


An Improved Cuckoo Search Algorithm for Multiple Odor Sources Localization

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Keywords: Cuckoo Search Algorithm, Odor Source Localization, Multi-robot Cooperation.


Abstract: This work presents an improved Cuckoo Search Algorithm (CSA) for multiple odor sources localization. The idea of forbidden areas is introduced to the CSA as territories of the cuckoo colonies, preventing the cuckoos from being trapped into local optimal solutions. A source is declared when a certain number of cuckoos are located in close proximity with each other, and a territory is formed around the declared source centered at the local best among those cuckoos. When territories overlap, they are merged into one territory to prevent the same source from being found multiple times. Simulation results show that the proposed method can locate multiple odor sources with high accuracy.

1 INTRODUCTION

Odor source localization, a problem of retrieving the source of an odor based on its traces emitted from the source, has various applications in our lives, including searching for locations of toxic gas leakages, survivors, sources of fires, and explosives. Currently, people mainly solve this problem by using either static robots or trained animals. However, these approaches have certain constraints that limit their performances in certain environments. Static robots are inflexible and hard to setup in an unknown environment. Trained animals can't get close to places with toxic gas and gets tired easily. To overcome these constraints, source localization with active robots becomes more prevalent (Chen and Huang, 2019). Compared to static robots, active robots can collaborate with each other flexibly without the limitations of their locations. Compared to trained animals, active robots are able to work in a variety of environments for prolonged periods of time.

Solving the odor source localization problem with multiple active robots can have two different cases: single source localization and multiple sources localization. When solving single source localization problem with multiple active robots, maintaining diversity and handling problems with local optimal

solutions during the search can be challenging. When solving multiple sources localization problem with multiple active robots, researchers tend to divide the robots into groups. Group formation, group aggregation maintenance, following the same plume by more than one group, and avoiding re-finding the same odor source are the main challenges of multiple odor sources localization problem with multiple robots. Therefore, researchers have been exploring different algorithms in respond to these challenges. These algorithms can be classified into three types: collaborating with a team of robots in nature-inspired ways (Shida, *et al.*, 2005; Marques, Nunes, Almeida, 2002) calculating the distribution of the plume (Pang, 2010), and visualizing the search area (Wang, Meng, Zeng, 2011). One subcategory of the nature-inspired algorithms is swarm intelligence where robots highly collaborate with each other. Swarm intelligence based algorithms convert the odor localization problem into an optimization problem that doesn't require precise information about the gas distribution to solve the problem. However, the algorithms that are used to solve for the source localization problems face some limitations. For example, the Genetic Algorithm (Marques, Nunes, Almeida, 2002) and the Particle Swarm Optimization (PSO) (Feng, *et al.*, 2019) can easily fall into local optimal solutions when solving the single source localization problem, while some

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multi-modal optimization algorithms such as the Glowworm Optimization Algorithm (Thomas and Ghose, 2009) and the Ant Colony Optimization (Cao, *et al.*, 2013) require large number of robots and might not be able to find all the sources accurately when solving the multiple source localization problem. Attempting to address these issues, we proposed an improved Cuckoo Search Algorithm (CSA) for multiple odor sources localization problem.

The CSA is proposed by Yang and Deb (2009, 2010). Modelled after the cuckoos' parasitic reproduction strategy, the CSA uses the coevolution between the parasitic cuckoos and their hosts to maintain diversity of the cuckoo population. The cuckoo population would migrate toward the best nest for a certain distance determined by the Lévy Flight, a flying strategy by a lot of birds, in each generation, hoping to encounter a better solution around the best nest while the best nest stays at the same location in case the plume is lost. Solving the odor source localization problem with CSA requires high collaboration between the robots (represented as cuckoos in the algorithm) and captures the global scope well. It is simple and efficient, requiring little number of inputs to operate. Nevertheless, it can easily fall into local optimal solutions and has a slow rate of convergence. Some improvements have been made to deal with these drawbacks of the CSA. For example, Valian, Mohanna, and Tavakoli (2011) modified the algorithm such that it can adjust its parameters, such as the step size, by itself depending on its environment; Ghodrati and Lotfi (2012) combined the Cuckoo Search with PSO to improve the efficiency of the algorithm; In Srivastava, *et al.* (2012), the CSA was mixed with the Tabu Search to prevent the Cuckoos from falling into local optima and flying repeated paths.

In this paper, an improved CSA is proposed to solve the multiple odor sources localization problem, where the idea of territories and group based strategies are introduced such that once some robots are in close proximity, the area is declared as a territory containing the source. If the newly declared territory overlaps with previously declared territories the new territory would merge with the territories it overlaps with. Unlike the work of Srivastava, *et al.* (2012), which marks the very place the cuckoos landed on as a forbidden area, our algorithm actively predicts the forbidden area that might contain a good solution. Moreover, Srivastava, *et al.* (2012) stores the flying paths of the past cuckoos to prevent repeated flying paths, while we only store the areas where cuckoos are concentrated in. Simulation results show the effectiveness of the improved CSA in the

multiple sources localization problem, and its superiority over the classical CSA in single source localization problem in a particular case.

For the rest of the article, Section 2 states the problem. Section 3 states the details about the improved CSA, and Section 4 gives the simulation results. At Section 5, the conclusions are discussed.

2 PROBLEM FORMULATION

The Gaussian Dispersion Models (GDMs) are used in this paper as they are the most commonly used models in regulatory air dispersion modelling (Visscher, 2013). They are easy to use, able to accurately predict the concentrations around a source when the surrounding landscape of the source is fairly simple. It is valid under the assumptions below:

- The wind field is stable.
- The release source is a point source.
- The release rate is constant.
- The atmospheric turbulence is constant in space and time.

The three-dimensional GDM can be described as

$$c(x_r, y_r, z_r; \theta) = c(x_r, y_r, z_r; x_s, y_s, z_s, q) = \frac{q}{2\pi\sigma_y\sigma_z} \exp\left(-\frac{y^2}{2\sigma_y^2}\right) \left[\exp\left(-\frac{(z+h)^2}{2\sigma_z^2}\right) + \exp\left(-\frac{(z-h)^2}{2\sigma_z^2}\right) \right] \quad (1)$$

where c represents the concentration of the targeted gas at point (x_r, y_r, z_r) given the location of the source (x_s, y_s, z_s) . u is the wind speed, y is the dispersion parameter in the horizontal direction and z is the dispersion parameter in the vertical direction. σ_y and σ_z are the standard deviation in the horizontal and vertical directions, respectively. h is the effective source height.

To further simplify the GDM, formula (1) can be converted to a two-dimensional space, resulting in

$$c(x_r, y_r; \theta) = c(x_r, y_r; x_s, y_s, q) = \frac{q}{2\pi k \sqrt{(x_r - x_s)^2 + (y_r - y_s)^2}} \times \exp\left(-\frac{u(\sqrt{(x_r - x_s)^2 + (y_r - y_s)^2} - (x_r - x_s))}{2k}\right) \quad (2)$$

where c represents the concentration of the targeted gas at point (x_r, y_r) given the location of the source (x_s, y_s) . k is the gas diffusion coefficient.

The dispersion model for multiple point sources can be found based on the two-dimensional GDM under two assumptions:

- There is no chemical reaction and interactions between the substances released from the point sources
- The distance between the point sources are great enough to consider each point source separate from another.

Once these assumptions are satisfied, the gas dispersion model for multiple sources becomes a linear addition of formula (2), as represented below:

$$C(x_r, y_r; \theta) = C(x_r, y_r; \tilde{N}, X, Y, Q) = \sum_{i=1}^{\tilde{N}} c(x_r, y_r; x_i, y_i, q_i) \tag{3}$$

where C is the gas concentration at (x_r, y_r) , contributed by multiple point sources. \tilde{N} is the number of point sources. $X = x_i (i = 1, 2, \dots, \tilde{N})$ and $Y = y_i (i = 1, 2, \dots, \tilde{N})$ contains the X and Y coordinates of the \tilde{N} point sources $Q = q_i (i = 1, 2, \dots, \tilde{N})$ where q_i is the emission rate for the point source located at (x_i, y_i) .

Multiple odor sources localization can be challenging as the number of sources to be found is unknown and it is easy to find the same source multiple times. While the classical CSA is only used to locate a single source, it searches for sources efficiently and requires a small number of parameters to function. Therefore, an improved CSA is proposed to solve the multiple odor sources localization problem, that is, to find all the relative maxima of formula (3) within bounds.

3 THE CSA

Being the best known brood parasite, cuckoos never build their own nests and lay their eggs in other birds' nests, leaving the host birds to take care of their young. The cuckoo mother would remove one egg laid by the host mother, laying her own egg as a substitute and flying away quickly. Cuckoos can mimic the color and pattern of their eggs to match the eggs of the hosts, with each female specializing in one host species. Many host species learn to recognize cuckoo eggs in their nest and throw the eggs out of their nest, so the cuckoos have to constantly improve their mimicry to avoid being detected by the host birds.

For simplicity, three idealized rules are applied to the CSA (Yang and Deb, 2009, 2010):

- Each cuckoo lays one egg at a time, dumping it in a random nest;
- The best nests with high quality of eggs (solutions) carry over to the next generation;
- The number of available nests is fixed. A host can discover a cuckoo egg with a probability $P_a \in [0,1]$. In this case, the host bird can either throw away the egg or abandon the nest and build a completely new nest. For simplicity, the assumption is that the egg is thrown away and the nest stays in the same place.

As shown in Fig. 1, the CSA starts out with an initial population of cuckoos (robots in the context of odor source localization), having laid some eggs in the host bird's nest. The eggs that are more similar to the host's eggs have an opportunity to grow up and enter the next generation. Other eggs are killed by the hosts.

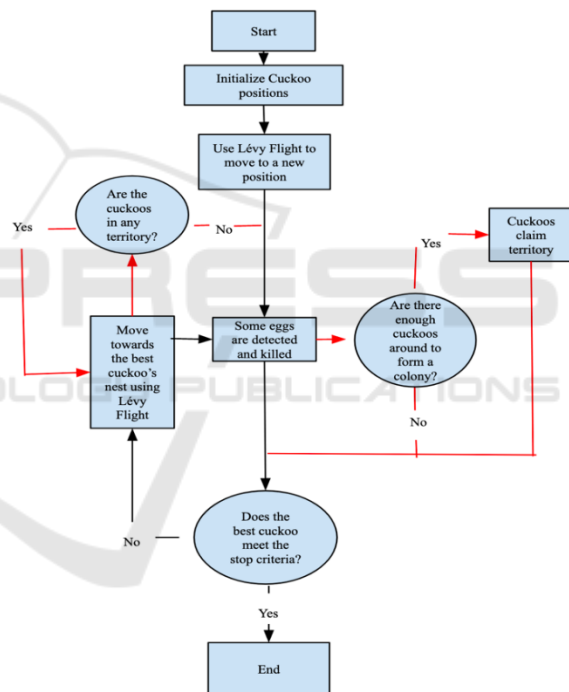


Figure 1: A flowchart of the classical and improved CSAs. The red lines represent the procedures added during the improved CSA while the black lines are the steps in the classical CSA.

To maximize the eggs' survival rates, the cuckoos search for the most suitable habitat and immigrate toward it using Lévy Flight, a flight style of a lot of birds. They will end up inhabiting somewhere near the best habitat and lay their egg within a certain distance from their position. In the classical CSA, this process would continue until most cuckoos gather at one position. However, in the proposed improved

CSA, this process continues until some cuckoos gather around the same position, forming a colony in that area and occupying that area as their territory. Any cuckoo that lands on a territory is kicked out using Lévy Flight with a large step size. After the program terminates, each territory would be declared as a source.

3.1 The Improved CSA

The cuckoos are distributed at random positions on the coordinate plane. R_i ($i = 1, 2, \dots, N$) contains the positions of the cuckoos on the coordinate plane where N is the number of cuckoos and $R_i = (x_i, y_i)$ is the position of the i -th cuckoo with x_i being the x -coordinate of the i -th cuckoo and y_i being the y -coordinate of the i -th cuckoo.

The cuckoos would be flying and forming colonies in T , the entire area, where

$$T = \{(x, y) \mid x \in [0, a], y \in [0, b]\} \quad (4)$$

The Lévy Flight random walk is used to update the position of the cuckoos given a step size. While the targeted gas still remain undiscovered, the i -th cuckoo during the g -th generation would update its position based on the following formula:

$$R_{i,g+1} = R_{i,g} + L_i \quad (5)$$

where $R_{i,g+1}$ is the position the i -th cuckoo would fly to in the next generation, and $R_{i,g}$ is the i -th cuckoo's current position. $L_i = a \oplus L(\lambda)$ for the i -th cuckoo where a is the step size, $L(\lambda)$ satisfies the Lévy distribution, and \oplus means entry-wise multiplication. The Lévy Flight provides a random walk with a random step length drawn from a Lévy distribution.

$$\text{Lévy} \sim \mu = t^{-\lambda}, \quad (1 < \lambda \leq 3) \quad (6)$$

Because Lévy distribution (6) has an infinite variance with infinite mean, the solution generated by the Lévy distribution can be too far away from the old solution and jump outside of the bounds when t is too small. The random step length is generated using Mantegna's algorithm which follows the symmetric Lévy distribution. A simplified version of Mantegna algorithm in Yang and Deb (2010) is used in this study as it does not apply nonlinear transformation to generate Lévy Flight, making Lévy Flight easier to calculate.

After traces of the targeted gas is discovered, the i -th cuckoo during the g -th generation would update its position based on the following formula:

$$R_{i,g+1} = \begin{cases} R_{best} + L_i & \text{if } i \neq N_{best} \\ R_{best} & \text{if } i = N_{best} \end{cases} \quad (7)$$

where R_{best} is the current best solution, being N_{best} -th cuckoo in the population.

Every time the position of the cuckoo is updated, a random number r is generated and compared with a discovery rate P_a , such that if $r < P_a$, the current egg is discarded. The cuckoos would attempt to declare territories after a certain number of generations (defined by the user) to determine T_0 , the area the cuckoos will be flying in during the next generation, which is

$$T_0 = T / \bigcup_{i=1}^p T_i \quad (8)$$

where p is the number of existing groups G_i ($i = 1, 2, \dots, p$) in T . T_i , the territory of G_i , is a square with a side length of b such that

$$T_i = \{(x_i, y_i) \mid x_i \in [G_{i,best} - \frac{b}{2}, G_{i,best} + \frac{b}{2}], y_i \in [G_{i,best} - \frac{b}{2}, G_{i,best} + \frac{b}{2}]\} \quad (9)$$

where $G_{i,best}$ is the local best within G_i .

If T_i overlaps with T_j , the territory of G_j , G_i and G_j would share territories such that

$$T_i = T_j = T_i \cup T_j \quad (10)$$

The foreign cuckoos in the T_i ($i = 1, 2, \dots, p$) would be chased out with a large step size Lévy Flight.

The complete improved CSA can be described as the following Algorithm 1. In which, the parameters b and \hat{N} need special attention when implementing the algorithm. If b is too large, the algorithm runs the risk of combining multiple sources into one source, while if b is too small, the algorithm might considering different parts of one source as two different sources. Theoretically speaking, b should be approximately the average length of each plume's shortest secant passing through the plume's center in a two-dimensional plane. However, this can be hard to calculate in the real world when the distribution of the sources is unknown. If \hat{N} is too large, some sources might never be found and the algorithm might get stuck when multiple groups of robots are each located at a different source while none of them is greater than \hat{N} , while if \hat{N} is too small, the algorithm might not be able to locate the sources accurately. Generally speaking, a large \hat{N} means slower searching speed and higher searching accuracy. The number of sources, N and b should be considered

when setting \hat{N} . A larger N and b require a larger \hat{N} to maintain the accuracy of the algorithm. However, a \hat{N} larger than optimum increases the searching time of the algorithm. As the number of sources increases in the area, \hat{N} should decrease so there are enough robots to spread between different sources at the same time. In order for the algorithm to search with great accuracy, the sources should be distant enough such that parts from multiple plumes can't be contained by a $b \times b$ square.

When the initial position of the robots are far away from the largest source, the improved CSA can actually find all the sources more quickly and more accurately than the classical CSA can find the largest source. This means when the boundaries of the area to be searched remains unknown, the improved CSA can be more suitable for the task of searching for the largest source than the classical CSA.

Algorithm 1: Improved CSA.

```

1. Initialization
   Initialize the positions of the cuckoos
   Find current best
2. Iterative Process
   while (current_Time < max_CPUTime)
     for every nest
       Use Lévy Flight to immigrate to new
       location
       if  $r < P_a$ 
         Egg is thrown away.
         Find new best
       end if
     end for
     if cuckoos found within a square of side
     length  $b$  of a cuckoo  $\geq \hat{N}$ 
       Find the local best in these cuckoos.
       Create territory centered at  $G_{i,best}$ .
       if new territory overlaps with pre-
       existing territories
         Combine territory based on (10)
       end if
     end if
     while  $R_{i,g+1}$  is in  $T_i$  ( $i = 1, 2, \dots, p$ )
       Use Levy Flight with a larger step
       to relocate.
     end while
   end while
   return current best

```

4 SIMULATION RESULTS

In this section, the searching time and accuracy of the classical CSA and the improved CSA are compared with different initial positions of the nests. We setup sources 1-7 in the designated area, located at (10,10), (23,45), (45,10), (40,45), (30,30), (13,35), and (25,16) respectively, with source 1 being the largest source. Figs. 2 and 3 show the concentration of the odor around the designated area calculated by the GDM.

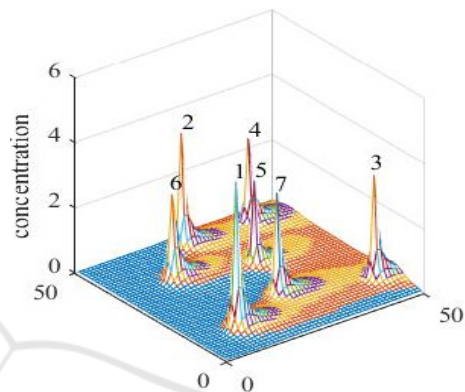


Figure 2: 3D graph of odor sources.

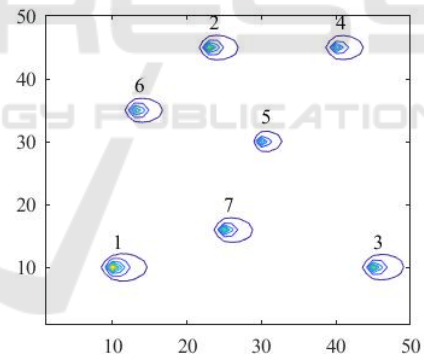


Figure 3: Countour graph of odor sources.

In the following simulation, N is set to be 50. The max CPU time (max_CPUTime) is set to be 0.15, but this can give various results depending on the computer's running speed. \hat{N} is set to be 5 and b is set to be 6. For classical CSA the requirement is to find the largest source, while for the improved CSA the requirement is to find all sources in the designated area. Each case is run 100 times. In order to estimate the total searching time, we assume that the searching time in the g -th generation is given as

$$t_g = \max_i D_{i,g} / \text{speed}$$

where $D_{i,g} = \sqrt{(x_{i,g+1} - x_{i,g})^2 + (y_{i,g+1} - y_{i,g})^2}$ denotes the i -th cuckoo's flying distance in the g -th

generation and speed is set to be 3600 meters/hour in this simulation. Then the total searching time can be estimated as

$$t_{total} = \sum_{g=1}^{max_generation} t_g.$$

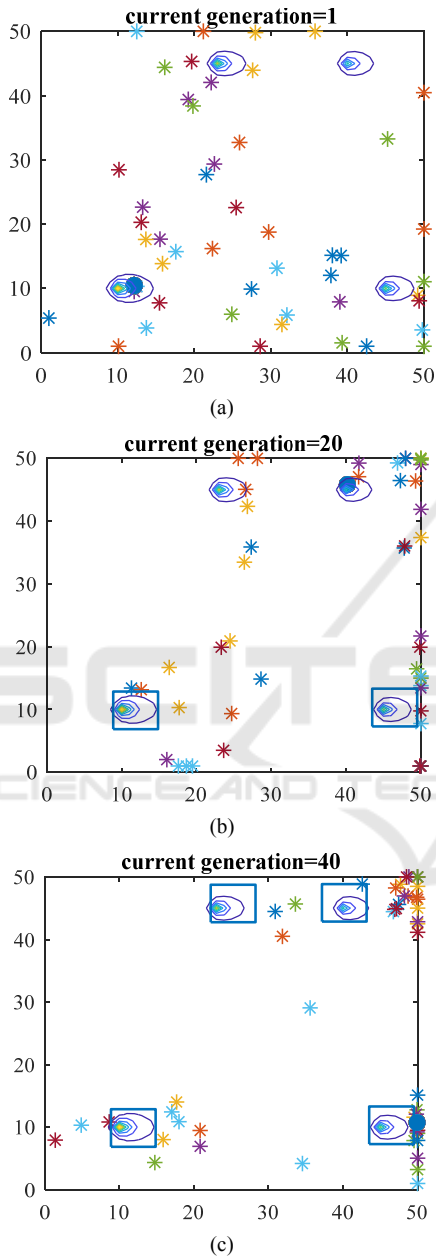


Figure 4: Searching procedure of improved CSA.

Fig. 4 shows the searching procedure of the improved CSA. In Fig. 4(a), the initial cuckoo population is uniformly distributed. In Fig. 4(b), two sources are found by the cuckoos in twenty generations. In Fig. 4(c), all four sources are found by the cuckoos in forty generations, with the location of

the source located within the squares, and for most of the time relatively near the center of the square.

4.1 The Initial Cuckoo Distribution

Two different initial distributions, one is uniform and the other is far from largest source, are experimented to compare the efficiency of the conventional Cuckoo Search and the Improved Cuckoo Search.

When the cuckoos are distributed uniformly across the area (shown in Fig. 4(a)), the classical CSA achieves its requirement only slightly faster than the improved CSA most of the time. This is because the improved CSA would have to cover extra distance to find all the sources while the classical CSA only needs to find the main source. However, the time it takes for the improved CSA to find all four sources is generally within the range of time the classical CSA takes to find the largest source. From Fig. 5, we can see that the accuracies of the CSAs are similar, with the classical CSA having 98% accuracy and the improved CSA having 95% accuracy.

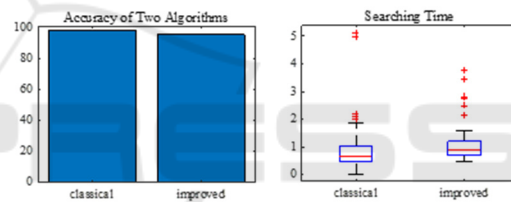


Figure 5: Accuracy and searching time of classical and improved CSA when cuckoos are uniformly distributed.

When the initial distribution of the cuckoos are far from the main source (shown in Fig. 6), the improved CSA can outperform the classical CSA. This is because the cuckoos can get trapped in local sources that are not the largest source in the classical CSA while the idea of territories in the improved CSA eliminates that problem.

It can be seen from Fig. 7 that, the accuracy of the classical CSA is 16% when the cuckoos' initial positions are far from the largest source while the accuracy of the improved CSA is 85%. Even though both algorithms have increased searching time and decreased searching accuracies, the change in initial positions has a minor impact on the improved CSA when compared to its impact on the classical CSA. This shows that the improved CSA is not as restricted to its initial positions as the classical CSA and therefore when the area of search remains unknown and the robots cannot be uniformly distributed, using the improved CSA to find the absolute maximum can be faster than using the classical CSA.

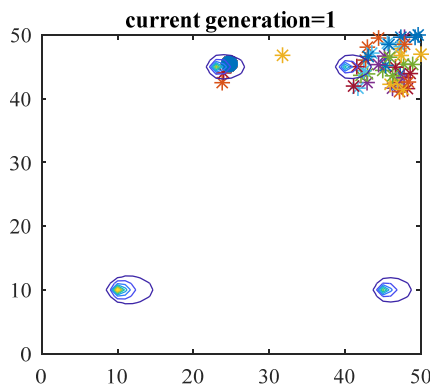


Figure 6: Initial distribution far from the largest source.

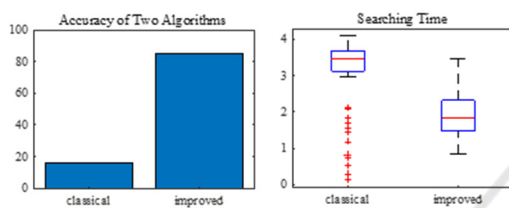


Figure 7: Accuracy and searching time of classical and improved CSAs when cuckoos population is distributed far from the largest source.

4.2 The Number of Sources

In this subsection, the performances of the classical CSA and the Improved CSA are compared with different number of sources set up in the designated area. Table 1 records the median of the searching time of the algorithms in 100 trials while Table 2 records the accuracy of the algorithms in those trials.

Table 1: Searching time of the algorithms with different number of sources.

Sources in the area	Classical CSA Time	Improved CSA Time
1-2	0.4508	0.4467
1-4	0.8376	0.8294
1-6	0.9926	1.3213
1-7	1.1013	2.6410

Table 2: Accuracy of the algorithms with different number of sources.

Sources in the area	Classical CSA accuracy	Improved CSA accuracy
1-2	100%	98%
1-4	100%	97%
1-6	98%	98%
1-7	97%	96%

From Table 1 we can conclude even though both algorithms search at increased time as the number of sources increases, the improved CSA's searching

time increases at a faster rate compared to that of the classical CSA. This is because the improved CSA has to search for all the sources and therefore the more sources there are the more time it needs to find all of them while for the classical CSA the sources only add distractions to finding the largest source. From Table 2 we can conclude that the accuracy of both algorithms are mostly maintained. Because of the uniform distribution of the initial nest positions in this simulation, the increase in the sources did not affect the accuracy of the CSAs by much since they can easily spot the different sources.

4.3 The Number of Cuckoos

In this subsection, the classical CSA and the Improved CSA are simulated with different number of cuckoos. Because N is significantly changed, \hat{N} needs to change accordingly to maintain the accuracy and speed of the improved CSA. We set \hat{N} to be $12\%N$ in this experiment because it gives us a relatively good \hat{N} to work with most of the time. However, there can be a \hat{N} that gives better results in the different cases. In the case of 50 cuckoos, a better \hat{N} to use is 5 instead of the output of the formula which is 6, and that's why we set \hat{N} 5 in the previous simulations with 50 nests. Nonetheless, in this subsection we would use the number calculated by the formula as our \hat{N} such that there's less confusion.

Table 3 records the median of the searching time of the algorithms in 100 trials while Table 4 records the accuracy of the algorithms in those trials. Table 3 shows the number of cuckoos has a large effect on the speed of the improved CSA. While the speed of the improved CSA slightly increases with an increase in number of cuckoos, the number of cuckoos during the search has a larger impact on the classical CSA than the improved CSA. From Table 4 we can see that while the number of cuckoos generally don't have a big effect on the accuracy of both algorithms, the accuracy and speed for the improved CSA decreased sharply with the case of 10 cuckoos. This is because there is no good \hat{N} for the case with 10 cuckoos. While according to our calculation \hat{N} should be 2 in the case of 10 cuckoos, it is really not a good \hat{N} because this means once two cuckoos meet they would declare that area as a source, leading to declaration of incorrect areas as sources. However, a \hat{N} larger than 2 would mean that the cuckoos have to be less dispersed which means when the cuckoos encounter a source, they might have to move away from it to meet other cuckoos at another source located further away from them, which greatly

increases the searching time. Nonetheless, if improvements in accuracy is needed, a \tilde{N} of 4 is able to increase the accuracy to around 85%, but with a tradeoff in time for as long as 4.4918.

Table 3: Searching time of the algorithms with different number of cuckoos.

Number of Cuckoos	Classical CSA Time	Improved CSA Time
10	1.9161	1.7611
30	1.1818	1.2394
50	0.7873	1.1571
70	0.3717	1.0639

Table 4: Accuracy of the algorithms with different number of cuckoos.

Number of Cuckoos	Classical CSA accuracy	Improved CSA accuracy
10	89%	72%
30	99%	95%
50	100%	93%
70	100%	93%

5 CONCLUSIONS

In this paper, an algorithm for the multiple odor sources localization problem based on an improved CSA has been proposed. The improved CSA uses the ideas of territories and colonies to solve multiple odor sources localization problem and is able to accurately find all the sources in a relatively short period of time with great accuracy. Simulation results show that the improved CSA can successfully search for all the odor sources in the area for mostly above 90% of the times. In future work, we will try to shorten the searching time this algorithm takes and possibly derive a formal formula to use for \tilde{N} .

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