, ranging from 10 dB to 40 dB, as well as the number of quantization bits,  $q \in [5, 9]$ . Clearly, the CVS system achieves a significant improvement against MPEG-2 in the case of noisy data, requiring a significantly reduced bit-rate especially for low input SNR values, while it achieves a comparable reconstruction quality when compared with MPEG-2 in the medium to high input SNR regime.

### 3.3 Adaptive Measurement Allocation

The superiority of MPEGx, which is usually observed for videos with slowly varying content is primarily due to the large number of small-amplitude DCT coefficients of the residual blocks because of the (almost) static regions in the original frames. A way to account for this redundancy is to perform a uniform thresholding on each CS block by applying the CVS scheme on the same percentage ( $\alpha\%$ ) of the largest amplitude DCT coefficients.

The main drawback of a uniform measurement acquisition is that it does not exploit the true sparsity of each individual residual block. Motivated by this, we design an *adaptive CS measurement allocation* mechanism, which is then added in the “Block CS” module of Fig. 2, analogously to the bit allocation process used by many modern compression architectures.

To this end, for a given  $N \times N$  residual frame  $R$ , the noise standard deviation,  $\sigma_\eta$ , is estimated first using the median absolute deviation (MAD) rule. Then, a block-wise DCT is applied followed by a thresholding of the transform coefficients with threshold  $\rho_{Th} = \lambda \sigma_\eta \sqrt{2 \log(N^2)}$ , where  $\lambda$  is a predefined scaling factor. Let  $K_{max} = r \cdot n_B^2$  be the maximum number

of CS measurements corresponding to a sampling ratio  $r$ , where  $n_B \times n_B$  is the CS block size. Doing so, the adaptive sampling ratio for the  $j$ -th CS block is given by

$$r_j = \frac{1}{n_B^2} \cdot \min(\text{card}(\{C_j > \rho_{Th}\}), K_{max}), \quad (4)$$

where  $C_j$  denotes the set of DCT coefficients of the  $j$ -th block. Finally, the associated number of CS measurements to be acquired for the  $j$ -th block is equal to  $M_j = \lfloor r_j \cdot n_B^2 \rfloor$ .

The bit-rate gain of the adaptive measurement allocation process is quantified by  $\text{bit-rate}_{gain} = \frac{B_0 - B_1}{B_0}$ , where  $B_0$  is the total number of bits for CVS coding of the original residual frames  $R$  using our adaptive measurement allocation method, and  $B_1$  is the total number of bits for coding the residual frames obtained by zeroing all except for the  $\alpha\%$  largest DCT coefficients of  $R$  and reconstructing using the IDCT.

Next, results are presented for the iruw02 sequence only, whilst a similar behavior was observed for the other two sequences. The achieved gains with respect to the required bit-rates are shown in Fig. 5. As it can be seen, a significant bit-rate gain is attained by applying the intermediate thresholding step followed by the adaptive allocation of CS measurements. Specifically, this gain is higher for smaller sampling ratios and quantization bits.

## 4 CONCLUSIONS

In this work, a variant of an MPEGx-based video compression system was introduced based on the principles of CS. Motivated by the success of MPEGx to remove spatio-temporal redundancies among frames by working with the residual frames, we exploited the sparse nature of the residual frames in conjunction with the power of CS to achieve a high reconstruction quality at reduced bit-rates. The performance was further improved by means of an adaptive measurement allocation scheme. Preliminary experimental results on infrared sequences revealed that the proposed CVS system is competitive with the well-established MPEG-2 approach, under appropriate specification of the several system components.

Several extensions of the current CVS design are possible. First, regarding the ME/MC modules, the simple but efficient ARPS method used in the current implementation can be substituted by a more accurate method resulting in even sparser residual frames. However, we must be always aware of keeping a balance between the estimation accuracy and the computational complexity in an imaging system with limited

<sup>3</sup>Matlab code and paper: <http://taco.poly.edu/selesi/DoubleSoftware/>

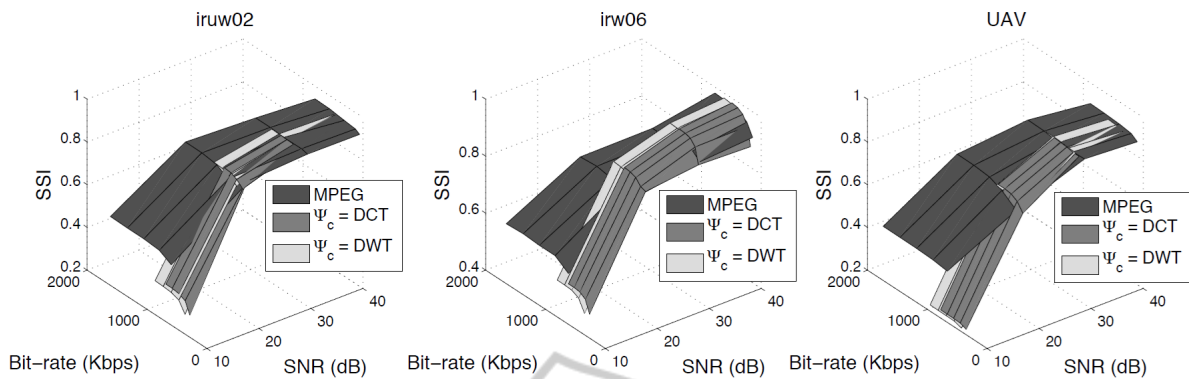


Figure 4: Average SSI as a function of bit-rate and input SNR.

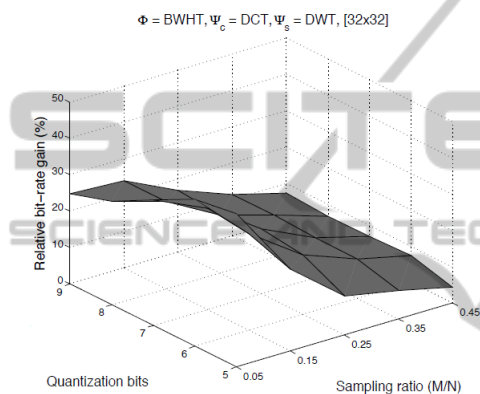


Figure 5: Effect of thresholding and adaptive measurement allocation on the bit-rate gain for the iruw02 sequence.

resources. Furthermore, the use of a uniform quantizer is by no means a sub-optimal choice. Instead, we expect that a quantizer adapted to the characteristics of CS measurements along with an appropriate reconstruction approach, as proposed in (Baig et al., 2010), could increase the compression rates at the encoder and the reconstruction quality at the decoder. Finally, concerning the CS reconstruction, especially in the noisy case, a challenging task will be to find systematic ways to set the optimal sampling operators, as well as the regularization parameters so as to adapt to the statistics of the noisy signals.

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