

# Multi-agent based Synchronous Communication for Dynamic Rescheduling in Railway Network

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**Keywords:** Message Passing, DCOP, Multi-agent based Modeling, Selective Flooding.

**Abstract:** This paper presents a multi-agent based solution to change a predefined Railway schedule dynamically. This paper models a railway network consisting of passenger and freight trains, along with their fixed schedules following the rules of Indian Railways. The trains in the system are modelled as Train Agents and rail segments as Segment Agents. Delay of a single train due to unavoidable hazards like track related problems, rain, fog may cause severe delays for next trains in sequence. This paper proposes a method to suggest overtaking maneuvers for trains by passing different types of messages between Train Agents and Segment Agents. This paper proposes Selective Flooding of messages to avoid congestion overhead. All types of messages passed are elaborately described in the problem formulation section. This paper also contains a theoretical proof showing that Selective Flooding technique is always able to reach every node required. The proposed method has been simulated using JADE platform and the results are presented.

## 1 INTRODUCTION

Creation of optimal timetable for Railway Network and introducing new train according to requirement are time consuming processes for the countries where Railway Network is maintained manually. Most of the research works done on railway scheduling have focused on creating optimal timetable that maintains the constraints provided by the railway operators. Apart from optimizing the schedule there are other issues that should be taken care of. Some dynamic strategies should be there to handle unavoidable hazards that may occur in railway network. Schedule of a train can be affected by unpredictable delay due to meteorological conditions such as rain, fog or track related issue. This paper aims to implement the robustness feature along with the optimal timetable so that delay of one passenger or freight train can not affect others severely. In Indian Railways freight trains generally do not have any fixed schedule. So, on demand scheduling should be there to handle freight trains along with passenger trains. During last few years distributed approaches of solving any real time problem have been admired rather than centralized approach. To take the rescheduling decision dynamically multiple autonomous entities or Agents can be introduced to solve the issues stated above.

The main focus of this work is to model N-track

railway network in which passenger and freight trains are scheduled and rescheduled dynamically with the notion of Distributed Constraint Optimization Problem (DCOP). Each train and segment acts as an autonomous agent (termed as Train Agent and Station Agent). Based on different types of delay objective functions are formed depending on certain constraints related to Indian Railways. The agents communicate among themselves to find a way out when disturbance occurs. The total procedure of sharing, updating, taking decisions are properly stated in proposed algorithm.

## 2 RELATED WORK

Authors of (Takeuchi et al., 2007) have used Monte Carlo technique to calculate robustness index that represents passengers disutility when delay occurs. Authors of (Liebchen et al., 2010) have shown five possible types of activities and tried to minimize the objective function which considers different kinds of delay associated to each activity along with number of passengers on the train. Space graph strategies were proposed in (Cacchiani and Toth, 2012) where four different arcs starting, segment, station, ending are used and each arc has initial profit. If global profit of any train becomes NULL or negative train cancellation is

allowed. Authors of (Fischetti and Monaci, 2009) have proposed a light robustness technique which is flexible to allow the violation of constraints while imposing a maximum efficiency loss. Authors of (Cicerone et al., 2009) have measured price of robustness by the ratio between recoverable robust timetable and the optimal non-robust solution. They have shown that problem of finding optimal recoverable robust timetables is NP-hard. Authors of (Sahana et al., 2014) have proposed ant colony based optimization for solving scheduling problem for train having same speed and for different speed also. But they have not focused on unpredictable delay. Genetic Algorithms proposed by (Tormos et al., 2008) and (Chung et al., 2009) are appropriate methods to explore the search space of this complex problem but they have not considered the robustness related issue. In (Kiekintveld et al., 2010) authors have proposed k-distance optimality using Subset Locking and Partial Synchronization. Bipartite factor graph is used in (Farinelli et al., 2008) for sending messages. (Kuo et al., 2010) contains a process to schedule freight train dynamically. Agent based approach for modeling domain dependent constraint satisfaction problem has been shown in (Salido et al., 2007).

### 3 SCOPE OF THE WORK

In case of railway scheduling most of the research papers focused on creating optimal timetable that maintains the constraints provided by the railway operators. Using different objective functions they have tried to solve Railway scheduling problem where delay management problem has not been addressed properly. This paper considers a railway network of passenger and freight trains along with a given timetable. If a train becomes affected by severe delay the predefined schedule becomes inefficient. The aim of this paper is to take dynamic overtaking decision to improve robustness of overall Railway Network. Implementation of robustness feature which maintains the overall system utility is a good scope to work on. In some cases overtaking should be allowed without violating the hard constraints. But there are also such scenarios where change of ordering bring more devastating result. This paper identifies the utility for both of the cases and takes a decision.

## 4 SYSTEM MODEL

All possible types of junction points (where trains can change their track) are not considered in this pa-

per. Alternatively junction points are assumed to be present at the both end of each station. So, signal points are available only before entering and exiting each station. The portion of railway track between two consecutive signal points is called segment. Gallop train does not stop at those stations where it has no commercial stop.

$SEG_j$  is ordered set of segments that train  $j \in N \cup M$  has to cover.  $S_j$  is ordered set of stations from originating station to final destination of train  $j \in N \cup M$ .

$N$  = Set of all passenger trains.

$M$  = Set of all freight trains.

$SEG$  = Set of all segments.

$ET_j$  is ordered set of all events that a train  $j \in N \cup M$  has to go through.  $ln_j$  is the last event of set  $ET_j$ .

$N.S_j$  is the set of stations where train  $j \in N$  has commercial stop.

$ES_k$  is ordered set of all events that are scheduled to occur at segment  $k \in SEG$ . Each event in  $ES_k$  on segment  $k$  has originating point  $OP_k$  and finishing point  $FP_k$  where  $OP_k, FP_k \in SEG_k$ .  $ln_k$  is the last event of  $ES_k$ .

If  $v$  and  $v'$  are two same directional events of segment  $k$ , then  $OP_v = OP_{v'}$  and headway distance  $\Delta_{same} = |x_v^{end} - x_{v'}^{beg}|$

$UT_k$  and  $DT_k$  are set of up tracks and down tracks of segment  $k$ .

$U^{old}$  is the overall system utility if overtaking is not granted,  $U^{new}$  is the new utility if overtaking request is granted.

### 4.1 Binary Functions

$$ADJ(i, k) = \begin{cases} 1, & \text{if segment } i, k \text{ is adjacent.} \\ 0, & \text{otherwise.} \end{cases}$$

$$UP(k, i) = \begin{cases} 1, & \text{if } k \text{ is towards up from } i. \\ 0, & \text{otherwise.} \end{cases}$$

$$DOWN(k, i) = \begin{cases} 1, & \text{if } k \text{ is towards down from } i. \\ 0, & \text{otherwise.} \end{cases}$$

$$LOOP(k) = \begin{cases} 1, & \text{if segment } k \text{ has a loop line.} \\ 0, & \text{otherwise.} \end{cases}$$

$$FREE(l_k) = \begin{cases} 1, & \text{if track } l \text{ of } k \in SEG \text{ is free.} \\ 0, & \text{otherwise.} \end{cases}$$

$$REC(msg) = \begin{cases} 1, & \text{if } msg \text{ has been received.} \\ 0, & \text{otherwise.} \end{cases}$$

$$PREC(v, v') = \begin{cases} 1, & \text{if event } v \prec v' \text{ in schedule.} \\ 0, & \text{otherwise.} \end{cases}$$

## 4.2 Train Agent and Segment Agent

Each segment consists of one Segment Agent (SA) that maintains all records of that particular segment and communicate with other SAs and Train Agents. Each of the passenger and freight trains consist of one Train Agent (TA) which can communicate only with 3 segments- current, previous and next. We are avoiding the communications among different TAs to reduce communication hazard.

$\forall$  event  $\in ET_j$ , Train Agent  $j$  stores the  $FT_j$ . Number of event in  $ET_j$  is equal to the number of segments to cross.  $\forall$  event  $\in ES_k$ , Segment Agent  $k$  stores *finish\_time* and *start\_time* as per predefined schedule. actual start and finishing time are  $ST_j, FT_j$ .

## 4.3 Directions and Fields of Messages

Direction of messages			
Message type	SA to TA	SA to SA	TA to SA
ARR	no	no	yes
LINK_PROB	no	yes	no
DEPT	no	yes	no
REQ	no	yes	no
WAIT	yes	yes	no
GRANT	yes	yes	no
OT_RQ	no	yes	no
OT_GRANT	yes	yes	no
TH_UTIL	no	no	yes

Two functions send() and receive() are used to send and receive messages. Fields of different messages are as follows.

ARR(*train, track, prevSA, nextSA, currentSA, time*)

LINK\_PROB(*segment, track, tolerance, flag*)

DEPT(*train, track, time*)

REQ(*train, track, sender\_segment*)

WAIT(*train, segment, loopline*)

GRANT(*train, segment, free\_track*)

OT\_RQ(*train\_behind, train\_heading, requesting\_SA, time, count, U<sup>old</sup>, U<sup>new</sup>*)

OT\_GRANT(*train, green\_signal*)

TH\_UTIL(*train, U<sub>Thj</sub>*)

## 5 METRIC DEFINITION

Here is a list of metrics to calculate the delay factor that helps the agents to take decisions. All of the

utility factors have negative impact and have a range [0, 1].

- Utility of delay of freight train  $j$  ( $U_{\delta_{fj}}$ ): According to Indian Railways departure of a freight train from originating point is officially decided at least before 3 hours of departure. So we can assume freight trains do not have fixed schedule. They have deadlines to reach at the final destination and almost fixed route to follow.
- Utility of arrival at commercial stop ( $U_{\delta_{aj}}$ ): For passenger trains arrival delay is calculated at each commercial stop except the originating station. If a passenger train has reached all the commercial stop on time except one stop, then also it can not have the best utility 0.
- Utility of delay of departure from commercial stop ( $U_{\delta_{dj}}$ ): Our proposed method calculates this utility at each commercial stop except the final destination of passenger train.
- Threshold delay ( $U_{Thj}$ ): This threshold utility calculation is done for each passenger train at the final station.

## 6 PROBLEM FORMULATION

This paper does not concentrate on adding a new train in the schedule or creating a optimal timetable from the scratch. The main concern of this paper is to reschedule some predefined events ( $ES$ ) so that overall system performance does not downgrade too much. There is already a fixed predefined schedule given for each and every train  $j \in M \cup N$ . Each SA (let  $k$ ) contains information about which train is scheduled to cross it in form of  $ES_k$  along with start time  $ST_i$  and  $FT_i$  where  $i \in ES_k$ .

### 6.1 Delay Measurement

#### 6.1.1 Delay Measurement for Freight Train

For freight train there is prior knowledge about the deadline. Initial utility is 0 and maximum value of utility can be reached when  $(\Delta t_j \times \frac{1}{t_{d_j} - t_{e_j}}) \times p_j$  becomes 1 for freight train  $j$  where,

$\Delta t_j$  = total delay of freight train  $j$ .

$t_{d_j}$  = deadline for freight train  $j$ , where  $t_{d_j} > t_{e_j}$ .

$t_{e_j}$  = expected finish time for freight train  $j$ .

$p_j$  = priority of train  $j$ . For higher priority train (containing special goods) must reach at final stop within time. So, for them  $p_j = 1$ . They suffer maximum negative weightage when  $\Delta t_j \leq t_{d_j} - t_{e_j}$ .

But lower priority train may some relaxation on their deadline by assigning  $p_j$  value less than 1.

$$U_{\delta_{f_j}} = \min((\Delta t_j \times \frac{1}{t_{d_j} - t_{e_j}}) \times p_j, 1) \quad (1)$$

### 6.1.2 Delay Measurement for Arrival

No credit is given to a passenger train for early arrival ( $arrive\_delta_{ji} = 0$ ) at it's commercial stop . If a train arrives early that means it has to wait more at station and thus free platform resources decrease. Arrival time delay generally affects the utility of the train itself. Suppose, a train  $j$  delays  $arrive\_delta_{ji}$  to arrive at station  $i$  and  $jrny\_time_j$  is scheduled journey time of train  $j$  from originating station to final destination, then utility for a single train  $j$ ,

$$U_{\delta_{a_j}} = \min(\sum_{i=1}^{|N_{S_j}|} (arrive\_delta_{ji}/jrny\_time_j), 1) \quad (2)$$

### 6.1.3 Delay Measurement for Departure

Departure of a passenger train can't be allowed before predefined scheduled. On the other hand departure time delay affects the following train in sequence. Arrival time and Departure time delay are measured at each scheduled commercial stop. Suppose, a train  $j$  delays  $dept\_delta_{ji}$  before leaving station  $i$ , then utility for a single train  $j$ ,

$$U_{\delta_{d_j}} = \min(\sum_{i=1}^{|N_{S_j}|} (dept\_delta_{ji}/jrny\_time_j), 1) \quad (3)$$

### 6.1.4 Threshold on Delay

Depending on the priority, each of the passenger trains has certain level of delay threshold.  $Th_j$  indicates the maximum tolerable delay of train  $j$  in arrival time at the final destination.

$$U_{Th_j} = \max(\lfloor (r\_time_j - jrny\_time_j)/Th_j \rfloor, 0) \quad (4)$$

where,  $r\_time_j$  is the actual journey time of train  $j$ . As the worst value of threshold utility is 1 at the final station when train exceeds threshold delay. So, if a train is being delayed beyond its threshold permit it can not be reflected in the objective functions. A restriction must be there to save a lower priority train to be a victim of huge delay. A train  $j$  can suffer from a huge delay if following trains in sequence are allowed to overtake train  $j$  to minimize their delay. Always aiming for the betterment of overall system is impractical, if a particular train is suffering from too much delay. To avoid this starvation problem we must introduced a

constant  $OT_j$  for each of the train  $j$  that indicates how many train can overtake  $j$  during its whole journey.

The cost associated to deviation from actual arrival and departure time of passenger train and violation of deadline by freight can be measured by following objective function:

$$\min(\sum_{j=1}^{|M|} U_{\delta_{f_j}} + \sum_{j=1}^{|N|} U_{\delta_{a_j}} + \sum_{j=1}^{|N|} U_{\delta_{d_j}} + \sum_{j=1}^{|N|} U_{Th_j}) \quad (5)$$

## 6.2 SA - SA Communications

Segment  $k$  sends *LINK\_PROB* message to the adjacent segments if there is a problematic track in segment  $k$ . If a train is delayed by problem in certain track there is no logic to go for overtaking. If a hazard is there in a particular segment, it affects all of the train in same direction. Initially  $\Delta\_allowed_{kl}$  is reset to 0. It gets some positive value in presence of any track error in the Railway Network. Algorithm 1 describes the steps followed by sender of *LINK\_PROB* message. If a problem occurs in the UP link then sender SA sends message only to adjacent UP SA. Receiver SA repeats this process using Algorithm 2 and updates  $\Delta\_allowed_{kl}$  accordingly. If the problem occurs in DOWN link rather than UP link same processes are followed up towards DOWN direction.

## 6.3 TA - SA Communications

As TA is mobile entity, critical decisions should not depend on communication involving TA. Most of all types of signaling decisions are taken depending on the SA to SA communication. TA asks each segment before entering into that whether it is meeting the entry criteria.

When a freight train  $i \in M$  is about to enter a segment having loop line the SA must check whether following passenger train  $j \in N$  needs to overtake  $i$  as described in Algorithm 4. Overtaking can be scheduled in following three cases:

- The freight train was already scheduled to wait at the loop line.
- There is a  $j$  behind freight train  $i$  where  $j$  is supposed to be in front of  $i$ . For some reason  $j$  is suffering from delay.
- $i$  is suffering from delay and there is a following passenger train  $j$  running on time. So, there should a procedure to pass that passenger train  $j$  by make  $i$  waiting in the loop line.



## 6.4 Overtaking Decision

If a train is late for more than  $\Delta_{allowed_{kl}}$  at segment  $k$  and still not getting free slot or green signal for entering next segment, the segment  $k$  sends *OT\_REQ* message to the next segment in sequence. If priority of train  $i$  is less than the preceding train  $j$ ,  $i$  is not allowed to overtake train  $j$  unless it is a prescheduled overtaking. Otherwise overtaking decision can be taken after following conditions are satisfied.

### 6.4.1 Recalculate Objective Function Value

If a train  $i$  overtakes train  $j$ ,  $i$  needs an extra time of  $\Delta_{cross_{ij}}$  and  $j$  needs an extra time of  $\Delta_{cross_{ij}} + \delta_{ij}$  (line 5 of Algorithm 7).  $\Delta_{cross_{ij}}$  depends on how much time train  $i$  takes to change the track and gets back to the previous track after overtaking  $j$ . In real scenario  $\Delta_{cross_{ij}}$  is not constant. But we are assuming it as a constant for a particular railway network as 'how to optimally change track at junction point' is not main concern of this paper.  $\delta_{ij}$  depends on how much time train  $j$  takes to regain its original speed after getting back to its own track in addition with the time taken by train  $i$  to cross the headway distance  $\Delta_{same}$ . We are not considering  $\delta_{accelerate_i}$  (time required to accelerate and get back the normal velocity  $V_i$ ), as it is already included in  $\Delta_{cross_{ij}}$ .  $\delta_{ij} = \delta_{accelerate_j} + \Delta_{same}/V_i$ .

Objective function value can be recalculated properly considering the whole route of two trains. The technique is optimal for betterment of threshold utility. But to decrease arrival and departure delay at each segment we must take Zonal decision. Indian Railway uses Zonal management and decision strategy manually. Our proposed technique reflects the existing policy. In Zonal decision strategy objective function value is recalculated up to a constant number of segments.

### 6.4.2 Check for Feasibility

If overtaking is not feasible due to unavailability of free slots for overtaking, rescheduling decision should not be finalized. To check the rescheduling feasibility we are following almost same strategy as described by author of (Dalapati et al., 2014). But unlike (Dalapati et al., 2014) SA does not contain all information in our proposed method. So, SA needs to communicate with other SAs and TAs to calculate objective function. In this paper all segments towards destination segment are considered and each SA  $k$  updates event list  $ES_k$  after finalizing the rescheduled overtaking. The event list of all TA remain unchanged

as each train is following the order in which they are supposed to cross the segments.

## 6.5 Message Passing

When a TA enters a segment it sends *ARR* using Algorithm 3. On receiving *ARR* using Algorithm 6, the SA sends the followings

- *REQ* to the next SA in sequence.
- *DEPT* to the previous segment.
- Overtaking request *OT\_REQ* if required.

After receiving *DEPT* using Algorithm 5, SA calculates  $U_{\delta_{d_j}}$  and set the track free. On receiving *REQ* the SA sends followings according to Algorithm 4

- *GRANT* to SA and TA when track is free.
- *WAIT* to both of SA and TA.

Line 9 and 10 of Algorithm 4 create a loop if there is no free track. The loop breaks immediately when a track becomes available. On receiving *GRANT* and *WAIT* the SA provides proper signal to TA using Algorithm 5. An extra security is provided by Algorithm 8 as TA also receives *WAIT* and *GRANT* along with traditional signal. Algorithm 7 describes the method to check the requirement and feasibility of overtaking and send *OT\_GRANT* which is received by Algorithm 5. In Algorithm 7 Zonal decision is taken within next 10 segments (line 6,7). The segment comes after 10th segment takes the final decision depending on received  $U^{old}$  and  $U^{new}$ .

## 6.6 Selective Flooding of LINK\_PROB

After detecting the link related problem *LINK\_PROB* message is required to be sent to other Segment Agents. The naive approach is to inform all Segment Agents in the railway Network. But to reduce message passing complexity and avoid broadcast storm problem, Selective Flooding can be introduced. In Selective Flooding technique the messages are sent to selective Segment Agents. Algorithm 1 and Algorithm 2 describe the procedure how Segment Agents are selected from the total set of segments *SEG*.

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Algorithm 1: SA detects track related problem.

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- 1:  $k \leftarrow$  ID of SA where problem occurs at Track  $l$
  - 2:  $tol \leftarrow$  predicted delay of crossing track  $k$
  - 3:  $\Delta_{allowed_{kl}} \leftarrow (\Delta_{allowed_{kl}} + tol)$
  - 4: for  $i \in SEG$  do
  - 5:   if  $(l \in UT_i)$  then
  - 6:     if  $(ADJ(i, k) = 1 \wedge DOWN(k, i) = 1)$  then
  - 7:       send (*LINK\_PROB*( $k, l, tol, 1$ ),  $i$ )
  - 8:     else if  $(ADJ(i, k) = 1 \wedge UP(k, i) = 1)$  then
  - 9:       send (*LINK\_PROB*( $k, l, tol, 0$ ),  $i$ )
-

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Algorithm 2: On receiving  $LINK\_PROB(segment, track, tol, flag)$  message by SA from other SA.

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```

1: receive ( $LINK\_PROB(k, l, tol, flag)$ )
2:  $i \leftarrow$  ID of receiving SA
3:  $\Delta\_allowed_{il} \leftarrow (\Delta\_allowed_{il} + tol)$ 
4: if ( $flag = 1$ ) then
5:   for  $i \in SEG$  do
6:     if ( $ADJ(i, k) = 1 \wedge DOWN(k, i) = 1$ ) then
7:       send( $LINK\_PROB(k, l, tol, 1), i$ )
8:     else if ( $ADJ(i, k) = 1 \wedge UP(k, i) = 1$ ) then
9:       send ( $LINK\_PROB(k, l, tol, 1), i$ )

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Algorithm 3: On arriving of TA  $j$  at track  $l$  of segment  $sc$  at time  $t$ .

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1: send ( $ARR(j, l, sp, sn, t), sc$ )
2:  $FT_{sc} \leftarrow t$ 
3: if ( $sc = ln_j$ ) then
4:   calculate  $U_{Th_j}$  using Equation 4
5:   send ( $TH\_UTIL(j, U_{Th_j}), sc$ )

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Algorithm 4: On receiving  $REQ(train, track, sender segment)$  message by SA  $k$  from other SA.

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1: receive( $REQ(j, l, s)$ )
2: if ( $j \in M$ )
3:   calculate  $U_{\delta_{fj}}$  using Equation 1
4:   if ( $REC(OT\_RQ, j') = 1 \wedge PREC(j, j') = 1 \wedge j' \in N \wedge LOOP(k) = 1 \wedge FREE(lt_k) = 1$ )
5:     send( $WAIT(j, k, lt_k), s$ )
6:     send( $WAIT(j, k, lt_k), j$ )
7:      $FREE(lt_k) \leftarrow 0$ 
8:     EXIT
9: if  $\forall l' \in UT_k \cup DT_k$ , connected to  $l$  and  $FREE(l') = 0$ 
10:   go to line 9
11:  $FREE(l') \leftarrow 0$ 
12: send( $GRANT(j, k, l'), s$ )
13: send( $GRANT(j, k, l'), j$ )

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**claim:** *The Selective Flooding technique described by Algorithm 1 and Algorithm 2 covers sufficiently large portion of network and the unaware SAs do not require this LINK\_PROB message from segment  $k$ .*

**Proof:** In figure 1  $k$  is an arbitrary segment among a set of segments represented by nodes. A joining arc connecting two segments represents suitable entry and exit criteria of the connecting segments. The triangle( $T$ ) shaped segments indicate the UP segments with respect to segment  $k$  and square( $S$ ) shaped segments represent DOWN segments with respect to  $k$ . The round white( $RW$ ) segments are not sharing any route with segment  $k$ . According to Indian railway a train can be either UP or DOWN directed. If a train has a route that consist of UP directed route followed by a Down directed route, Indian railway uses two

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Algorithm 5: On receiving  $DEPT(j, l, t)$ ,  $GRANT(j, k, l')$ ,  $WAIT(j, k, lt_k)$ ,  $OT\_GRANT(j, g)$  message by SA from SA.

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```

1:  $msg \leftarrow$  receive()
2: if ( $type(msg) = DEPT$ ) then
3:    $FT_j \leftarrow t$ 
4:    $dept\_delta_{ji} \leftarrow (FT_j - finish\_time_j)$ 
5:   if ( $i \in N\_S_j$ ) then
6:     calculate  $U_{\delta_{aj}}$  using Equation 3
7:    $FREE(l) \leftarrow 1$ 
8: else if ( $type(msg) = GRANT$ ) then
9:   send green signal to  $j$  to enter track  $l'$  of segment  $k$ 
10: else if ( $type(msg) = WAIT$ ) then
11:   send signal to  $j$  to enter loop track  $lt_k$  of segment  $k$ 
12: else if ( $type(msg) = OT\_GRANT$ ) then
13:   if ( $g=1$ ) then
14:     check feasibility by sending  $REQ$  to  $sn$ 
15:     else
16:       Stop train  $j$  and wait for  $REQ$ 

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Algorithm 6: On receiving  $ARR(train, track, previousSA, nextSA, currentSA, time)$  message by SA  $i$  from TA  $j$ .

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```

1: receive ( $ARR(j, l, sp, sn, t), sc$ )
2: send( $DEPT(j, l, t), sp$ )
3:  $s \leftarrow i$ 
4: send( $REQ(j, l, s), sn$ )
5:  $ST_j \leftarrow t$ 
6:  $arrive\_delta_{ji} \leftarrow ST_j - start\_time_j$ 
7: if ( $i \in N\_S_j$ ) then
8:   calculate  $U_{\delta_{aj}}$  using Equation 2
9: if  $j \in N$  then
10:   if ( $(\Delta\_allowed_{ij} < arrive\_delta_{ji}) \wedge GRANT$  message not received from  $sn$ ) then
11:     send( $OT\_RQ(j, 0, i, t, 0, 0, 0), sn$ )

```

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different numbers of the train for two different directions. So, logically each train can have only one direction. We categorize all segments into 3 sets ( $S, T, RW$ ) from the perspective of segment  $k$ . According to proposed formulation for  $i \in S$ ,  $UP(k, i)$  function returns 1, for  $i \in T$ ,  $DOWN(k, i)$  returns 1 and for  $i \in RW$  both functions returns 0 .

Suppose segment  $k$  finds a problem in UP track and it informs the adjacent segments towards UP direction. Let us assume that there be a segment  $kt \in T$  so that  $DOWN(k, kt) = 1$  and  $kt$  does not receive  $LINK\_PROB$  initiated by segment  $k$ . If  $kt$  does not receive  $LINK\_PROB$  that means there is no segment  $i \in T \setminus k, kt$  such that line 6 of Algorithm 2 is satisfied. As railway network is connected graph there must be a path from  $k$  to  $kt$ . As  $i \in T$ , the existing path from  $k$  to  $kt$  must be completely UP directed. So, second condition in line 6 of Algorithm 2 is true  $\forall i \in T$ . If there is  $n$  nodes in between  $k$  to  $kt$  (let  $i_1, i_2 \dots i_n$ ), then  $DOWN(k, i_1) = 1, DOWN(i_1, i_2) = 1 \dots DOWN(i_{n-1}, i_n) = 1$  and  $DOWN(i_n, kt) = 1$ . So,

Algorithm 7: On receiving  $OT\_RQ(trainbehind, trainheading, requestingSA, time, count, U^{old}, U^{new})$  message by SA from other SA.

```

1: receive( $OT\_RQ(j, j', s, t, c, x, y)$ )
2: if ( $j \notin ES_k$ ) // the SA who do not have  $j$  as event
3:   EXIT
4:  $U^{old} \leftarrow (U_{jk}^{old} + U_{j'k}^{old} + x)$ 
5: calculate  $U^{new}$  considering  $\Delta\_cross_{ij} + \delta_{ij}$  using  $t$ 
6: if ( $c \leq 10$ ) then //restricting zonal decision
7:    $c \leftarrow c + 1$ 
8:   if ( $UP(k, s) = 1$ ) then
9:     for  $\forall k' \in SEG \wedge ADJ(k, k') \wedge UP(k, k')$ 
10:      send( $OT\_RQ(j, j', s, t, c, U^{old}, U^{new}), k'$ )
11:   else
12:     for  $\forall k' \in SEG \wedge ADJ(k, k') \wedge DOWN(k, k')$ 
13:      send( $OT\_RQ(j, j', s, t, c, U^{old}, U^{new}), k'$ )
14: else
15:   calculate Objective function using Equation 5
16:   if (new value of objective function is minimum)
17:     send( $OT\_GRANT(j, 1, s)$ )
18:     send( $OT\_GRANT(j', 0, sn)$ )

```

Algorithm 8: On receiving  $GRANT(j, k, l')$  or  $WAIT(j, k, lt_k)$  message by TA from SA.

```

1:  $msg \leftarrow receive()$ 
2: if ( $type(msg) = GRANT$ ) then
3:   enter segment  $k$  using track  $l'$ 
4: else if ( $type(msg) = WAIT$ ) then
5:   wait at loop line  $lt_k$  of segment  $k$ 

```

Algorithm 2 guarantees delivery of  $LINK\_PROB$  to each node  $i \in T$  except the following situation.

If all nodes in  $T$  are adjacent of  $k$ , then 2nd condition of line 6 of Algorithm 2 becomes false. In that case Algorithm 1 guarantees delivery of  $LINK\_PROB$  message to all of the adjacent nodes of  $k$ . So our assumption was wrong and we conclude that all nodes in set  $T$  receive the message.

## 7 EXPERIMENT AND RESULTS

As depicted in Figure 2 a small Railway Network is considered which consists of 26 segments (among them 13 segments are stations) along with 10 passenger trains and 3 freight trains. The longest  $jrny\_time$  is of 180 minutes. Segment and Train Agents are created using JADE<sup>1</sup> (Java Agent Development Framework) where different types of messages are created by different formatives of ACL message. In our simulation 7 different types of abnormal delay (hazards) are created randomly at different segments.

<sup>1</sup><http://jade.tilab.com/>

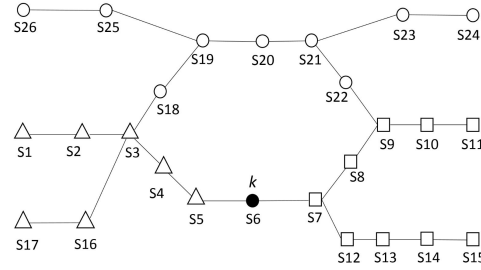


Figure 1: Segments towards UP and DOWN from SA  $k$ .

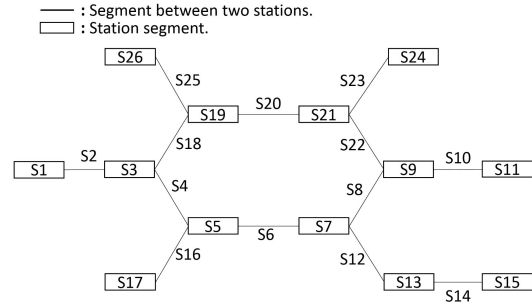


Figure 2: Railway Network having 13 stations.

### 7.1 Delay Handling

Figure 3 shows simulation result where our proposed method restricts the delay from being severe. It is obvious that the overtaking of trains takes some additional time, but that helps to minimize the delay as shown Figure 3. Delay cannot be minimised too much as maximum journey time is too small in our simulation environment (only 180 minutes). In case of a real time scenario (having long  $journey\_time$ ) the delay can be reduced a lot by speeding up the affected train after overtaking. In case of hazard number 6 our algorithm does not provide better result as it is track related issue as described in algorithm 1. If a track is in problematic state then overtaking is illogical.

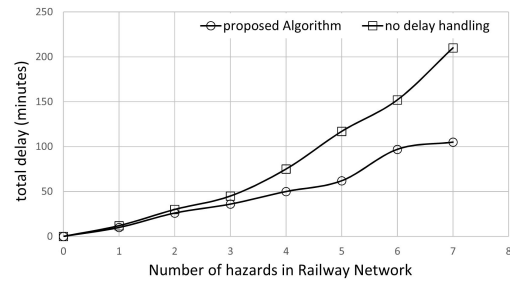


Figure 3: Overall delay comparison.

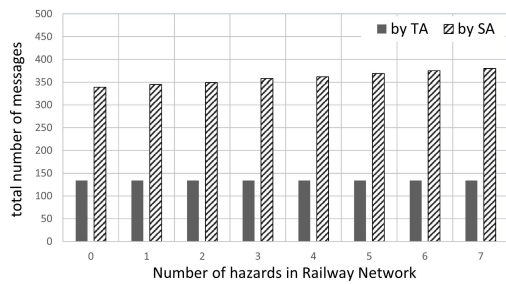


Figure 4: Summary of message passing.

## 7.2 Communication Overhead

Each TA sends two types of messages - *ARR* and *TH\_UTIL*. During any type of hazard TA need not to send any extra message. So according to figure 4 the number of messages sent by all Train Agents remains same irrespective of number of hazards occurred. Each Segment Agent sends 7 types of messages. Number of messages *REQ*, *DEPT*, *WAIT* and *GRANT* remains unchanged irrespective of number of hazards. But number of *OT\_GRANT*, *OT\_REQ*, *LINK\_PROB* messages changes depending on the number and type of hazards. As shown in Figure 4 number of messages sent by all Segment Agents is not increased a lot with the increase of number of hazards.

## 8 CONCLUSION

With the increase in number of trains and tracks in Indian Railways, the on demand scheduling task becomes time consuming. As per the case study it is evident that Multi-agent based approach described in this paper has promising aspects for taking dynamic decision more accurately. As Railway Network graph is not too much complex as complete graph, no preprocessing is required like other DCOP algorithms like (Petcu and Faltings, 2005) and (Modi et al., 2005). It is a major advantage to have additional time for multi-agent communication. In this paper robustness is implemented in Railway Network. To support this research the microscopic view of 'how to change track and optimize the delay at junction points' should be taken under consideration in the near future.

## ACKNOWLEDGEMENT

This research work is funded by Visvesvaraya PhD scheme of DeitY (Department of Electronics & Information Technology), Govt. of India.

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