

A Bio-inspired Auto-velocity Detection Algorithm for Autonomous Robots

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Abstract: As examples of computationally cheap and robust sensors the eyes of a fly are well known in literature. Attempts to replicate the function of the eye in electronic technology has resulted in several algorithms and implementations based on those algorithms. These implementations are either impractical for industrial use or use costly Application Specific Integrated Circuits. In an attempt to use a low-cost Commercial off the Shelf camera as a sensor in a real-world robot navigation use-case we investigate two commonly used algorithms and find them unsuitable. We develop a new algorithm – the Distance of Travel algorithm – show its suitability and investigate its properties in both simulation and practical experiments.

1 INTRODUCTION

A Motivation

Mobile robots working in semi-structured environments co-habited with humans will need to travel at variable speeds and trajectories and perform collision avoidance including subsequent re-routing should the chosen path be blocked. In other words they must be capable of (micro-) autonomous activity within the scope of a defined mission (macro-activity) within set deadlines. The body of work presented here belongs firmly in the domain of bio-inspired engineering where we seek to achieve lower computational cost and higher robustness by the emulation of biological examples as opposed to more traditional state-space oriented engineering. We do this in the knowledge that the performance of the robot may not be as efficient as a state-space based design and that work is required to make robot behaviour predictable so that humans know when and how to respond to an approaching robot.

The motivation for this body of work was to explore the practical ramifications of using biological precedence, the eye of a fly, in autonomous robots designed for practical purposes – in this case delivery along an office corridor. The fly eye has been well-studied over the last sixty years and can boast multiple

implementations is thus well-understood and hence a good example of a bio-inspired algorithm.

Much of the implementation work replicates the fly eye in a low-pixel count ASIC (Application Specific Integrated Circuit) and often in the context of drones. Our understanding of the use-case includes recognition of the fact that mobile robots will use a camera not only to perform low level navigational duties but also for high-level image processing tasks, a scenario precluded by single-function ASIC-based sensors. We are unaware of any fly-eye implementations on low-cost COTS (Commercial off the Shelf) camera so the novelty of our paper is therefore to analyse and implement a fly-eye algorithm on this class of platform.

Fly-eye algorithms can be categorised into four general types which we analysed and found wanting in various aspects. Response linearity at higher (robot) velocities is a common factor so we developed, simulated and implemented a new algorithm which we called the Distance of Travel Algorithm. It can be shown that the algorithm functions with better linearity of response at lower sampling rates than the reference algorithms and is better suited for use in the use-case we are working towards.

This paper is structured accordingly. We finish this section by discussing the related work, methodology and algorithms. The next section describes the simulation of standard algorithms we chose to implement. Section III discusses the Distance of

Travel (DoT) algorithm and simulations on it. Section IV discusses the practical implementation of the DoT algorithm and the final section draws conclusions and proposes future work.

B Related Work

Scientists have been examining the perception and navigation of insects in general and the fly in particular, for some 60 years and this has led to much work in replicating capabilities in technology. There is a substantial body of literature, including summaries to be found in this area of which Franceschini (Franceschini, 2014) is a leading example. Literature summarises the algorithms used in replicating the vision system in technology (Srinivasan, 1999) and summaries of published work detailing future trends / Orchard, 2014.) The field is divided into several distinct strands of research. Biological research generating replicable models was notably achieved by Hassenstein and Reichardt (Hassenstein, 1961) with their description of the Elementary Motion Detector (EMD - Figure 1) and continued with various elaborations or contrasting models such as the Barlow and Levick model (1965) or the Watson and Ahumada model (1985.) Engineering research has replicated these models using a variety of algorithms, largely using an analogue electronics approach. Initial work in this area (Tanner, 1986) set the tone for a largely analogue replication of the biological models (Harrison, 1999), (Pant, 2004), and (Roubieu, 2013.)

However engineering research has been by and large unable to look past the EMD and the attempt to optimally replicate it has resulted in the attempt to build neurological detectors (Higgins, 2000.) In contrast there has been little work done to explicitly apply the principles to CMOS detectors. Arreguit (1996) builds of a pointing device on a CMOS chip whereas Basch (2010, 2011) use of standard imagers to build Hassenstein-Reichardt based collision detectors stand out in an otherwise sparsely occupied literature canon.

C Methodology

Current published (research) solutions use anywhere from 8 to 254 pixels to build EMDs and it is perfectly acceptable to predict that these devices are capable of being industrialised at prices amenable to them becoming a standard low-cost, low-complexity sensor used in robot-construction.

Given that robot vision is still research-in-progress, especially in the higher strata beyond object recognition towards perception, it is also reasonable to

expect that CMOS-based vision systems will be expected to provide the data to perform several tasks, quite probably in parallel and possibly hardware off-loaded to ASIC or Field Programmable Gate Arrays (FPGA) devices. Auto-speed detection using a fly-eye algorithm of low computational cost and promising high robustness is a low-level task that can intuitively be mapped to a CMOS camera. This idea is strengthened by the fact that a CMOS camera can deliver the data for 3D speed detection, something we have not yet seen in ASICs produced by research.

From this background an appropriate methodology would be to choose an algorithm to implement, prove the use-case in software and measure the real-time properties of the solution to decide whether hardware offloading is necessary or beneficial.

D Algorithms

The EMD is a unidirectional unit that measures the time taken from the detection of an intensity-recognised feature by the first receptor to its detection by the second receptor. This time represents a metric for the speed of movement.

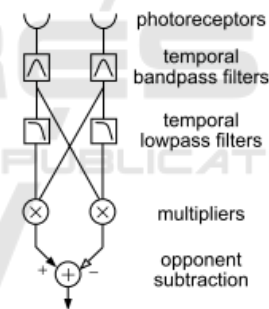


Figure 1: Elementary Motion Detector (EMD) according to Harrison (Basch et al., 2011).

The mechanisms whereby this is achieved in flies and modelled for replication in technology have been extensively researched to the extent that the technical implementations (Floreano, 2009) have been divided into two methodologies of each two categories (Figure 2.) The methodologies are intensity based and token based and subdivided into categories of gradient and correlation methodologies and the correlation and time-of-travel based methodologies respectively.

We place value on low computational and resource expense and used this as the primary criteria

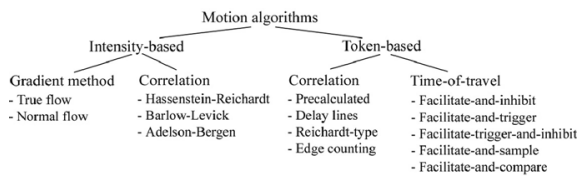


Figure 2: Categorisation of fly-eye based navigation algorithms (Barlow and Levick, 1965).

for examining the different algorithms. The gradient methodology was deemed to be computationally expensive whereas the published correlation/token-based methodologies require substantial memory resources and so were also excluded from further consideration. We chose the publications from Harrison and Koch (1999) who applied intensity based correlation using the Hassenstein-Reichardt principle and from Roubieu et al., (2013) who applied token based methods, as the most promising role-models and used them in further evaluation.

2 SIMULATION OF KNOWN ALGORITHMS

Further evaluation consisted of implementing and performing tests on these two algorithms in Matlab. We applied the general motion detection model, the EMD defined as two photoreceptors, as the input source. The outputs of the algorithms are based on the response measured between two photoreceptors – with a preferred direction. The optical space covered by a single photoreceptor is generally quite large so in the simulations these receptors are assembled from a number of pixels of the image/camera as shown in Figure 3 where a receptor was made up of an averaged 5*5 array of pixels.

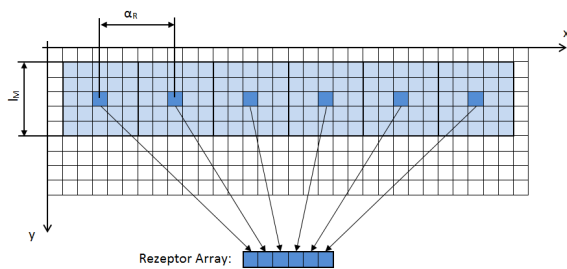


Figure 3: Assembling receptors from camera pixels.

Testing real-time response of vision-algorithms is difficult at the best of times and generally achieved by using patterns of some sort. Regular patterns such as square waves (black and white bars) and sinusoidal (white to black via a grey scale) are commonly used

and are useful for matching actual to predicted behaviour. For our use-case the material used for walls must also be considered so several different patterns were used. Results shown in this paper are generally derived from black-white vertical bars (square wave) and a randomly chosen concrete pattern (Figure 4,) which represents a stochastic signal.

We tested the algorithms by passing the patterns in front of the receptors at a number of constant velocities. To achieve this a script was programmed to produce 500 copies of a test pattern with each copy differing from the previous by a shift equivalent to the velocity the receptor is intended to be subjected to. By passing these pattern sequences at discrete intervals in front of the receptors – and allowing the algorithm to perform after being exposed to one shifted image – the speed of passing a pattern could be precisely simulated free of any real-time and computing-time restraints imposed by the test platform.

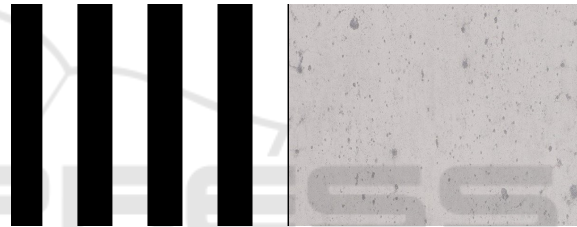


Figure 4: Black and white (left) and concrete (right) patterns for simulation of tokens.

A Hassenstein – Reichardt Detection

For the Hassenstein-Reichardt detector the configuration of the fly-eye assembled from camera pixels was determined as follows:

Table 1: Fly-Eye Parameters for the Hassenstein-Reichardt detector.

Parameter	Value
Distance between receptors (α_r)	4°
Mask Size	43 Pixels
Number of receptors	12 Receptors

After implementation in Matlab the first simulation was carried through with a sample time of 20 ms and it can be seen that good linear response of estimated velocity can be achieved up to an actual velocity of about 3 rad/s when the measured and actual velocities diverge (Figure 5.) This simulation was repeated at the faster sampling rate of 5 ms

(Figure 6) and the linearity of the response to the actual velocity is considerably better. Low cost cameras generally deliver images at frame rates of up to 60 fps, equivalent to a sampling rate of 16 ms, so we surmise the Hassenstein-Richardt does not appear to be suited for implementation on such a camera.

B Time of Travel Algorithm

The same procedure was repeated for the time of travel algorithm (ToT) proposed by Roubieu (2013.) The parameters for this simulation were set at the values given in Table 2.

Table 2: Fly-Eye Parameters for the Time of Travel detector.

Parameter	Value
Distance between receptors (α_r)	7°
Mask Size	77 Pixels
Number of receptors	6 Receptors

In (Figure 7) and (Figure 8) the results of sampling rate of 10 and 20 ms are shown. As with the Hassenstein-Richardt algorithm the linearity of the response of the algorithm to the actual velocity suffers at higher velocities, dramatically so at velocities over ~ 3 rad/s and sampling rates of 20 m/s.

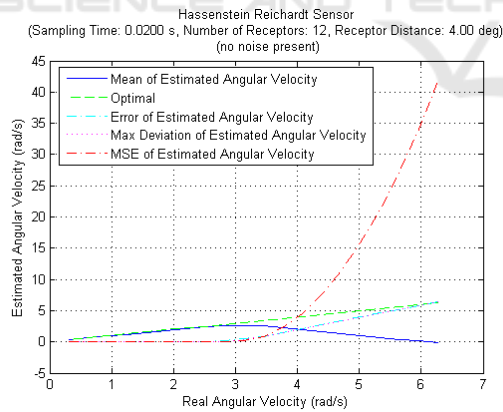


Figure 5: Performance of the Hassenstein-Richardt algorithm simulation at sampling rates of 50 Hz.

C Conclusion

Clearly the linearity is unsatisfying for low sampling rates at higher velocities which convinced us that investigation of a new algorithm better suited to the use case of a low-cost camera would be justified.

3 DISTANCE OF TRAVEL ALGORITHM AND SIMULATION RESULTS

A Distance of Travel Algorithm

We therefore propose a new algorithm which we call Distance of Travel (DoT) which bears close relationship to the time of travel algorithm. We actually break the concept of the EMD by extending the detection of tokens across the entire line of photoreceptors, and in principle across the entire line-width of the camera and treat the camera pixels as a coherent array.

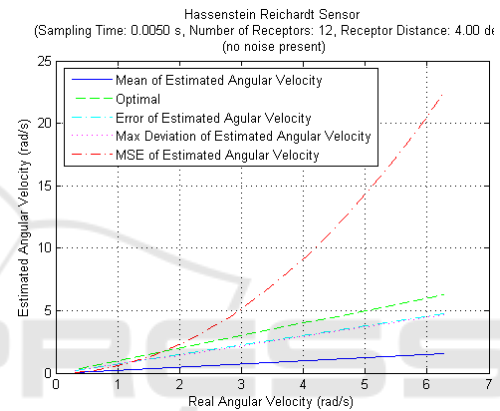


Figure 6: Performance of the Hassenstein-Richardt algorithm simulation at sampling rates of 200 Hz.

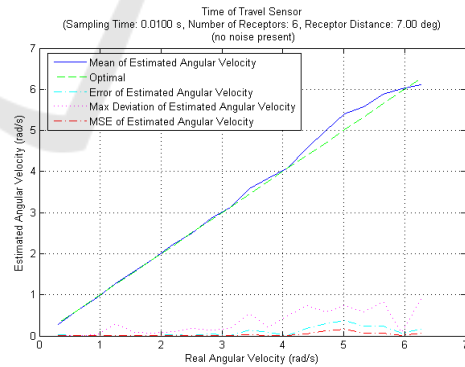


Figure 7: Performance of the Time of Travel Algorithm at sampling rates of 100 Hz.

The sampling time can be reduced by decreasing the distance between receptors but simultaneously retaining the precision of measurement as the algorithm measures the number of receptors the token traverses during a set sample time. The algorithm's principle of operation is shown in Figure 9 below.

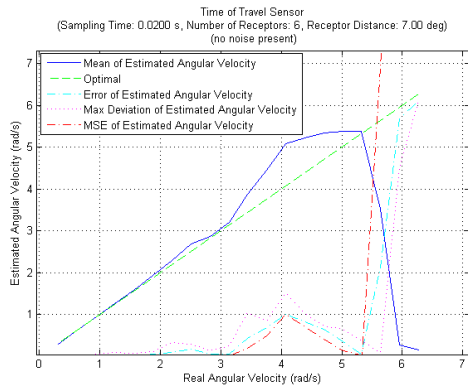


Figure 8: Performance of the Time of Travel algorithm at sampling rates of 50 Hz.

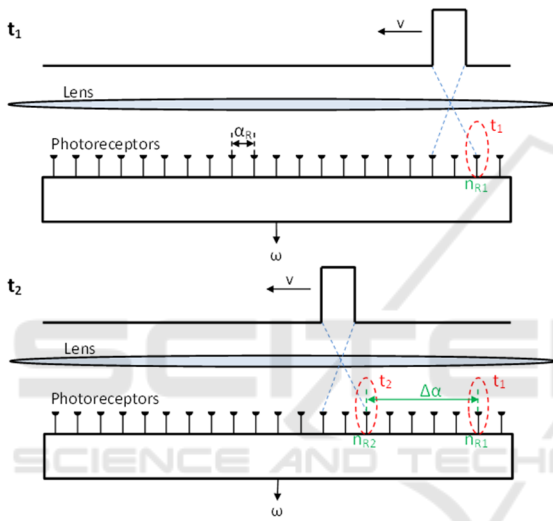


Figure 9: Principle of operation: Distance of Travel Algorithm.

From right to left, at t_1 a token is detected at the second receptor, at t_2 the seventh receptor detects the same token. From the travelled distance the angular velocity can be calculated using (1.)

$$\omega = \Delta\alpha / \Delta t = (\eta_{R2} - \eta_{R1}) \cdot \alpha_R / (t_2 - t_1) \quad (1)$$

The measured value may be refined by repeated detections of the (same) token across the pixels/receptors. Once the token reaches near the end of the pixel/receptor array the algorithm stops seeking another detection and returns to the beginning of the pixel/receptor array to search for a new token. If there is a new token the algorithm will be able to produce a stream of measurement values (Figure 10.)

The receptor's macro-construction is similar to classical elementary motion detectors and function as shown in Figure 11: A high pass filter (HP) eliminates offset components and heightens contrast. The next

block applies an intensity hysteresis. The determination of this hysteresis level was not without difficulty. If the value is too high a value then low contrast tokens won't be detected. If the level is too low the SNR degrades. For this reason we propose a method adaptive to the signal strength of the receptors. If a new token has been detected then, using the first 2/3 of the receptors (r), a minimum and maximum value is found and from this a high and low threshold value (T_{min} , T_{max}) calculated according to (2) and (3.)

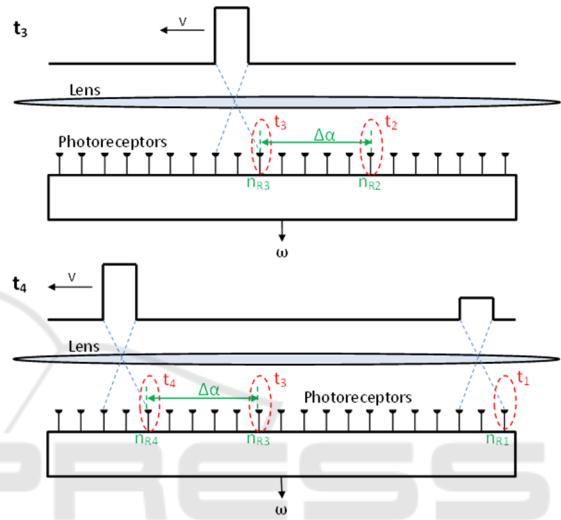


Figure 10: Principle of operation: Distance of Travel Algorithm - case of token leaving field of vision.

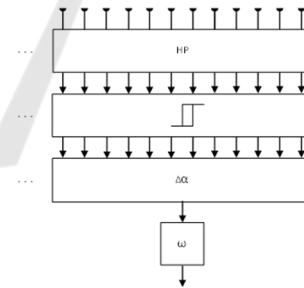


Figure 11: Architecture of threshold detection.

$$T_{min} = \min(r_{si-j}) + \min(r_{si-j}) / 5 \quad (2)$$

$$T_{max} = \max(r_{si-j}) + \max(r_{si-j}) / 5 \quad (3)$$

B Simulation Results

The Distance of Travel implementation was exposed to the same simulation benchmarks as the other algorithms. In this case the receptors were built from an empirically determined 5x5 pixel mask with one overlapping column of pixels with the neighbouring

receptor (Figure 12.) Table 3 shows the parameters which were used for the simulations.

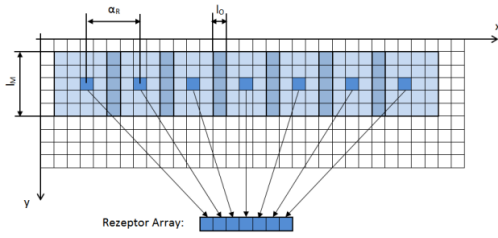


Figure 12 Assembling receptors from camera pixels for the Distance of Travel Algorithm.

Table 3: Fly-Eye Parameters for the Distance of Travel detector.

Parameter	Value
Distance between receptors (α_r)	0.36°
Receptor size	$5 * 5$
Receptor Overlap	$1 * 5$
Number of Receptors	100

The first test was to trigger the algorithm with a simulation pattern at a constant angular velocity of 0.63 rad/s . and the results proved encouraging. Unlike the Hassenstein-Reichardt or ToT detectors the measured velocity exhibited no oscillations. The velocity was then varied to produce a set of measurements, analogous to Figure 5– Figure 8, the results of which are replicated in Figure 13. The linearity is far better across the entire test range, at sampling times of 20 ms, than both the Hassenstein-Richardt and time of travel algorithms.

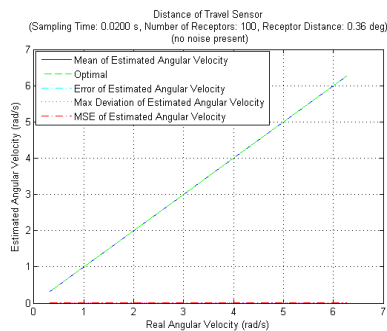


Figure 13: Performance of the Distance of Travel Algorithm simulation at sampling rates of 50 Hz.

The algorithm was further examined, also using different test patterns, specifically wood, brick and concrete (Figure 4.) Good results were achieved with the first two only on the concrete pattern did the linearity of the detector degrade at angular velocity above 3.5 rad/s (Figure 14).

4 DISTANCE OF TRAVEL ALGORITHM IMPLEMENTATION AND TESTS

A Implementation

We considered the principle of the algorithm to be confirmed by these simulations and implemented the algorithm on the low-cost, COTS, leanXcam from SCS. This camera, is based on a $1/3''$ CMOS colour sensor and features a 500MHz Blackfin under uClinux, Unfortunately camera production has now been discontinued but the data sheet is still available (SCS 2016.)

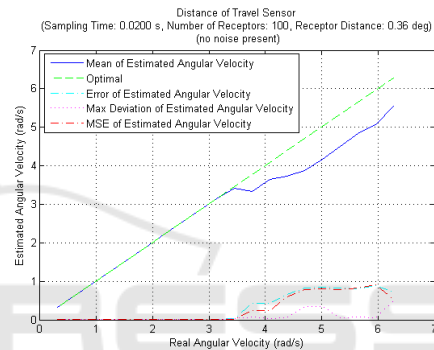


Figure 14: Performance of the Distance of Travel algorithm simulation at sampling rates of 50 Hz. and using the concrete pattern.

The implementation top-level code runs in an endless loop with both the run time of the software and the image capturing/transfer time determining the (real-time) timing characteristics. This allowed us to measure the run-time of the tasks and algorithms and determine whether further optimisations were necessary to ensure the system was capable of processing an adequate frame rate. The code flow is shown in Figure 15.

The camera chip is polled, using code supplied as libraries with the camera, in order to detect whether a new image is available and proceeds to further processing if this is the case. Set-up of parameters is achieved via an implemented web-interface, exposure time and max/min speeds for the search window are, amongst others, parameters that can be set. The velocity value output is via a simple `printf` on the camera's Ethernet console output.

The image processing (block "Processing Image" in Figure 15) is depicted in Figure 16.

The implementation, in contrast to the Matlab simulations, performs an intensity check exiting with

an appropriate return value if the intensity is not sufficient to detect a token. If there is sufficient intensity then the code searches for a second instance of the token under the assumption that a first instance is already available. If this is found then the angular velocity can be calculated. Should a first instance not be available, then it branches and searches for a first token – which will be the case when f.i. the system comes out of reset.

B Measurements

In order to get a direct correlation between the simulation and the implementation it was desirable to use exactly the same patterns in both environments. It might have been possible to run the test images on a computer screen but the PC screen generates light as opposed to reflecting it and it is difficult to ensure that a standard PC adheres to the real-time constraints necessary to ensure a constant streaming of images at the required rate/velocity. For this reason a test-jig based around a conveyer belt was built (Figure 17.) The images previously generated were printed and stuck onto the conveyer belt (black and white image on the conveyer belt in Figure 17) and the speed of the conveyer belt could be adjusted.

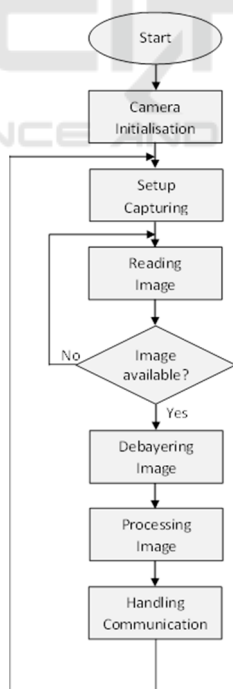


Figure 15: Flow Chart for the General Operation of the Fly-Eye Camera.

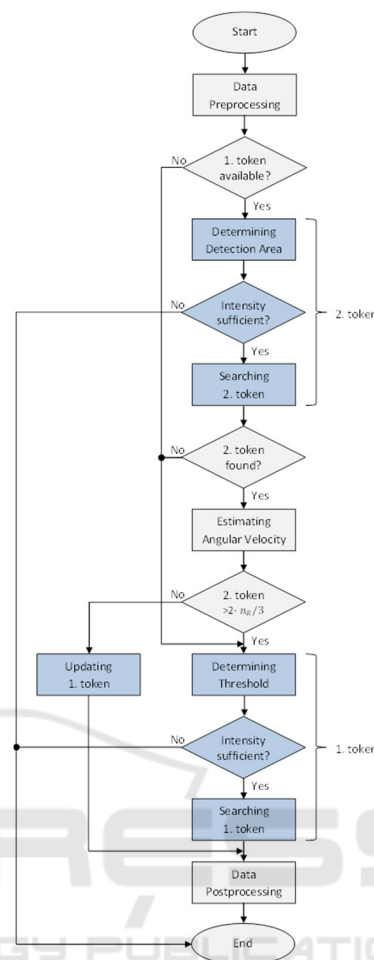


Figure 16: Flow Chart for the operation of the Distance of Travel Algorithm Implementation on the LeanXCam.

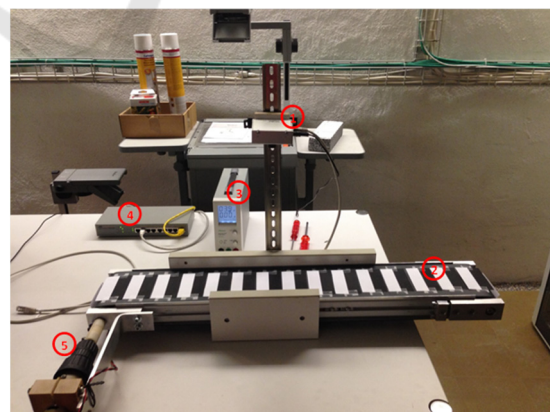


Figure 17: Picture of test-jig.

The schematic in Figure 18 shows the jig parameters used in the tests and in most of the tests the parameters noted in Table 4 were used.

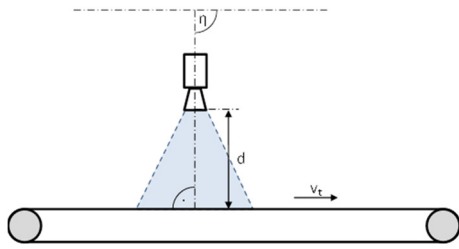


Figure 18: Schematic of test jig.

Table 4: Parameter Settings of Test-Jig.

Parameter	Value
Distance camera to the belt (d)	0.2 m
Angle of Camera to belt (η)	90°
Velocity of belt (vt)	0.2 – 0.8 m/s
Illumination	room
Illumination time	0.05 s
Test pattern	black/white stripe

The first results received a mixed reception. Encouraging was the closeness of velocity measurement to that of the belt but substantial oscillations were also visible in the output of the DoT sensor. Further investigation resulted in an attempt to provide the motor with better gears as it appeared that the motor wasn't rotating at constant speed. That brought no resolution but it was noticed that the motor was periodically sticking. A test run where the motor current and voltage were also measured, albeit not synchronised with the conveyer-belt or DoT/camera sensor, was made. The motor voltage and current subsequently graphed against the velocity measured by the DoT implementation is shown in Figure 19. The estimated angular velocity tracks the “stickiness” of the motor/belt, as measured by motor voltage/current, very well and we consider this to be a sign of the quality of the DoT algorithm and its implementation.

Evidenced by further test runs with the belt moving at different velocities and the camera mounted at distance of 0.3 meters from the belt, the DoT algorithm shows an excellent correlation between expected and measured velocity albeit, there is a deviation observable at speeds greater 0.75 m/s which requires further investigation. Unfortunately a different test-jig is required as the maximum velocity of the conveyer belt is 0.85 m/s.

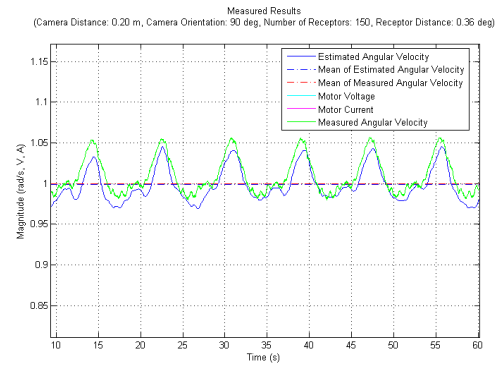


Figure 19: Correlation of Distance of Travel algorithm with motor current.

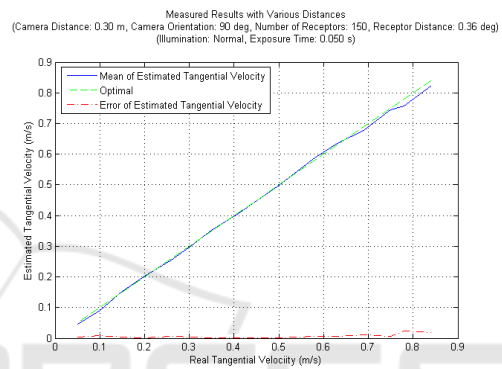


Figure 20: Performance of the Distance of Travel algorithm implementation at sampling rates of 50 Hz. and using the stripes pattern.

1) Wall Pattern

The DoT algorithm depends on contrast changes in its line of sight to determine velocity. As in the simulations several other patterns were taped onto the conveyer belt and the velocity measured, the results being shown in Table 5.

Table 5: Measurement error of Distance of Travel implementation using various test patterns.

Test Pattern	Average measured angular velocity (rad/s)	Average estimated angular velocity (rad/s)	Error %
Stripes	0.67	0.66	1.5
Brick	0.67	0.73	9.0
Concrete	0.67	0.72	7.5
Wood	0.67	0.74	10.5

2) Camera Orientation

The use case is a mobile robot moving in a straight line down a corridor under closed loop control with the output of this algorithm/sensor as an input value.

The robot is bound to turn appreciably towards and from the wall so the angle of the camera to the wall will change and thus the measured angular velocity. The effect of camera rotation on the measured velocity can be seen in Figure 21.

3) Real-Time Constraints

We assume that images will be streamed at a constant rate from the CPTS camera so algorithm code must adhere to real-time deadlines. We measured the time for the algorithm to determine velocity on a per captured frame basis over a time period of 60 seconds for which an average CPU time of 171 μ s was determined (Figure 22.) The operating system interfering with the execution of the tasks is responsible for the peaks seen $> 200 \mu$ s. The measurement was repeated for the de-Bayering algorithm and an average of 514 μ s was determined for the execution time.

5 CONCLUSION, DISCUSSION AND FURTHER WORK

A Conclusion

We have shown by simulation that current implementations of the fly-eye algorithm for auto-velocity detection are unsuitable for implementation on low-cost commercially available cameras. This is largely due to the fact that the usual technical construction of the elementary motion detector is such that sampling times higher than that deliverable by these cameras are required for accurate measurement.

We have proposed a new algorithm, called the Distance of Travel algorithm, which is suitable for implementation on low-cost commercial cameras operating at low sampling rates. We showed that the algorithm exhibits better linearity at high angular velocities than two well-established algorithms and has potential for real-world application. We implemented this algorithm and showed through tests that the promise shown through simulation is reflected in real-world measurements. The real-time characteristics of the implementation are also attractive.

B Discussion

The Distance of Travel algorithm was also examined with the explicit aim of enabling a robot to orientate and navigate down a corridor and hence both regular (square wave) and irregular real-world patterns, brick

and concrete, were used during tests.

Whilst the results are good, as the figures for the square-wave patterns show, some of the simulation results can not be reproduced in the real-world.

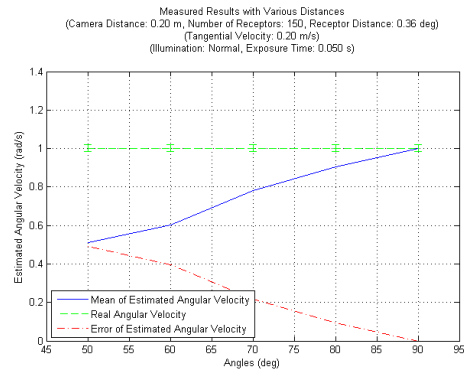


Figure 21: Performance of the Distance of Travel algorithm implementation at different camera angles.

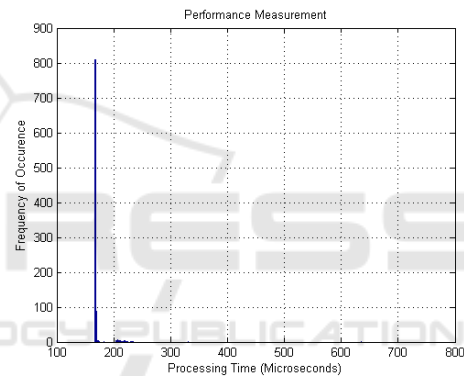


Figure 22: Processing time distribution Distance of Travel implementation.

In the case of concrete up to 7.5% error can be observed in the velocity range tested. Further work is required to understand and evaluate these discrepancies. In the real-world it cannot be expected that regular patterns will be painted on walls to help mobile robots with their orientation so the algorithms used need to be robust to variations in wall patterns. We don't expect a bio-inspired robot, or one using bio-inspired sensors, to drive a perfectly parallel to a corridor wall so we must get some feeling for how much the robot will oscillate around the line of direction and, of course, whether this is acceptable in a real-world environment.

In the case of the concrete pattern, a stochastic pattern that we can find in our own institutional buildings, we observe an error of $\sim 7.5\%$, we don't know whether this is acceptable in a real world case. Neither do we know what the minimum pattern is necessary for a wall to have so that an acceptable

robot trajectory emerges. These are all issues for further research.

C Further Work

The first focus for further research is mounting the camera(s) on a mobile robot and allowing it to drive semi-autonomously down a corridor at speeds of up to 1 m/s. The final aim is for the robot to liaise with “pheromone” carrying RFID tags placed at discrete and longer intervals in the corridor as described by Doran (2011.) This body of work will include investigating an extension of the algorithm for the 2D case and whether and how the robot should be allowed to move in reverse. General robustness is also an issue.

The suitability for offloading the algorithm into an FPGA is also to be examined as we believe that the combination camera, CPU and FPGA – as opposed to the use of GPUs - to be the most cost efficient for mobile robotics. This idea is supported by the increasing number of SoC FPGA devices with multi-(hard) cores being offered on the market. A second reason is that Lichtensteiger (2004) showed that an optimal fly-eye facet pattern (i.e physical arrangement and size of photoreceptors) could be derived for specific tasks. By using a learning algorithm Lichtensteiger generated one pattern for navigation along a wall and a second one for optimised obstacle detection, both in the direction of travel. By streaming images through an FPGA it is possible to apply the facet principle multiple times, like a filter, on different physical locations of the image. It should therefore be possible to generate hybrid fly-eyes that achieve different aims at very low computation expense. Work is needed to show the viability of this approach.

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