

Forecasting River Water Quality using Autoregressive Integrated Moving Average (ARIMA)

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Abstract: Water quality affects the level of public health and the welfare of society. So it is necessary to keep the water clean. This study aims to predict the water quality of river X using the Arima method. The research uses the degree of acidity (pH), COD, and BOD data from 2007 to 2018. The forecasting results show that pH is 7.44, the COD value is 50.4184, and the BOD value is 3.310473. Therefore, in 2019, river X is in class III, which is the river is for freshwater fish cultivation, livestock, or crop irrigation.

1 INTRODUCTION

Sustainable availability of clean water is a global problem, including in Indonesia (Rahim and Soeprobowati, 2019). Clean water vitally needs for drinking, daily needs, agriculture, and also economic needs, such as fishery and plantation. If water quality decreases (contaminated), it will affect the level of public health and the welfare of society (Smiley and Hambati, 2019). Water quality control is needed to reduce the risk of river water pollution and the availability of sustainable clean water. The Indonesian government issued regulations regarding the use of clean water-based on the allocation into four classes. Class I is for raw water of drinking water. Class II is for infrastructure or water recreation facilities, freshwater fish cultivation, livestock, water for irrigating crops. Class III is for freshwater fish cultivation, livestock, crops irrigation, while Class IV is for irrigating crops only.

In this study, we used three parameters of river water quality. These parameters are the degree of acidity (pH), Chemical Oxygen Demand (COD), and Biological Oxygen Demand (BOD). pH indicates the levels of hydrographic ions contained in the water (Rahim and Soeprobowati, 2019) (Waleed et al., 2019). pH levels in the body affect the body's metabolism and ability to produce enzymes and hormones in the central nervous system. COD parameters indicate the need for oxygen to oxidize dissolved compounds and

organic particles in water (Chen et al., 2018) (Le et al., 2018). The smaller the COD value of water, the cleaner the water becomes. BOD shows the oxygen demand needed by microorganisms to break down dissolved and suspended organic substances in water (Liang et al., 2018) (Spurr et al., 2018).

The Indonesian government states that clean water has a pH between 7 and 9. If the pH more than nine and less than seven water is polluted. COD parameters have different values for each class. Class I pH value of 10 mg / l, class II of 25 mg / l, class III of 50 mg / l, while class IV 100. This value indicates the oxygen needed by organic particles to carry out oxidation. So the higher the value of COD can be said the water is increasingly polluted. Because the level of oxygen needed to carry out oxidation is higher than usual. BOD parameter values for each class differed, namely in class I BOD values of 2 mg / l, class II by 3 mg / l, class III by 6 mg / l, while grade IV by 12 mg / l. This value is different because the BOD value indicates the amount of oxygen needed by microorganism for suspended organic substances. So that if the BOD value indicates more than 12 mg / l, that river water is polluted.

This study aims to predict river water quality by examining river water data. Research data used are river X measurement data. Whereas X river is a river located on the island of Java, Indonesia. This river is used to meet the needs of clean water by residents. The prediction results will be used to determine wa-

ter pollution prevention policies. The method used is a time series that analyses data based on a certain. ARIMA time series method analyses stationary and non-stationary data to make predictions. Its accuracy can reach 91.85% (Arya and Zhang, 2015) (York and Gernand, 2017). So the ARIMA method can make more accurate predictions.

2 LITERATURE REVIEW

2.1 Time Series

Time series analysis is a set of observations with uniform observation. The time-series analysis on the assumption that the values of a data set are historically consecutive with the same intervals between observations (Ivanović and Kurbalija, 2016). The purpose of using time series analysis is to identify the characteristics of the phenomena observed sequentially and predict the value that will occur in the time series. To achieve these two objectives requires the identification of the data pattern of the observation time series. So that its relationship with other phenomena can show. Thus, the identified time series patterns can be extrapolated to predict future events. In general, the time-series pattern can describe two primary components, which are trends and seasonality.

2.2 Autoregressive Integrated Moving Average (ARIMA)

The Autoregressive Integrated Moving Average (Arima) method, commonly called the Box-Jenkins method is a method developed by George Box and Gwilym Jenkins in 1970 (Arya and Zhang, 2015). The Arima method is a method used for short-term forecasting. The use of the ARIMA method in short-term forecasting is very appropriate to use because the ARIMA method has a very accurate accuracy (Arya and Zhang, 2015). Also, determine an excellent statistical relationship between variables to be predicted with the value used for forecasting. While for long-term forecasting, the accuracy of forecasting is not good. Usually, the forecast value will tend to be constant for a reasonably long period.

In solving problems from a time series data using pure AR / ARIMA (p,0,0), pure MA / ARIMA (0,0,q), ARMA / ARIMA (p,0,q) or ARIMA (p,d,q) through several stages, namely identification, parameter estimation, diagnostic testing and forecasting application. Model groups included in the ARIMA method are (Tauryawati and Irawan, 2014).

1. Autoregressive Model (AR)

The assumption held by this model that data influenced by past data. Called the Autoregressive model because in this model it is regressed against the previous values of the variable itself. The autoregressive model with the order p shortened to AR (p) or ARIMA (p, 0,0). The general equation of the AR model (p,0,0) in equation 1.

$$Z_t = \mu + \phi_1 Z_{t-1} + \phi_2 Z_{t-2} + \dots + \phi_p Z_{t-p} + a_t \quad (1)$$

Wheres,
 Z_t = stationary time series
 μ = constant
 Z_{t-p} = independent variable
 ϕ_p = coefficient of the autoregressive at p
 a_t = error value at t

2. Moving Average Model (MA)

The general form of the moving average of the order q (MA (q)) or ARIMA (0.0, q) shown in equation 2.

$$Z_t = \mu + a_t - \theta_1 a_{t-1} - \theta_2 a_{t-2} - \dots - \theta_q a_{t-q} \quad (2)$$

Wheres,
 Z_t = stationary time series
 μ = constant
 a_{t-q} = independent variable
 θ_q = coefficient of the autoregressive at p
 a_t = error value at t

3. ARMA

The Autoregressive Moving Average (ARMA) model is a combined model of the Autoregressive (AR) and Moving Average (MA). This model has the assumption that the previous data influence current data. The general form of ARMA shown in equation 3.

$$Z_t = \mu + \phi_1 Z_{t-1} + \dots + \phi_p Z_{t-p} + a_t - \theta_1 a_{t-1} - \dots - \theta_q a_{t-q} \quad (3)$$

Wheres, Z_t = stationary time series μ = constant
 Z_{t-p} = independent variable ϕ_p = coefficient of the autoregressive at p a_{t-1} = independent variable θ_q = coefficient moving average parameter a_{t-q} a_t = error value at t

4. ARIMA

The Integrated Moving Average Autoregressive Model (ARIMA) is used based on the assumption that the time series data used must be stationary, meaning that the average variation of the data

in question is constant. However, several things happen when data is not stationary. In overcoming this unstable data, a differencing process so that the data becomes stationary. The Autoregressive (AR), Moving Average (MA), Autoregressive Moving Average (ARMA) models are not able to explain the meaning of the difference. A mixed model called the Autoregressive Integrated Moving Average (ARIMA), or ARIMA (p,d,q) thus becomes more effective in explaining the differencing process. In this model, the stationary series is a linear function between past value with present value and the past error. The general form of ARIMA shown in equation 4.

$$\phi_p(B)D^d Z_t = \mu + \theta_q(B)a_t \quad (4)$$

Where, ϕ_p = coefficient of the autoregressive at p
 θ_q = coefficient moving average parameter a_{t-q} B = backshift operator D = differencing μ = constant
 a_t = error value at t p = degree of autoregressive d = differencing process level q = degree of moving an average

3 DATA ANALYSIS METHOD

ARIMA can make a forecast using stationery and non-stationery data (Arya and Zhang, 2015). So, the first step is to analyze data patterns. This analysis is needed to find out stationary or non-stationary data. If data not-stationer, it will be transformed into stationer data before make analysis forecast. Flow chart of forecasting data using ARIMA show Figure1.

Identification of data patterns shows from Auto-correlation (AC) and Partial Correlation (PAC) graph. Another way can also use the root test to see the Augmented Dickey-Fuller (ADF) value. Stationery data has an ADF absolute value is higher than the test critical values. If the ADF value is smaller than the critical value, then do difference level 1 and do the root test again. If the root test results for differencing one show stationary data. Then the identification of the Arima model identification can be made with differencing 1. However, if the data is not stationary, then do difference level 2. Then do the root test for differencing level 2.

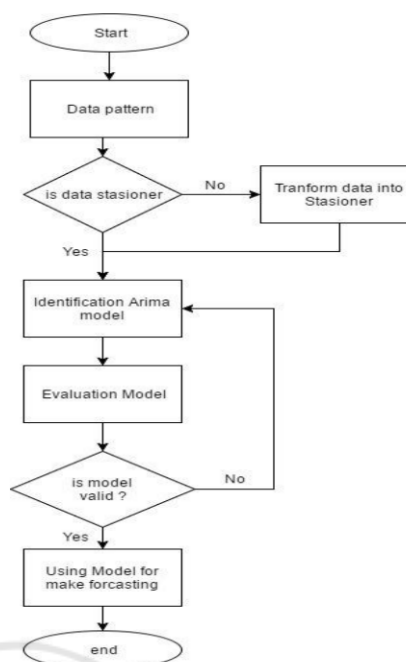


Figure 1: Flow chart of forecasting data using Arima.

AC and PAC graphs predict p and q ordo can. If the AC chart, there is a graph that crosses the line then we have an MA candidate 1. in the PAC graph there is a bar that crosses the line, then we get a AR 1 candidate. Then the D coefficient is the differencing level for converting data into stationary data

The selected Arima model has the smallest values of the Akaide Info Criterion (AIC) and Schwarz criterion (SC). Than developing ARIMA equation model based on the coefficient, AR, MA, ARMA values. For evaluation chosen model, in this paper, use residual test. Residual test show autocorrelation problem in Grafik AC, PAC and QStat values. A good model successfully resolves the autocorrelation problem. It can show from the Q-stat value, which is not significant in each lag.

The best model chosen is used to make forecasting. The resulting model accuracy show from the Mean Absolute error (MAE) value. The more the MAE value approaches 0, the more accurate the model. Because the MAE value shows the difference between predictions with real values.

4 RESULT AND DISCUSSION

This study uses the measurement data of river water pollution from 2007 to 2018 in on one of the rivers in Java. Measurement data are analyzed to determine data patterns. The data is analyzed using the root test. The results of the data analysis shown in Figure 2.

Parameter	ADF Test (level)	Test Critical Values (5%)	Conclusion (level)
pH	-1.910441	-3.259808	Non-stationary data
COD	-5.431870	-3.175352	Stationary data
BOD	-1.735694	-3.175352	Non-stationary data

Figure 2: Stationarity Test Results Using The Augmented Dicky Fuller Test Method.

Based on Figure 2, the pH and BOD parameter data are non-stationary data, because the absolute ADF value is smaller than the critical test value at a 5% confidence level. So the pH and BOD values are transformed using difference level 1. The COD parameter data is stationary because the absolute ADF is higher than the critical test value. So the difference value (D) is 0.

Analysis of pH and BOD parameters using different level 1 in Figure 3. The results of the data analysis show that parameter pH and BOD data are stationary. It can show that the absolute ADF value is higher than the critical test value for the two parameters. So the difference value for pH and BOD parameters is 1.

The next step is to determine the possibility of p and q ordo using AC and PAC tests. These result AC and PAC analysis for parameter pH (Figure 4), COD (Figure 5), and BOD (Figure 6).

Parameter	ADF Test (diff 1)	Test Critical Values (5%)	Conclusion (diff 1)
pH	-5.480464	-3.212696	Stationary data
BOD	-3.407288	-3.212696	Stationary data

Figure 3: Stationary test results of pH and BOD parameters after being transformed Using Augmented Dicky Fuller Test Method.

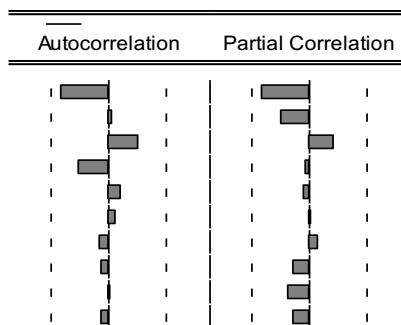


Figure 4: AC and PAC Analysis for pH Parameter

AC and PAC graphs of pH parameters (Figure 4) show no bar crossing the line. So that the order p and

q are 0 or 1. Besides, the value of D defines as 1. So that the possibility of the Arima model that will be used is ARIMA (1,1,1), ARIMA (1,1,0), ARIMA (0,1,1) or ARIMA (0,1,0).

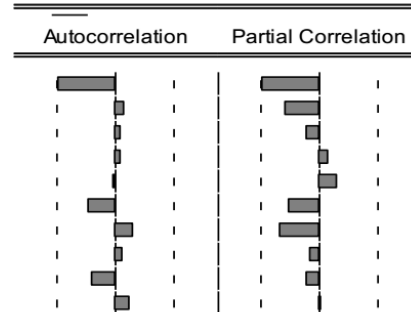


Figure 5: AC and PAC Analysis for COD Parameter

AC and PAC graphs show COD parameters (Figure 5) show no bar crossed the line. So that the order p and q are 0 or 1. Besides that, the D value defined as 0. So that the possibility of the Arima model that will show is ARIMA (1,0,1), ARIMA (1,0,0), ARIMA (0,0,1) or ARIMA (0,0,0).

AC chart and PAC for BOD parameters (Figure 6) show no bar crossed the line. So that the order p and q are 0 or 1. The value of D is 1. So that the possibility of the Arima model that will be used is Arima (1,1,1), Arima (1,1,0), Arima (0,1, 1) or Arima (0,1,0)

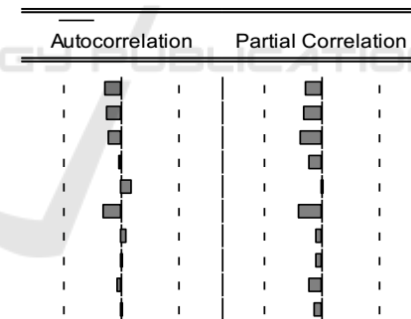


Figure 6: AC and PAC Analysis for BOD Parameter

The possibility of the Arima model on each parameter was analyzed to find out AIC and SC values. The model chosen has the smallest AIC and SC values.

Model Arima	AIC	SC
ARIMA (1,1,1)	-5.660924	-5.516235
ARIMA (1,1,0)	-5.752083	-5.643566
ARIMA (0,1,1)	-5.856626	-5.748109
ARIMA (0,1,0)	-5.792120	-5.755948

Figure 7: AIC and SC values for pH parameter.

In Figure 7 shows ARIMA (0,1,1) has the smallest AIC and SC values of -5.856626 and -5.748109. So, pH parameters using the ARIMA (0,1,1).

Model ARIMA	AIC	SC
Arima (1,0,1)	2.797757	2.942446
Arima (1,0,0)	3.057738	3.166255
Arima (0,0,1)	2.900695	3.009212
Arima (0,0,0)	3.307519	3.343691

Figure 8: AIC and SC values for COD parameter.

In Figure 8 shows ARIMA (1,0,1) has the smallest AIC and SC values of 2.797757 and 2.942446. So for COD parameters using the ARIMA (1,0,1).

In Figure 9 shows ARIMA (0,1,0) has the smallest AIC and SC values of 2. 1.583488 and 1.619660. So for BOD parameters using the ARIMA (0,1,0).

Model ARIMA	AIC	SC
Arima (1,1,1)	1.942098	2.086787
Arima (1,1,0)	1.919380	2.027896
Arima (0,1,1)	1.900953	2.009470
Arima (0,1,0)	1.583488	1.619660

Figure 9: AIC and SC values for BOD parameter.

The model selected for each parameter validated by residual white noise test. This test aims to determine whether the model can solve the autocorrelation problem or not.

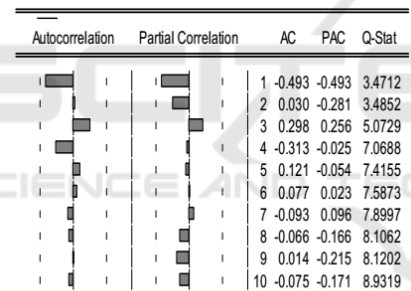


Figure 10: Residual cost test results for pH parameter

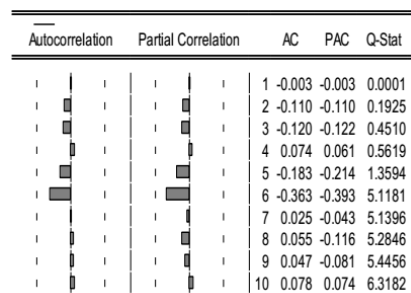


Figure 11: Residual cost test results for COD parameter

Figure 10 shows the results of the residual white noise test for pH parameters. ARIMA (0,1,1) for the pH parameter. Figure 11 shows the results of the residual white noise test for COD parameters. Figure 12 shows the results of the residual white noise

test for BOD parameters. In all three pictures, no bar crosses the line. So, the ARIMA (0,1,1) for the pH parameter, ARIMA (1,0,1) for the COD parameter, and ARIMA (0,1,0) for the BOD parameter can solve the autocorrelation problem. So that Arima equation can be built based on the coefficient values, AR, MA and S.E of Regression from each Arima model for the three parameters.

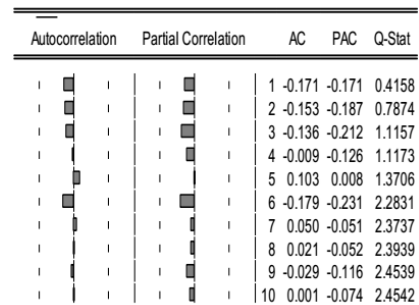


Figure 12: Residual cost test results for BOD parameter

Figure 13 shows the analysis result coefficient, AR, MA and SE of Regression for ARIMA (0,1,1) for the pH parameter, ARIMA (1,0,1) for the COD parameter, and ARIMA (0,1,0) for the BOD.

Parameter	C	AR	MA	S.E. Of Reg.
pH	0.005454	-	-0.999971	0.010320
COD	0.019746	-0.584698	-0.999998	0.719903
BOD	-0.044177	-	-	0.511479

Figure 13: Coefficient AR, MA and ARMA values.

Forecasting equation for pH parameters using ARIMA (0,1,1) is in equation 1. Forecasting equation for COD parameters using ARIMA (1,0,1) is in equation 2. Forecasting equation for BOD parameters using ARIMA (0,1,0) is in equation 3.

$$Z_t = 0.005454 + 0.010320a_{t-q} - (-0.999971) \quad (5)$$

$$Z_t = 0.019746 + (-0.584698)a_{t-p} - (-0.999998a_{t-q}) + 0.999998 \quad (6)$$

$$Z_t = -0.044177Z_t + 0.511479a_{t-1} \quad (7)$$

The forecast value of pH in 2019 is 7.45 with the MAE coefficient of 0.008649 based on equation 1. the forecast value of COD in 2019 is 50.4184 with the MAE coefficient of 0.552897 from equation 2. the forecast value of BOD in 2019 is 3.310473 with the MAE coefficient of 0.414456 from equation 3.

5 CONCLUSIONS

The prediction of water quality on river X in 2019 for the pH parameter is 7.45, the COD parameter is 50.4184, and the BOD parameter is 3.310473. Thus in 2019, river X water is in class III. X river water is predicted not to use as raw material for drinking water, only for freshwater fish cultivation, livestock, crop irrigation. So the government must make policies and plan for pollution prevention on river X. So that in the future river X can be used as raw material for drinking water and other activities.

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