Specularity, Shadow, and Occlusion Removal from Image Sequences using Deep Residual Sets

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Abstract: When taking images of planar objects, the images are often subject to unwanted artifacts such as specularities, shadows, and occlusions. While there are some methods that specialize in the removal of each type of artifact individually, we offer a generalized solution. We implement an end-to-end deep learning approach that removes artifacts from a series of images using a fully convolutional residual architecture and Deep Sets. Our architecture can be used as general approach for many image restoration tasks and is robust to varying sequence lengths and varying image resolutions. Furthermore, it enforces permutation invariance on the input sequence. The architecture is optimized to process high resolution images. We also provide a simple online algorithm that allows the processing of arbitrarily long image sequences without increasing the memory consumption. We created a synthetic dataset as an initial proof-of-concept. Additionally, we created a smaller dataset of real image sequences. In order to overcome the data scarcity of our real dataset, we use the synthetic data for pre-training our model. Our evaluations show that our model outperforms many state of the art methods that are used in related problems such as background subtraction and intrinsic image decomposition.

1 INTRODUCTION

When taking images of planar objects such as magazines, paintings, posters, books, or facades, one is confronted with many possible obstructions. Some of these, such as specularities or shadows, may be due to illumination, while others may be due to occlusions. These effects can lead to information loss and significantly reduce the image quality. It is often not possible to capture a single flawless image, however obstructions, such as specularities or occlusions, usually vary with the viewpoint of the camera or move over time. Our proposed method aims to provide a practical solution for reconstructing the content using multiple partially-obstructed images.

We introduce a novel approach using deep learning that learns an end-to-end image transformation to remove artifacts from a sequence of distorted images. Due to the lack of an existing dataset, we generate a synthetic dataset and a real dataset. Our synthetic data creation process follows a realistic image formation model and creates complex artifacts containing occlusions, specularities, shadows, and varying illumination.

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Training a deep neural network requires a large amount of training data in order not to overfit. Our real dataset is not large enough; however, we can create an arbitrarily large amount of artificial data. Therefore, we use a combined approach of pretraining on artificial data (200,000 image sequences) and only fine-tuning on the significantly smaller real dataset (100 image sequences).

The proposed architecture uses the concept of Deep Sets (Zaheer et al., 2017), making it robust to varying lengths of input sequences and invariant to permutation. We provide a memory-efficient algorithm for processing arbitrarily long input sequences. Furthermore, the architecture is fully-convolutional, i.e. it can handle images of varying resolution. We compare our deep learning method to unsupervised methods that are commonly used for outlier removal, background subtraction, and intrinsic image decomposition.

2 RELATED WORK

Many methods deal with each problem individually, typically modeling shadows as multiplicative distortions of the original content, and specularities as ad-

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ditive distortions. Some methods model the problem as an intrinsic image decomposition, that is, an image is decomposed into a reflectance image (albedo) and a shading image. Reflectance describes the amount of light an object reflects; it is an intrinsic value that depends only on the object's material. Shading is a varying property that depends on the lighting conditions and the position of objects relative to the light sources. Background subtraction methods deal with a similar problem. Given a series of images with a dynamic foreground, the background has to be extracted, which is assumed to be constant.

One can differentiate between single-image and multi-image approaches for artifact removal. Singleimage approaches use prior knowledge to identify specularities (Artusi et al., 2011) and shadows (Finlayson et al., 2009), relying heavily on assumptions about the appearance of said artifacts. Multi-image approaches can use statistical properties (Weiss, 2001) or optimization (Yu, 2016) to combine information from all images for reconstruction.

Deep learning approaches that do not rely on rigid assumptions are used in many state-of-the-art image processing tasks. Convolutional Neural Networks (CNNs) have been successfully used on single images for shadow removal (Qu et al., 2017; Hu et al., 2019) and specularity removal (Lin et al., 2019). They have also been applied to intrinsic image decomposition (Lettry et al., 2018). However, none of these methods gives a general solution for artifact removal. Moreover, there are few methods that use multi-image approaches, even though additional images could provide more information for the reconstruction. Furthermore, some objects, such as paintings, photographs, or posters, can contain shadows, specularities, and various objects as stylistic elements. Single-image methods could distort parts of the content by mistake. For example, without using additional images, it can be impossible to differentiate between a shadow that has been cast onto an book cover and a shadow that is part of the book cover's content.

Our use case contains a combination of all previous problems: varying illumination, shadows, specularities, and occlusions. This work proposes a universal approach, using deep learning that utilizes input sequences in order to solve a more complex problem. There are deep learning models that learn to transform image sequences into single images (Chang and Luo, 2019; Wang et al., 2018; Xingjian et al., 2015). However, many methods that rely on RNNs, LSTMs, transformers, or 3D convolutions do not enforce permutation invariance or cannot handle dynamic sequence length. Moreover, many models are not very memory efficient. They either require low resolution images or they only process each image individually, discarding a lot of information. Permutation invariant CNNs have also been successfully used for image deblurring (Aittala and Durand, 2018). However, the proposed architecture can only handle low resolution images.

Our work provides the following main contributions:

- 1. Our architecture removes shadows, occlusions, and specularities simultaneously.
- 2. A synthetic dataset is created, using a 3D pipeline to generate artificial image distortions. The dataset can be used for pre-training machine learning models.
- 3. A dataset with real distortions is created, using commodity hardware.
- 4. We provide a general purpose deep learning architecture for image reconstruction from image sequences. The architecture is permutation invariant, robust to varying sequence lengths, and robust to varying resolutions.
- 5. We show for our use case that one can overcome data scarcity using pre-training on synthetic data.
- 6. The architecture was optimized to process images sequences of at least 4K resolution. We provide a simple online algorithm for processing arbitrarily long image sequences using a constant memory consumption.

3 DATASET

3.1 Synthetic Data

To the best of our knowledge, there is no labeled dataset containing aligned images with shadows, specularities, and occlusions, together with corresponding ground-truth. We therefore use a dataset consisting of 207,572 images of book covers taken from Amazon (Iwana et al., 2016). We add artificially-generated artifacts to these images and use the original book cover as ground truth. The dataset contains varying illuminations, occlusions and shadows. Figure 1 shows how we create a 3D scene: we position a plane such that it perfectly covers the image plane when projected and apply one of our book covers to this plane as a texture. We then generate multiple point light sources of varying position, intensity, and color. Afterwards, we position a random object between the image plane and the book plane.

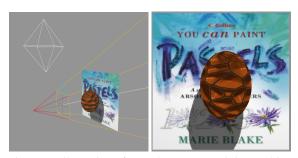


Figure 1: Illustration of a random scene and the resulting image. The white octahedron illustrates a point light source. The pyramid shows the frustum of the perspective camera and the image plane.

We create random reflectivity and roughness, which affects the shininess of the texture and the brightness of the book cover. These physical properties affect the appearance of specularities and the effect of lighting on the underlying image. For occlusions, we use a set of predefined geometries such as spheres, cones, planes, etc. and we randomly sample a shape for each scene, setting the orientation, size, texture, and position of the object at random. Although we use a finite number of shapes as occlusions, there are infinitely many ways to position, scale and texturize them.

The dataset is not a perfect representation of a realistic use-case, but it contains a broad variety of image distortions, which makes it suitable for pretraining our model. The pre-trained model can then be fine-tuned on the real dataset.

3.2 Real Data

We create an additional dataset containing real image sequences of planar objects, such as book covers and movie covers. The dataset contains 100 image sequences, each containing 11 images. One image is free of distortions, while the other 10 contain shadows, specularities, and occlusions. The images were taken indoors. The occlusions were created by placing various objects on top of the planar object. Specularities were created with lamps and flashlights. Shadows were cast onto the planar objects. The groundtruth images were made by taking images of the planar objects under ambient illumination.

Each sequence was aligned using a feature based method. We used a SIFT feature detector and computed element-wise homographies between the ground-truth image and all distorted images. In order to further improve the alignment, we used a method described by Schroeder et al. (2011) (Schroeder et al., 2011). We then cropped the images so that they only contain the content of the planar object.

4 DEEP LEARNING

4.1 Architecture

Our use-case requires the architecture to handle a dynamic number of input images. One possibility to implement this would be to use models for sequential data, such as recurrent neural networks or transformers. However, RNNs and transformers are not permutation invariant. Moreover, both architectures require a lot of memory, limiting the maximal resolution of the input images.

Therefore, we decided to use a Residual Network for our architecture. Residual Networks (ResNets) are used for many image restoration tasks; however, they usually require a fixed number of input channels. To apply ResNets to dynamic input sequences, we adapted the concept of Deep Sets by Zaheer et al. (2017) (Zaheer et al., 2017). Deep Sets enforce permutation invariance. Given a finite set $X = \{x_1, x_2, \dots, x_N\}$, a function *f* is permutation invariant, if it can be decomposed as follows:

$$f(x_1, x_2, \cdots, x_N) = \rho\left(\sum_{i=1}^N \phi(x_i)\right) \tag{1}$$

 ρ and ϕ describe deep learning models. Note that although *f* takes an ordered sequence as input, the order is irrelevant due to the commutative property of the sum. Besides, neither ρ nor ϕ are dependent on *N*; therefore, we can apply *f* to arbitrarily large image sets.

We created an architecture that follows this decomposition. The architecture consists of an encoder ϕ and a decoder ρ , which both make use of residual blocks. However, we replace the summation by a mean:

$$f(x_1, x_2, \cdots, x_N) = \rho\left(\frac{1}{N}\sum_{i=1}^N \phi(x_i)\right)$$
(2)

The mean normalizes the embedding space and enforces a scale invariance. It has been shown that ResNets are more robust to train than regular CNNs, especially on data that is close to an identity mapping (He et al., 2016). To increase the receptive field of our architecture, we use dilation. Yu et al. (2017) (Yu et al., 2017) showed that residual networks with dilation have an increased receptive field and outperform most non-dilated models without increasing the model complexity. Additionally, downsampling layers are used to reduce the dimensionality of the embedding and to further increase the receptive field. The downsampling layers are particularly necessary to reduce memory consumption in order to apply the architecture on high resolution image sequences. Figure 2 illustrates the encoder and decoder architecture and how they are combined. We use transposed convolutions to upsample our feature maps. Residual blocks decode the feature maps and generate the resulting image. After every convolutional layer in the encoder and decoder follows a *ReLU*-layer as non-linearity. Our architecture is fully-convolutional and can be applied on any image resolution.

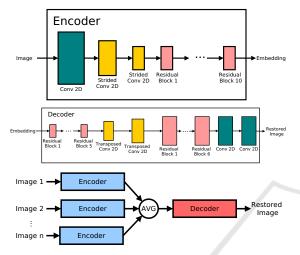


Figure 2: The first two images illustrate the encoder and decoder architecture. The third image shows how the encoder and decoder are used as building blocks in the overall architecture.

4.2 Training

All our models are trained on a NVIDIA Geforce RTX 2070 with 8GB memory. First, we train our model on the synthetic data. We use 100,000 synthetic image sequences for our training. The data is split into 75% training data and 25% test data. We use the Adam-optimizer with default parameters $\beta_1 = 0.9$, $\beta_2 = 0.999$, $\varepsilon = 10^{-8}$ and a learning rate $\lambda = 0.0001$. We use a decaying learning rate that is reduced every 5 epochs by a factor of 10. The mean squared error is used as optimization criterion. We use varying sequence lengths of up to 9 images. We use a batch size of 10 images sequences. All images have a resolution of 256×256 .

In order to apply our architecture to real images, we fine-tune our previous model on real data. We split the data into 60% training data and 40% test data. We train the model using the same parameters as before. The images have a resolution of 1024×1024 . The higher resolution increases memory consumption significantly, such that the model is not able to process a batch size of 10 images simultaneously. Instead, we emulate the batch size by processing individual image sequences and aggregating the gradients calculated by

backpropagation. After every 10th image sequence we perform the optimization step.

4.3 Online Inference

The standard implementation of Deep Sets has a high memory consumption, since an embedding $\phi(x_i)$ has to be computed and stored in memory for each input image before summation. One can optimize this by replacing the mean in (2) with an iterative computation:

$$e_0 := 0 \tag{3}$$

$$e_N := \frac{1}{N} \sum_{i=1}^N \phi(x_i) \tag{4}$$

$$= e_{N-1} + \frac{\phi(x_N) - e_{N-1}}{N}$$
(5)

$$\Rightarrow f(x_1, \cdots, x_N) = \rho(e_N) \tag{6}$$

A derivation for formula 5 can be seen in Finch (2009)(Finch, 2009). e_N is the accumulated average of all results from the encoders up to the *N*-th input image. e_N can be computed iteratively using an online algorithm (5). One can see that only the last accumulated result e_{N-1} and the new encoding $\phi(x_N)$ have to be stored in memory instead of all embeddings $\phi(x_1), \dots \phi(x_N)$.

With this method, deep sets can be efficiently applied on arbitrarily long sequences. Formula (6) also describes the applicability of online inference to realtime data. Using this method, we are able to process image sequences with 4K resolution on our GPU. Note that the model requires much more memory during training for gradient computations.

5 EVALUATION

5.1 Evaluation on Synthetic Data

We evaluate Residual Deep Set and several other methods on our synthetic dataset using varying lengths of input sequences n. From each image sequence, we randomly sample n images, which are then used for reconstruction and evaluation; we repeat this process 10 times for each image sequence. We then compare the results of our architecture to those of common approaches for outlier removal, background subtraction, and intrinsic image decomposition. Firstly, we use a pixel-wise median of the RGB intensities for reference. Secondly, we use an intrinsic image decomposition method that uses a Maximum Likelihood Estimation (MLE) of the reflectance (Weiss, 2001). Thirdly, Robust PCA (RPCA) is being used. RPCA uses optimization to decompose an image into a low-rank image containing the content, and a sparse image containing the artifacts(Bouwmans et al., 2018). RPCA is a state-of-the-art method that has been used both in background subtraction and intrinsic image decomposition (Yu, 2016). In addition, the pixel-wise mean of the input sequence is used for comparison as a worst-case solution that only attenuates artifacts.

We use the mean squared error (MSE), the structural similarity index (SSIM), and the peak signal-tonoise ratio (PSNR) as quality measures. 1,000 image sequences, each containing 9 images from a validation set, are used for evaluation. Figures 3, 4 and 5 show the average error for each model on varying lengths of input sequences.

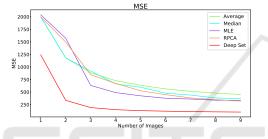


Figure 3: MSE for each method applied on varying image sequences of synthetic data.

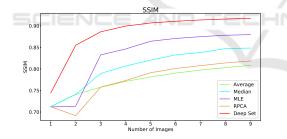


Figure 4: SSIM for each method applied on varying image sequences of synthetic data.

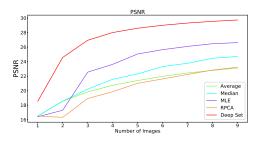


Figure 5: PSNR for each method applied on varying image sequences of synthetic data.



Figure 6: Sequence of four distorted images from the synthetic dataset with resulting reconstructions and error metrics.



Figure 7: Sequence of eight distorted images from the synthetic dataset with resulting reconstructions and error metrics.

Our evaluation shows that the Deep Set architecture has a consistently better performance compared to all other unsupervised methods over all metrics. As expected, the pixel-wise mean gives the worst results. Figures 6 and 7 illustrate the difficulty of the reconstruction for classical outlier removal methods. The artifacts overlap frequently and the underlying content is rarely seen uncorrupted. The figures both contain very complex illumination and specularities. Even when parts of the image do not contain artifacts such as shadows, occlusions, or specularities, the reconstruction is still ill-posed due to varying illumination. In figure 6, the statistical methods are unable to remove the overlapping occlusions, while Deep Set is able to extract the relevant content.

Since the encoder is applied on each image independently, it is reasonable to assume that the averaged embedding space of the encoders contains attenuated features of artifacts, similar to the average in the RGB color space. However, the result in figure 6 indicates that the decoder is able to extract the real content from the corrupted embedding. Moreover, the occlusions are removed, despite their overlapping in three out of four images. This implies that the architecture does not solely rely on a pixel-wise consensus, but also uses contextual information in each image.

Note that RPCA performs poorly on our synthetic dataset. This is likely due to the fact, that RPCA assumes sparse distortions. Since our image sequences are relatively small compared to other background subtraction tasks, many distortions are not considered sparse by RPCA.

Figure 7 shows a sequence, where the illumination distorts the homogeneous color of the book. Although it is impossible to extract the exact color, Deep Set is the only method able to generate an image with a homogeneous color. This requires a highlevel understanding of the image. We assume that the large receptive field enables Deep Set to understand the broader context of each image and makes it less prone to errors inherent in methods, which are based on pixel-wise statistics, e.g. mean, median or MLE (Weiss, 2001).

5.2 Evaluation on Real Data

We use the 40 image sequences from our test set for evaluation. All images have a resolution of 1024×1024 . We follow the same evaluation steps as for the synthetic data. Figures 8, 9 and 10 show the results of our evaluation.

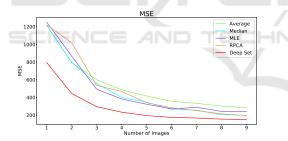


Figure 8: MSE for each method applied on varying image sequences of real data.

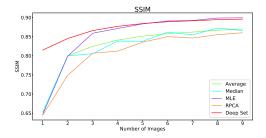


Figure 9: SSIM for each method applied on varying image sequences of real data.

The evaluation on the real input images shows that Deep Sets have the best performance with regards to

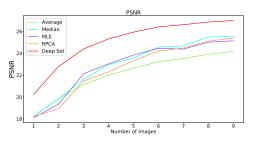


Figure 10: PSNR for each method applied on varying image sequences of real data.

MSE and PSNR. MLE gives slightly better results with regards to SSIM on longer input images. However, the examples in figure 11 and 12 show that no metric fully captures the quality of the reconstruction. In figure 11, the result of Deep Set has a much lower MSE error than all of the other methods, but has the same SSIM as MLE. In figure 12, RPCA has the result with the lowest MSE, although it contains more ghosting artifacts than the results of MLE and Deep Sets. Although the results of Deep Sets look promising, this suggests that MSE is not the most suitable metric for optimizing our architecture. The exam-



Figure 11: Sequence of four distorted images from the real dataset with resulting reconstructions, ground truth image, and error metrics.

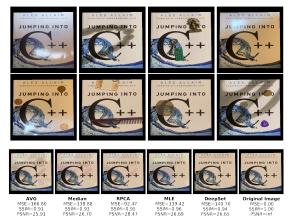


Figure 12: Sequence of eight distorted images from the real dataset with reconstructed images, ground truth image, and error metrics.

ples also show that outlier removal methods such as RPCA or median filtering, that are also used in background subtraction, can not remove varying illumination. The evaluation also confirms that one can compensate for the lack of training data (with only 60 image sequences available for training) using a synthetic dataset.

6 ABLATION STUDY

In our ablation study, we tested various depths for the encoder and decoder architecture. It is a tradeoff between reconstruction quality and memoryconsumption. The configuration shown in figure 2 is best suited for our use case. Further increasing the number of residual blocks for either component did not significantly improve the quality of the resulting model. However, the memory consumption increases significantly with the depth of the encoder, because the feature maps for each image in the sequence have to be computed. Reducing the number of residual blocks results in a worse reconstruction quality. Furthermore, we evaluated the effect of dilation in our residual blocks. Dilation significantly improves the quality of the reconstruction, without changing the number of parameters of the model, by increasing the receptive field. Our Deep Residual Sets therefore analyze a larger context of the images, which allows them to better distinguish between a distorted image patch and an undistorted one. Additionally, we tried adding and removing downsampling layers (adjusting upsampling layers accordingly). Increasing the number of downsampling layers reduces the quality of the reconstruction due to information loss. However, not using downsampling layers had no noticeable effect on the reconstruction quality, it only increased the memory consumption of the architecture. Memory consumption is a limiting factor for our architecture. It limits the batch size and maximum sequence length of our model during training. Additionally, it limits the maximum resolution our architecture can handle.

7 CONCLUSION AND FUTURE WORK

In this paper, we introduced a deep learning architecture, which can successfully learn to remove shadows, specularities, and occlusions from image sequences. The architecture uses residual blocks and the concept of Deep Sets(Zaheer et al., 2017). The architecture enforces permutation invariance and can be applied to dynamic input sequences and high resolution images. In section 4.3, we showed a memory-efficient method for applying our architecture to arbitrarily long image sequences, that is also suited for high resolutions, including streaming data, without an increase in memory consumption.

We created a synthetic dataset containing complex illumination, occlusions, shadows, and specularities with corresponding ground truth data. The synthetic dataset was initially created to establish a proof-ofconcept for our architecture and was later used for pre-training the model. Our evaluation shows that a supervised method can outperform unsupervised methods for outlier removal, background subtraction, and intrinsic image decomposition. Although the reconstruction is ambiguous and ill-posed, the model was still able to generate images that were visually consistent, see figure 7.

Furthermore, we evaluated our model on a real dataset. Deep Set was able to compete with the existing methods. We showed that one can compensate for the lack of a large dataset using synthetic data. The model was pre-trained on synthetic data and fine-tuned on the real data, resulting in a superior reconstruction compared to unsupervised methods. This method of pre-training on a large augmented dataset combined with fine-tuning on a small real dataset is especially helpful for use cases where it is hard or impossible to obtain large datasets. We have shown that Deep Sets are a simple and efficient method to improve on existing deep learning models in image restoration.

In future work, we are interested in applying Deep Sets to other computer vision tasks utilizing multiple images, such as super-resolution, background extraction, or panorama stitching. Introducing adversarial loss could further enforce visually coherent results, rather than exact reconstructions.

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