

On the Design of a Traffic Observatory Application based on Bus Trajectories

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Abstract: Buses, equipped with active GPS devices that continuously transmit their positions, can be understood as mobile traffic sensors. Indeed, bus trajectories provide a useful data source for analyzing traffic, if the city is served by a dense bus network and the city traffic authority makes the bus trajectories available openly, timely and in a continuous way. This paper explores the design of a traffic observatory application based on bus trajectories, defined as an application developed to detect when the traffic patterns of selected streets of a city, observed during certain periods of time, deviate from the typical traffic patterns. The major contributions of the paper are a list of requirements for traffic observatory applications, a detailed discussion of key operations on bus trajectories and a description of experiments with a traffic observatory prototype using bus trajectories made available by the traffic authority of the City of Rio de Janeiro.

1 INTRODUCTION

An intelligent control and management system, that has a data-driven approach for modelling, analysis, and decision-making (Zhang et al. 2013), may help achieve better traffic control and create mobility plans. As their main input data, such systems adopt trajectories, generated by GPS devices installed in vehicles (Shi et al. 2008), such as taxis (Zhu and Xu 2015) and buses (Sunil et al. 2014).

Indeed, buses, equipped with active GPS devices that continuously transmit their position, can be understood as mobile traffic sensors. A *raw bus trajectory* is a continuous data stream acquired from such a GPS device.

Bus trajectories provide a useful data source for analyzing traffic, if the city is served by a dense bus network and the city traffic authority makes the bus trajectories available openly, timely and in a continuous way. Under such conditions, bus trajectories are a better data source to analyze traffic than data generated by proprietary traffic applications that acquire the position of private cars and that depend on drivers' volunteered traffic feedback. Indeed, bus trajectories are a stable data source, in the sense that they cover the same set of streets, at

predictable regular intervals, if traffic conditions permit. In fact, this is the point: if the buses in a given area are not running according to the usual schedule, then a traffic perturbation is the most probable cause. Furthermore, if stored in an adequate way, bus trajectories will provide, over time, a historical picture of how the city evolved, much in the same way as satellite imagery gives a historical picture of how an urban area grew.

This paper explores the design of a *traffic observatory application* based on bus trajectories, defined as an application developed to detect when the traffic patterns of selected streets of a city, observed during certain periods of time, deviate from the typical traffic patterns. The design of such application poses at least the following challenges: (1) How to analyze the bus network (served by GPS-equipped buses) to select streets whose traffic can be monitored with the help of the bus trajectories; (2) How to mine a bus trajectory dataset to uncover traffic patterns; (3) How to detect traffic anomalies, estimate their impact and provide explanations, using data sources other than the bus trajectories; (4) How to maintain and compare different versions of the street network, the bus network and the traffic patterns, to help city planners assess changes.

The major contributions of this paper are three-fold: (1) a list of requirements for traffic observatory applications; (2) a detailed discussion of key operations on bus trajectories; (3) a description of experiments with a traffic observatory prototype using raw bus trajectories made available by the traffic authority of the City of Rio de Janeiro, which corroborate the usefulness of the proposed approach to monitor traffic.

The rest of this paper is organized as follows. Section 2 lists the basic requirements for a traffic observatory application. Section 3 introduces the main concepts related to street networks, bus networks and trajectories. Section 4 discusses some key operations on bus trajectories. Section 5 describes experiments with real data. Section 6 covers related work. Finally, Section 7 contains the conclusions.

2 REQUIREMENTS FOR A TRAFFIC OBSERVATORY APPLICATION

In this section, we enumerate the major requirements that a traffic observatory application, based on bus trajectories, must meet.

(1) *Select Streets Whose Traffic can be Monitored with the Help of Bus Trajectories.*

The first requirement quite simply reflects the fact that the traffic sensors are the buses equipped with GPS. The application must be able to analyze the bus network and select those streets that are frequently crossed by buses and whose traffic can, therefore, be monitored by analyzing the bus trajectories.

This requirement depends on a clear definition of the concepts of *street network*, *bus network* and *monitored street network*, the subset of the street network that can be monitored by analyzing the bus trajectories.

(2) *Discover Traffic Patterns.*

The second requirement refers to the basic question of defining what should be considered normal versus abnormal traffic behavior. Thus, the application must be able to mine a bus trajectory dataset to discover traffic patterns for select street segments, over a given period of time.

In addition to the definition of street network and bus network, this requirement depends on the concepts of *traffic patterns*, in the form of *traffic flow patterns* and *travel time patterns*.

(3) *Detect and Explain Traffic Anomalies, and Estimate their Impact.*

The third requirement covers the core of a traffic observatory application. It refers to monitoring the traffic for select street segments, over a given period of time, to uncover the observed traffic patterns, compare them with typical traffic patterns and, finally, mark the observed traffic patterns that deviate from the typical patterns above a given threshold.

Furthermore, this requirement includes identifying traffic events from additional data sources that might cause the deviations.

(4) *Maintain and Compare Different Versions of the Street Network, the bus Network and the Traffic Patterns.*

The last requirement imposes that the application must maintain versions of the street network, the bus network, the monitored street network and the traffic patterns. The application must also support comparing different versions of the street and bus networks to assess the impact of changes on select street segments, which provide a useful tool for city planners.

3 STREET NETWORKS AND TRAJECTORIES

In this section, we define the concepts identified in Section 2 and introduce the concept of trajectory.

3.1 Street Networks

For the purposes of this paper, a *geo-referenced street network* is modelled as a labelled, directed graph $G=(V,E,nl,el)$, where the node labelling function nl associates a geo-referenced point (in an appropriate geographic coordinate system) with each node in V and the edge labelling function el assigns a geo-referenced line segment (in the same the geographic coordinate system used by the node labelling function) to each edge in E . Intuitively, the edges represent street segments and the nodes indicate the start and end points of the street segments; these labelling functions must therefore be consistent with each-other. A street network may have other labelling functions, such as the street name to which the segment belongs.

The familiar notions of (*directed*) *path* and *circuit* from graph theory directly apply to street networks. A *street route* is simply a path in G .

A *flow pattern* for a node n in V is pair $\varphi=(\delta,\pi)$, where δ is a representation of the distribution of the flow of vehicles that pass by n and π is a specification

of the domain of δ (to facilitate comparing patterns). Likewise, a *travel time pattern* for a path p of G is a pair $\tau = (\gamma, \pi)$, where γ is a representation of the time distribution of the travel time of vehicles that traverse p and π is a specification of the domain of γ . Figure 2 at the end of the paper presents an example of travel time patterns.

Given a street network $G=(V,E,nl,el)$, a *bus line* of G is a set l of paths in G ; each path in l is called a *bus route* of l . That is, a bus line may have several alternative routes, which depend on the time of the day, for example. A *geo-referenced bus stop*, or simply a *bus stop*, of a bus route r is a point of a line segment that labels an edge in r . Given a street network $G=(V,E,nl,el)$, a *bus network* of G is a pair $N=(L,S)$, where L is a set of bus lines of G and S is a set of bus stops of the bus routes of the bus lines in L .

Finally, a *monitored street network* for a street network $G=(V,E,nl,el)$ and a bus network $N=(L,S)$ of G is a quadruple $M=(W,F,wl,fl)$ such that:

- $W \subseteq V$
- If (m,n) is in F then there is a bus route of a bus line in N that connects m and n
- wl is a function that labels each node n in W with the bus routes that pass through n
- fl is a function that labels each edge $f=(m,n)$ in F with the bus routes that that connects m and n

3.2 Trajectories

A *trajectory* is the representation of the position evolution of a moving object. We can have different representation levels: at the *raw trajectory level*, the sequence of sample points is represented as collected by the mobile device whereas, at the *segmented trajectory level*, homogeneous parts of a raw trajectory are identified based on some criterion.

More precisely, a *geo-referenced spatio-temporal point* is a pair $((x,y),t)$, where (x,y) is a geo-referenced point and t is a timestamp. A *raw trajectory* of a moving object is a sequence of geo-referenced spatio-temporal points, $s=((p_1,t_1),(p_2,t_2),\dots,(p_n,t_n))$, such that t_i is less than t_{i+1} , for $i=1,\dots,n-1$. A *segment* c of a raw trajectory s is a subsequence of s . Finally, a *segmented trajectory* of a raw trajectory s is sequence $g=(g_1,\dots,g_h)$ of segments of s such that s is the concatenation of g_1,\dots,g_h .

Since a bus is a moving object b , a *raw bus trajectory* s of b is simply a raw trajectory generated by b . Useful strategies to segment s would be based on the bus stops of a route of the bus line, the nodes of the monitored street network, or other control points. The next section discusses this last segmentation criterion in detail.

4 SOME KEY OPERATIONS OF A TRAFFIC OBSERVATORY

This section briefly discusses the following operations: segmentation of raw bus trajectories; detection of travel time anomalies; estimation of travel time delays; and finding explanations for travel time anomalies. These operations are at the heart of the traffic observatory prototype illustrated in Section 5. Other equally important operations, such as mining traffic patterns, will not be covered due to space limitations.

4.1 Segmentation of Raw Bus Trajectories

The *real-time control points segmentation problem* is defined as follows:

- Let R be a bus route and n_1,\dots,n_k be a list of *control points* that succeed each other along R . Given a raw trajectory s , generated by a bus b which follows bus route R , segment s into $g=(g_1,\dots,g_{k-1})$, in real-time, so that g_i corresponds to the segment of s that starts in a point q_i closest to n_i and ends in a point q_{i+1} closest to n_{i+1} , for $i=1,\dots,k-1$.

The control points may be arbitrarily chosen along the bus route R , they may be the bus stops of R or they may correspond to points pre-defined in a monitored street network. However, we assume that n_i immediately precedes n_{i+1} in R , for $i=1,\dots,k-1$.

By segmenting s in *real-time* we mean that the spatial-temporal points of s are processed as a data stream, that is, at time t , the segmentation algorithm has access only to the prefix of s up to t .

There are several practical problems to take into account, such as:

- (1) The bus route associated with s may be incorrect.
- (2) GPS devices introduce errors.
- (3) The sampling interval at which the GPS points are acquired may be too long.

We assume that Problems (1) and (2) have been solved by a pre-processing step so that the bus route R is correct and all points in s fall over R .

Problem (3) deserves a separate discussion. If the sampling interval at which the GPS points are acquired is too long, or the bus is running too fast, no point in the trajectory s may correspond exactly to any of the control points. Given a control point n_i , there are at least three possible solutions: (1) select the last point q_i in s that occurs before n_i along R ; (2) select the first point r_i in s after n_i ; (3) use the timestamps of q_i and r_i to generate a timestamp u_i by interpolation

and artificially add (n_i, u_i) to s . Any of these solutions actually use route R to impose a linear order on the trajectory points together with the control points.

In the rest of this section, we briefly discuss a real-time control points segmentation strategy based on the first option, for the sake of simplicity.

Let $s = ((p_1, t_1), (p_2, t_2), \dots, (p_n, t_n))$ be a raw bus trajectory generated by a bus that follows bus route R . Assume that the points in s correctly fall over R .

Suppose that we have already processed the prefix $((p_1, t_1), (p_2, t_2), \dots, (p_i, t_i))$ of s and that (p_i, t_i) is such that p_i is the last point in s before n_i . We must discover (p_j, t_j) in s such that p_j is the last (spatial) point before n_{i+1} along R . We will then have found the desired segment g_i , which is $((p_i, t_i), \dots, (p_j, t_j))$.

To discover one such point, we associate with (n_i, n_{i+1}) a variable C , which is initially *Null*, and which will hold a pair (p_h, t_h) , where (p_h, t_h) is the last known point of s .

Let (p_k, t_k) be a new spatial-temporal point of s , that is, (p_k, t_k) is added at the end of the current prefix of s . There are two cases to consider:

1. p_k lies before n_{i+1} along R . Then, update C to (p_k, t_k) .
2. p_k lies after n_{i+1} along R . Then, (p_k, t_k) is the first point in s after n_{i+1} and the current value of C is used as the end-point of the segment that started on (p_i, t_i) .

A few comments are worth at this point. As already indicated, this segmentation strategy depends on a pre-processing step so that the bus route R that is correct and all points in s fall over R .

The real-time control points segmentation strategy can be modified to simultaneously segment a set of raw trajectories that traverse the same control points (see examples in Section 5.3) simply by replacing variable C by a hash table whose key is the bus ID.

Also, the strategy can be used to (off-line) segment a set of raw trajectories stored in a trajectory dataset. Furthermore, with minor modifications, the segmentation strategy can be transformed into a strategy to monitor buses whose routes cover a given set of control points.

4.2 Detecting Travel Time Anomalies

The *real-time travel time anomaly detection problem* is defined as follows:

- Given a street route S and a time interval T , detect in real-time if the travel time to traverse S during T is deviating from the average travel time.
An example of a time interval T would be

“Monday, August 17th, from 6:00 AM to 10:00 AM”. We also say that a time interval U , such as “Monday, August 10th from 6:00 AM to 10:00 AM”, is *consistent with* T .

We recall that both a street route S and a bus route R are paths of the street network. We say that a bus route R *matches* S iff S is a sub-path of R (this notion is needed to select bus trajectories that cross S).

Let S be a street route and assume that S starts on a node labelled with point n_i and ends on a node labelled with point n_{i+1} . Let T be a time interval. Let π be a set of trajectories that are being generated, during the time interval T , by buses that follow routes that match S .

A real-time traffic anomaly detection strategy, similar to the segmentation strategy described in Section 4.1, would go as follows:

1. Off-line, as a preparation step, obtain an estimation for the average travel time to traverse S , denoted $\bar{\tau}[S, \alpha, T, P]$, using the travel times to traverse S observed in a set α of archived trajectories, for time intervals consistent with T , over a period of time P .
2. In real-time, given a trajectory s in π , suppose that the prefix $((p_1, t_1), (p_2, t_2), \dots, (p_i, t_i))$ of s has already been processed and that (p_i, t_i) is such that p_i is the spatial point in s closest to n_i . When a point (p_k, t_k) of s is received, if $t_k - t_i > \bar{\tau}[S, \alpha, T, P]$, then the bus that is generating s is running late to reach n_{i+1} , that is, to traverse S .
3. If more than one bus, but less than Y buses are running late to traverse S , raise a *yellow semaphore* where Y is a given constant.
4. If more than Y buses are running late, raise a *red semaphore*.

The use of semaphores is justified since buses might be delayed for a number of reasons and, hence, one cannot signal that there is a travel time anomaly to traverse S at T if just one bus is running late.

4.3 Estimating Travel Time Delays

The *travel time delay estimation problem* is defined as follows:

- Given a street route S and two periods of time P_1 and P_2 , estimate the differences between the travel times to traverse S at P_1 and at P_2 .

A quite simple travel time delay estimation strategy would go as follows:

1. Select a set a_k of trajectories from a set of archived trajectories such that the trajectories match S and cover P_k , for $k=1,2$.

2. Obtain an estimation for the distribution of travel times to traverse S , denoted $\tau_k[S, \alpha_k, P_k]$, using the travel times to traverse S at P_k observed in the trajectories in α_k , for $k=1,2$.
3. Compare $\tau_1[S, \alpha_1, P_1]$ and $\tau_2[S, \alpha_2, P_2]$.

Section 5.3 provides examples of travel time delay estimations.

Finally, using travel time delay estimations, it would also be possible to estimate the number of bus passengers affected, or the total loss of time (incurred by bus passengers), if bus passenger data were available.

4.4 Finding Explanations for Travel Time Anomalies

The *explanation of travel time anomalies* problem is defined as follows:

- Given a street route S and a time interval T such that a travel time anomaly has been detected, find a traffic event that can explain the anomaly.

A strategy to address this problem involves interpreting tweets that describe traffic-related events and that are distributed by government agencies or by news agencies (blind1). Briefly, the strategy would go as follows:

1. Suppose that a travel time anomaly has been detected for a given street route S and a time interval T .
2. Use the labelling functions of the street network to find the street names of the edges that compose the street route S .
3. Search the appropriate Twitter channels to find tweets that refer to traffic events that occurred in such streets during T ; the search requires interpreting the tweets to identify street names and other traffic event details (blind1).
4. If no such tweets are found, use the street network to find the neighboring streets along street route S , up to a certain distance, and repeat Step (3).
5. Output any tweet found.

Section 5.3 provide an example of a traffic event that caused a considerable traffic time anomaly.

5 EXPERIMENTS

This section describes experiments with the traffic observatory prototype developed to test the concepts introduced in previous sections.

5.1 The Bus Network of the City of Rio De Janeiro, Brazil

The public transportation system of the City of Rio de Janeiro is largely based on buses. The statistics published for the year 2014 are the following:

- Bus lines: 716
- Number of buses: 8,916
- Number of trips: 18.5 million
- Number of passengers transported: 1,263 million
- Kilometers travelled: 760 million
- Number of companies: 44
- Number of employees: 41,375
- Average bus age: 4.06 years
- Average no. of passengers per kilometer: 1.39
- Average no. of kilometers travelled per bus per month: 7,094

Yet more expressive is the fact that buses accounted for nearly 60% of all passengers transported over the past three years.

5.2 Data Collection and Visualization

The traffic observatory prototype offers a basic data collection service that:

1. Captures the bus lines, bus routes and bus stops from the traffic authority Web site.
2. Captures, at regular interval, the raw bus GPS points from the traffic authority Web site.
3. Keeps in core the last 5 positions of each bus.
4. Stores in secondary storage all points captured, organized by day.

From June 12th, 2014 until December 1st, 2015, the service collected more than 2 billion records.

The traffic observatory prototype also offers simple visualization services that allow users to overlay bus trajectory data on top of a street map of the city:

1. The last known position of each (operational) bus.
2. The last known position of each bus, up to a 10-minute delay.
3. The last known position of each bus of a given bus line, together with the actual bus route (forward and return).
4. The last 5 positions of a specific bus, together with the actual bus route (forward and return).

In all cases, the user may obtain the data associated with a bus by passing the mouse over the icon that represents the bus.

5.3 An Example of Travel Time Delay Estimation

To illustrate what one can expect from the traffic observatory prototype, we estimate the travel time delays caused by a traffic accident that occurred in the metropolitan area of the City of Rio de Janeiro.

The accident was a fatal collision that caused the death of a motorcyclist at the Zuzu Angel Tunnel, which is part of an expressway that connects the south and the west zones of Rio. As shown in Figure 1, the accident occurred on Monday, August 17th, 2015 and took place at, approximately, latitude -22.992342 and longitude -43.249278 (near the Rocinha community in the São Conrado area).

To evaluate the impact of this event in term of travel time delays, the road segments analyzed were: Zuzu Angel Tunnel, Jardim Botânico Street and Bartolomeu Mitre Avenue, identified in Figure 1 in blue, green and red, respectively. These segments were chosen based on the (crucial) nodes, shown in Figure 1, of the monitored street network of Rio de Janeiro.

Figure 2 shows the travel time spent to traverse the Zuzu Angel Tunnel on the day of the accident versus the typical travel time pattern for the segment, mined from the archived bus trajectories, for the same day of the week (i.e., Mondays). As the graph in this figure reveals, this event caused considerable travel time delays for a crucial period of the day. The travel time delays reached a peak of nearly 30 minutes at 8:00 AM and were observed for nearly four hours, from 6:00 AM to 10:00 AM. Travel time delays were also observed throughout the Jardim Botânico Street up to the Rebouças Tunnel (indicated by top most dot in Figure 1), located 10 km from the accident site.

To conclude, this example illustrates the ability of the traffic observatory prototype to mine a trajectory dataset to uncover typical and abnormal traffic patterns for selected road segments and time periods and to compare the patterns to assess travel time delays (Figure 2 shows typical patterns in green, or light grey, and abnormal patterns in red, or dark grey).

6 RELATED WORK

The segmentation of raw trajectories may use different criteria, ranging from the transportation means used (Biljecki et al., 2013; Biljecki, 2010), potential-transition locations (e.g. bus stops) (Liao, 2006), geo-spatiotemporal information (Buchin et al., 2015; Yoon et al., 2008), detection of similar sub-trajectories (Sankararaman et al., 2013) and

movement analysis (Alewijjnse et al., 2014; Buchin et al., 2012). Section 4.1 specifically discussed how to segment row trajectories based on the passing of buses by control points.

Estimating traffic patterns from GPS data streams is an important task to improve the efficiency of traffic systems. According to (Zhang et al., 2013), traffic applications using GPS data streams can be divided into two main groups: centralized and distributed. The first group uses traffic data from multiple GPS devices simultaneously, while the second group of applications uses individual GPS data. Traffic state estimation (Geisler et al., 2012), queue profile estimation (Ramezani and Geroliminis, 2015), detection of traffic anomalies (Kuang et al., 2015) are examples of applications of the centralized applications. Applications of the second group include: vehicle performance analysis (Kargupta et al., 2010), vehicle monitoring (Jose et al., 2015), and vehicle anomaly detection (Chen et al., 2012). This paper could be classified in the first group of applications, as it analyses traffic based on multiple GPS-enabled vehicles.

Kumar et al. (2005) presented a real-time surveillance system with a rule-based behavior and event-recognition module for traffic videos. Lu et al. (2008) developed HOLMES, which is a system for highway operation monitoring and evaluation.

Concerning bus transportation, several works addressed the problem of determining the estimated time of arrival (Bullock, Jiang and Stopher, 2005; Sun et al., 2007). Kormaksson et al. (2014) presented a specific study about the City of Rio de Janeiro.

7 CONCLUSIONS

We argued that buses, equipped with active GPS devices that continuously transmit their position, can be understood as mobile traffic sensors. Indeed, bus trajectories provide a useful data source for analyzing traffic, if the city is served by a dense bus network and the city traffic authority makes the bus trajectories available openly, timely and in a continuous way.

We briefly listed the fundamental requirements for traffic observatory applications. Then, we discussed some key operations on bus trajectories. Finally, we described experiments with a traffic observatory prototype using bus trajectories made available by the traffic authority of the City of Rio de Janeiro. The results obtained corroborate the usefulness of using bus trajectories to monitor traffic.

As for future work, we are gradually increasing the functionality of the traffic observatory prototype to cover all requirements listed in Section 2.

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REFERENCES

- Albuquerque, F.C., Casanova, M.A., Lopes, H., Redlich, L.R., Macedo, J.A.F., Lemos, M., Carvalho, M.T.M., Renso, C. A methodology for traffic-related Twitter messages interpretation. *Computers in Industry*. doi: 10.1016/j.compind.2015.10.005.
- Alewijnse, S., Buchin, K., Buchin, M., Kolzsch, A., Kruckenberg, H. and Westenberg, M. 2014. A framework for trajectory segmentation by stable criteria. Proc. 22nd ACM SIGSPATIAL Int'l. Conf. on Advances in Geographic Information Systems, 351–360.
- Biljecki, F., Ledoux, H. and Van Oosterom, P. 2013. Transportation mode-based segmentation and classification of movement trajectories. *Int'l. J. of Geographical Information Science*, Vol. 27, No. 2, 385–407.
- Biljecki, F. 2010. Automatic segmentation and classification of movement trajectories for transportation modes. TU Delft, Delft University of Technology.
- Buchin, M., Driemel, A., van Kreveld, M. and Sacristan, V. 2015. Segmenting trajectories: A framework and algorithms using spatiotemporal criteria. *J. Spatial Information Science*, No. 3, 33–63.
- Buchin, M., Kruckenberg, H. and Kolzsch, A. 2012. Segmenting trajectories based on movement states. Proc. 15th Int'l. Symp. Spatial Data Handling (SDH), 15–25.
- Bullock, P., Jiang, Q., Stopher, P. R. 2005. Using GPS technology to measure on-time running of scheduled bus services. *Journal of Public Transportation*, Vol. 8, No. 1, p. 21–40.
- Chen, C., Zhang, D., Castro, P. S., Li, N., Sun, L., and Li, S. 2012. Real-time detection of anomalous taxi trajectories from GPS traces. *Mobile and Ubiquitous Systems: Computing, Networking, and Services*, 63–74.
- Geisler, S., Quix, C., Schiffer, S., and Jarke, M. 2012. An evaluation framework for traffic information systems based on data streams. *Transportation Research Part C: Emerging Technologies*, Vol. 23, 29–55.
- Sunil, N., Ajinkya, V., Swapnil, C., and Vyankatesh, B. 2014. Dynamic bus timetable using GPS. *Int'l. J. of Advanced Research in Computer Engineering & Technology*, Vol. 3, No. 3.
- Jose, D., Prasad, S., and Sridhar, V. 2015. Intelligent vehicle monitoring using global positioning system and cloud computing. *Procedia Computer Science*, Vol. 50, 440–446.
- Kargupta, H., Sarkar, K., and Gilligan, M. 2010. Minefleet R : An overview of a widely adopted distributed vehicle performance data mining system. Proc. 16th ACM SIGKDD Int'l. Conf. Knowledge Discovery and Data Mining, 37–46.
- Kormaksson, M. et al. 2014. Bus Travel Time Predictions Using Additive Models. Proc. 2014 IEEE Int'l. Conf. on Data Mining (ICDM), 875–880.
- Kumar, P. et al. 2005. Framework for real-time behavior interpretation from traffic video. *IEEE Trans. On Intelligent Transportation Systems*, Vol. 6, No. 1, 43–53.
- Kuang, W., An, S., and Jiang, H. 2015. Detecting traffic anomalies in urban areas using taxi GPS data. *Mathematical Problems in Engineering*, 501:809582.
- Liao, L., Patterson, D.J., Fox, D. and Kautz, H. 2006. Building personal maps from GPS data. *Annals of the New York Academy of Sciences*, Vol. 1093, No. 1, 249–265.
- Lu, C.-T. et al. 2008. Homes: highway operation monitoring and evaluation system. Proc. 16th ACM SIGSPATIAL Int'l. Conf. on Advances in Geographic Information Systems., 85.
- Ramezani, M. and Geroliminis, N. 2015. Queue profile estimation in congested urban networks with probe data. *Computer-Aided Civil and Infrastructure Engineering*, Vol. 30, No. 6, 414–432.
- Sankararaman, S., Agarwal, P. K., Molhave, T., Pan, J. and Boedihardjo, A.P. 2013. Model-driven matching and segmentation of trajectories, Proc. 21st ACM SIGSPATIAL Int'l. Conf. on Advances in Geographic Information Systems, 234–243.
- Shi, W., Kong, Q.-J., and Liu, Y. 2008. A GPS/GIS integrated system for urban traffic flow analysis. Proc. 11th Int'l. IEEE Conf. on Intelligent Transportation Systems, 844–849.
- Sun, D. et al. 2007. Predicting Bus Arrival Time on the Basis of Global Positioning System Data. *Transportation Research Record*, Vol. 2034, No. 1, 62–72.
- Yoon, H. and Shahabi, C. 2008. Robust time-referenced segmentation of moving object trajectories. Proc. 8th IEEE Int'l. Conf. on Data Mining, 1121–1126.
- Zhang, J.-D., Xu, J., and Liao, S. S. 2013. Aggregating and sampling methods for processing GPS data streams for traffic state estimation. *IEEE Trans. on Intelligent Transportation Systems*, Vol. 14, No. 4, 1629–1641.
- Zhu, B. and Xu, X. 2015. Urban principal traffic flow analysis based on taxi trajectories mining. *Advances in Swarm and Computational Intelligence*, 172–181.

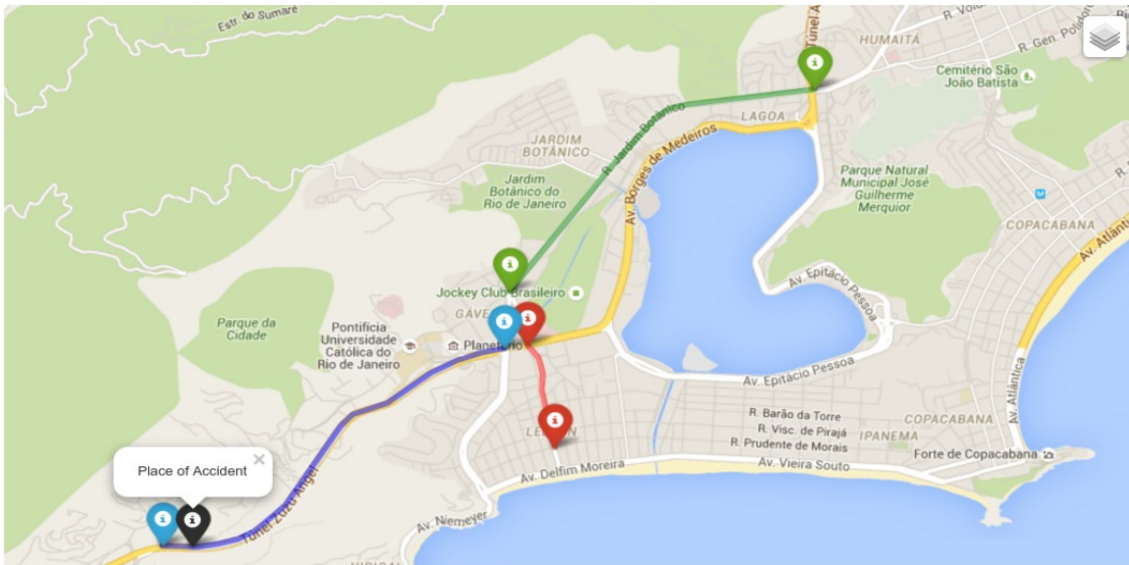


Figure 1: Place of the accident.

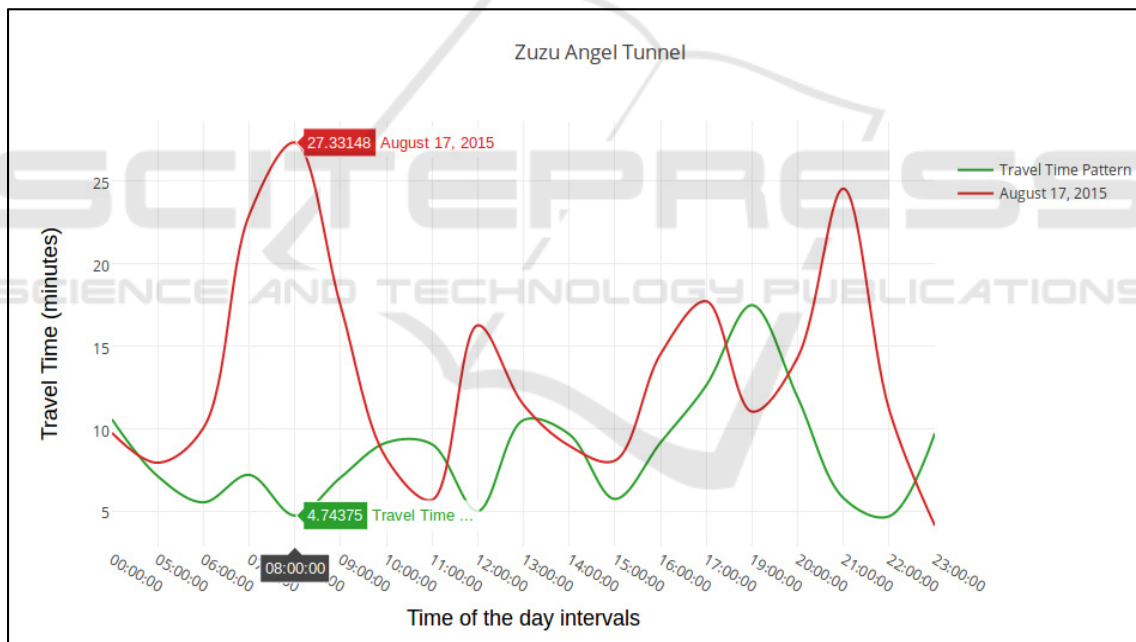


Figure 2: Travel Time Pattern vs Travel Time at the day of accident – Zuzu Angel Tunnel.